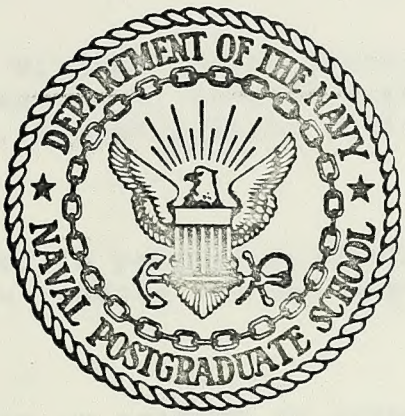
ESTIMATING BOUNDARY LAYER FLUXES FROM SHIPBOARD MEASUREMENTS OF DISSIPATIONS OF TURBULENT KINETIC ENERGY AND TEMPERATURE VARIANCE

William Edward Johnston

NAVAL POSTGRADUATE SCHOOL
Monterey, California



THESIS

Estimating Boundary Layer Fluxes from
Shipboard Measurements of Dissipations of Turbulent
Kinetic Energy and Temperature Variance

by

William Edward Johnston

Thesis Advisor: K. L. Davidson

March 1974

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William Edward Johnston
Lieutenant, United States Navy
B.S., Edinboro State College, 1965

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requirements for the degree of

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ABSTRACT

Velocity and temperature fluctuation measurements were made over the open ocean from instruments mounted on the R/V ACANIA. These data were examined to determine the validity of present formulations and prediction techniques.

Values of momentum flux, u_*^2, were inferred from the rate of dissipation of turbulent kinetic energy, ε. Dissipation values were obtained from spectral estimates and inner scale estimates. Values of u_* were examined for representativeness on the basis of the constant-flux assumption and by comparisons with other studies. The vertical variation of the dissipation rate was examined for possible effects of stability and wind-wave coupling.

The momentum flux, computed from spectra, supported the constant-flux assumption for neutral conditions. For periods of instability, the stability corrections applied to the vertical variation of ε resulted in the proper adjustments toward the predicted slope. The reductions in momentum transfer during periods of stable stratifications were consistent with wind-wave coupling effects described by Davidson. The shape of a spectrum of temperature fluctuations was in agreement with predictions.

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I. INTRODUCTION

The structure of turbulence in the marine boundary layer has become of increasing importance in naval systems design. To gain a better understanding of turbulence statistics, such as the spectral distribution of wind fluctuations, the effects of wind-wave coupling and the accuracy of present prediction expressions, personnel at the Naval Postgraduate School, Monterey, California have undertaken a study to obtain the shipboard observational data necessary for an accurate examination of these problems. The group consists of personnel from several departments; Meteorology, Mechanical Engineering, Oceanography and Physics, whose primary objective is to obtain observational data and then to evaluate and improve existing prediction techniques.

Several observational experiments have been conducted and were followed by data reduction and analyses periods. The second observational experiment is the one considered in this study and was conducted from 18 September 1973 to 22 September 1973. Meteorological measurements were made from the oceanographic research ship, the R/V ACANIA shown in Figure 1, in the vicinity of San Nicolas Island. Figure 2 illustrates the "near" ocean environment and the ACANIA's anchorage where the majority of measurements were taken.

Figure 1. The R/V ACANIA is operated by the Department of Oceanography, NPS.

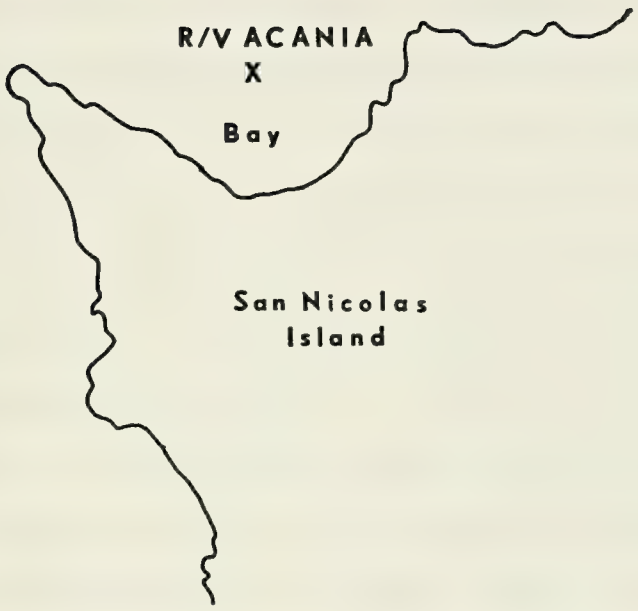


Figure 2. San Nicolas Island and ACANIA's Anchorage.

The meteorological measurements were of three different types. Two of these pertained to different scales of measurements and the third was of the influence of the moving platform on mean and turbulent measurements. The scales considered were the turbulent scale and that which is associated with the mean wind and thermal stratification.

The scope of this study is confined to turbulent fluctuations of velocity and temperature, although reference will be made to mean wind and thermal stratification measurements. The latter are important since they are required to relate to results from other experiments or for extrapolating to regions or conditions where turbulence measurements are not made. A nearly unique problem facing the Navy is that present expressions for the turbulent processes are empirical in nature and have only been previously validated, or at least tested, overland.

The purpose of this investigation is to test several expressions in the "near" ocean environment, interpret the results and evaluate existing turbulence expressions. To accomplish this, it was decided to concentrate the study on specific formulations. The formulations include (1) an evaluation of the constant flux layer (2) the variations of ε (the viscous dissipation of turbulent kinetic energy) with height and, where data permitted, (3) the variation of temperature fluctuations.

II. OBSERVATIONAL AND THEORETICAL CONSIDERATIONS

A. GENERAL BACKGROUND

This study represents one of the first attempts to make simultaneous, multiple-level observations over water from a ship. Previous measurements have been primarily overland or over water from near stable platforms. A study which closely approximates this experiment was described by Stegen, et al (1973). The measurements reported in that study were made from the Scripps Floating Instrument Platform (FLIP) during the Barbados Oceanographic and Meteorological Experiment (BOMEX). From FLIP, velocity and temperature measurements were made with a roving probe which cycled continuously between measurement stations located 2, 4, 7 and 12 meters above mean sea level. Results in the present study will be compared to those obtained by Stegen, et al, as well as to other contemporary studies.

The following paragraphs will provide a review of the theoretical considerations needed to interpret the data. From these considerations, the friction velocity (u_*) will be estimated from values of the dissipation of turbulent kinetic energy (ε) and ε will be obtained from spectra. For this reason we must examine both the turbulent kinetic energy balance expression and Kolmogorov's hypotheses.

B. TURBULENT BALANCE EXPRESSIONS

A general expression for the turbulent kinetic energy balance has the form

$$\frac{\partial}{\partial t}\left(\overline{\frac{V_i^2}{2}}\right) = -\overline{V_i V_j}\,\frac{\partial \bar{u}_i}{\partial x_j} + \frac{g}{T_o}\,\overline{V_i \theta}\,\delta_{i_3} - \varepsilon + \frac{\partial}{\partial x_j}\left[\overline{V_j\left(-\frac{P}{\rho} - \frac{V_i V_i}{2}\right)}\right] - \frac{\partial}{\partial x_j}\left[\bar{u}_j\,\overline{\frac{V_i V_i}{2}}\right] \qquad (1)$$

If all eddy transports except those along the vertical are neglected, the turbulent kinetic energy balance can be expressed as

$$\frac{\partial}{\partial t}\left(\overline{\frac{V_i^2}{2}}\right) = -\overline{V_3 V_i}\,\frac{\partial \bar{u}_i}{\partial x_3} + \frac{g}{T_o}\,\overline{V_i \theta}\,\delta_{i_3} - \varepsilon - \frac{\partial}{\partial x_3}\left[\overline{V_3\left[\left(\frac{V_i V_i}{2}\right) + \frac{P}{\rho}\right]}\right] \qquad (2)$$

The time variation of turbulent kinetic energy is thus seen to depend on four processes represented by the four terms on the right hand side of Equation (2). The first represents production of turbulent kinetic energy by the interaction of the Reynolds stress with the mean shear flow. The second represents turbulent kinetic energy released or gained due to the work of vertical motions against the effects of buoyancy. The third represents viscous dissipation of turbulent kinetic energy. The final term represents both pressure work and the flux divergence of turbulent kinetic energy due to transfer by turbulent motion.

To obtain those expressions normally used for estimating the shear stress or eddy flux ($-\overline{v_1 v_3} = u_*^2$) on the basis of turbulent kinetic energy balance, the following assumptions and definitions are made:

i) assume that the turbulent kinetic energy is in a statistically steady state

$$\frac{\partial}{\partial t}\left(\frac{\overline{v_i^2}}{2}\right) = 0$$

ii) conditions are horizontally homogeneous for the irregularity fields (i.e., spatial variations of mean fluctuations are taken to be negligible over distances comparable to the largest scales of interest in the analysis).

$$\frac{\partial}{\partial x_1}(\quad) = \frac{\partial}{\partial x_2}(\quad) = 0$$

iii) conditions are near neutral

$$\frac{g}{T_o}\overline{v_3\theta} \cong 0$$

iv) define the coordinate system so

$$\bar{u}_2 = \bar{u}_3 = 0$$

The above assumptions and definitions lead to the following turbulent energy balance expression

$$-\overline{v_1 v_3}\frac{\partial \bar{u}_1}{\partial x_3} = \varepsilon + \frac{\partial}{\partial x_3}\left[\overline{v_3\left\{\frac{v_1^2 + v_2^2 + v_3^2}{2} + \frac{p}{\rho}\right\}}\right] \quad (3)$$

Furthermore, if the divergence terms are negligible, Equation (3) becomes

$$-\overline{v_1 v_3}\frac{\partial \bar{u}_1}{\partial x_3} = \varepsilon \quad (4)$$

which states that mechanical production of turbulent kinetic energy equals dissipation of turbulent kinetic energy.

Equation (4) can be rewritten as

$$u_*^2 \frac{\partial \bar{u}}{\partial x_3} = \varepsilon \qquad (5)$$

where $u_*^2 = -\overline{v_1 v_3}$. For neutral conditions in a constant-stress boundary layer the following is an accepted expression for the wind shear

$$\frac{\partial \bar{u}}{\partial x_3} = \frac{u_*}{kz} \qquad (6)$$

where k is Von Karman's constant and z is the height. Combining Equations (5) and (6) yields the following estimate for u_* based on measurements of ε at known height z.

$$u_* = (\varepsilon z k)^{1/3} \qquad (7)$$

Equation (7) can be used to both estimate the value of the momentum flux, u_*^2, and to examine if it is constant with respect to height, the constant-flux assumption.

Table I provides the momentum flux calculations presented by Stegen, et al with ε values derived from time derivatives of the velocity fluctuations. These values will be compared to those obtained from shipboard measurements to establish the validity of the expressions and assumptions used in this study.

TABLE I

Results of Momentum-Flux Calculations.[1]

Height (m)	$kz\varepsilon$ ($cm^3 sec^{-3}$)	u_* ($cm\ sec^{-1}$)	u_* (corrected) ($cm\ sec^{-1}$)
11.69	4.02×10^3	15.9	14.0
6.70	6.86×10^3	19.0	17.3
3.89	6.36×10^3	18.5	17.4
2.39	6.03×10^3	18.2	17.4

[1]Results taken from Stegen, et al (1973)

Equation (7) can be rewritten as

$$\text{Ln } \varepsilon = -\text{Ln } z + \text{Ln } u_*^3/k \qquad (8)$$

Therefore a plot of Ln z versus Ln ε should yield a straight line with -1 slope. The intercept of this line with the Ln z axis, z = 1, will yield the estimate of u_*. A plot of this shown by Stegen, et al appears in Figure 3. Deviations from this particular relation could be interpreted for possible deviation from the constant-flux assumption or for influence of wind-wave coupling or non-neutral stratifications.

C. SIMILARITY EXPRESSIONS

The parameter ε can be estimated on the basis of similarity expressions for the inertial subrange. According to Kolmogorov's second hypothesis, the inertial subrange is a region (in wave number space) where there is negligible dissipation of energy and where inertial energy transfer to higher wave numbers is the dominate feature.

Figure 4 from Lumley and Panofsky (1964) depicts the inertial subrange considering spectral energy transfers.

Based on a dimensional analysis Kolmogorov's second hypothesis yields the following functional relation

$$E(k) = c\varepsilon^{2/3}k^{-5/3}$$

where E(k) represents the three-dimensional energy density, k is the wave number and c is an empirical constant.

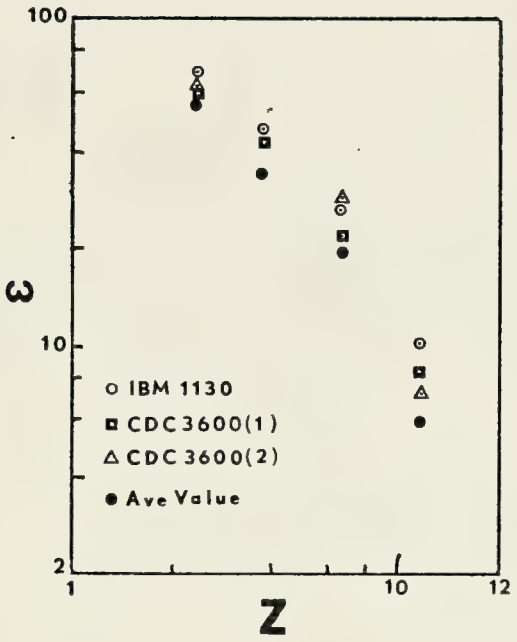


Figure 3. Measured Values of ε vs z, the Height Above the Mean Sea Surface (after Stegen, et al).

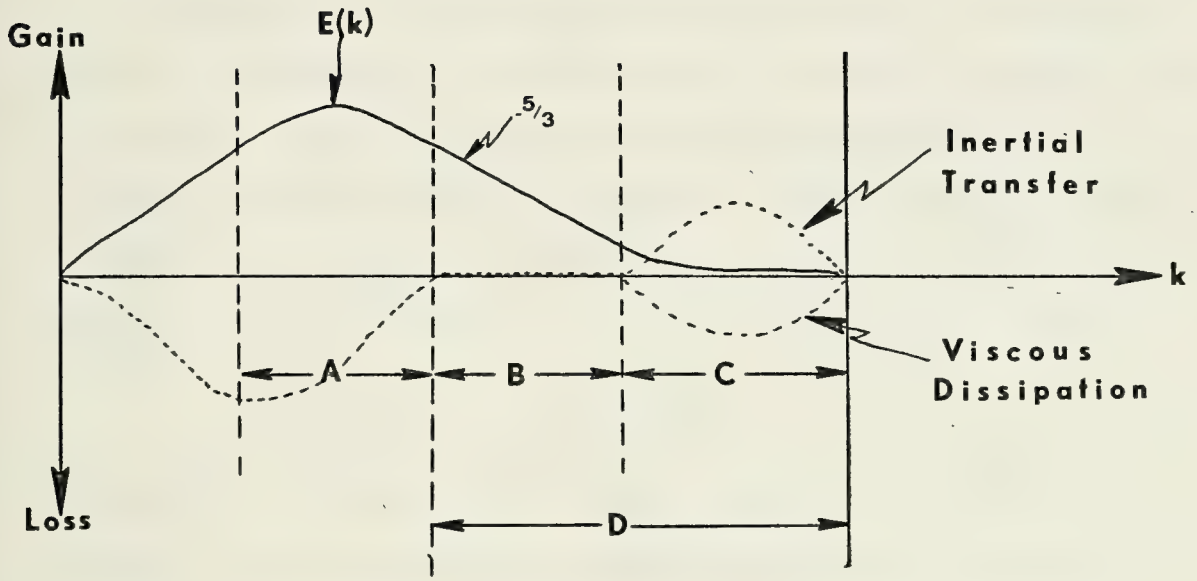


Figure 4. A Schematic Drawing Showing Spectral Transfer and Illustrating (A) Energy Containing Region (B) Inertial Subrange (C) Dissipation Range and (D) Universal Equilibrium Range.

Unfortunately, E(k) is impossible to measure. It can be shown, however, that the one-dimensional energy density, $\phi_{11}(k)$, which can be measured, also has the form

$$\phi_{11}(k) = \alpha\varepsilon^{2/3}k^{-5/3} \qquad (9)$$

where α = constant.

Furthermore, measurements at the scales of interest have to be made at a fixed point in the flow and the spectra therefore are obtained for temporal frequency, f. In order to use Equation (9), time and space scales must be related using Taylor's (1938) "frozen turbulence" hypothesis

$$k = 2\pi f/\bar{U}$$

where $\bar{U}$ is the mean wind speed, measured by a cup anemometer. The term "frozen turbulence' implies that the turbulence remains unchanged during the time required for it to sweep past the probe.

The following form of Equation (9) is often utilized and will be here,

$$f\phi_{11}(f) = k\phi_{11}(k) = \alpha\varepsilon^{2/3}k^{-2/3} \qquad (10)$$

The parameter ε will be obtained from the spectra using Equation (10). The ε values obtained from simultaneous, multiple level measurements will then be used to estimate the value of the momentum flux, u_*^2, from Equation (7).

There is another way of estimating ε based on the scale associated with the upper limit of the inertial subrange. If the spectrum is in statistical equilibrium it is independent of the source of the turbulence and depends only on ε, γ and k. A dimensional analysis yields the following expression for the inner scale, l_o

$$l_o = (\gamma^3/\varepsilon)^{1/4} \qquad (11)$$

where k_s (= $2\pi l_o/\bar{u}$) is the dissipation wave number and γ is the kinematic viscosity of air. The dissipation wave number can be obtained from spectra which show scale separation between pure inertial transfer (-5/3 regions) and the viscous dissipation region. Dissipation of turbulent kinetic energy can then be obtained from Equation (11) and compared to those obtained from Equation (10) to establish greater confidence in the spectral estimate.

D. FURTHER THEORETICAL CONSIDERATIONS

Although the expressions previously described are based on accepted and consistent theories, there are several serious assumptions which must be considered in applying them to observational data. In many instances the theory is empirical and the formulating analyses were based on overland data. A recent effort in turbulence theory has been to prove or disprove the validity of overland formulations for non-neutral conditions or over water regimes where the wave influence may be important. The latter has been described by Davidson (1974).

In developing the turbulent kinetic energy balance, given by Equation (3), the existence of neutral conditions was a critical assumption. For non-neutral stratifications, Equation (7) would include a buoyancy term and be of the form

$$\varepsilon = \frac{u_*^3}{kz} \left[\phi_1\left(\frac{z}{L}\right) - \frac{z}{L}\right] \qquad (12)$$

or

$$\varepsilon = \frac{u_*^3}{kz} \phi_2(Ri)$$

where $L = -\bar{T}u_*^3/gk\overline{V_3\theta}$ = Monin-Obuhkov Length; $\overline{V_3\theta}$ = heat flux,

Ri = Richardson Number,

ϕ_1 = empirical function of $\frac{z}{L}$,

ϕ_2 = empirical function of Ri.

For the non-neutral case, the expression corresponding to Equation (8) becomes

$$\text{Ln } \varepsilon = -\text{Ln } z + \text{Ln } \phi_2(Ri) + \text{Ln } \frac{u_*^3}{k} \qquad (13)$$

Possible deviations from the constant flux assumption or wind wave coupling influence exhibited by spectral results could be examined by testing overland expressions for $\phi_2(Ri)$. A stability correction could then be applied for periods of non-neutral stratifications. A possible effect of the instability on the predicted plots of Ln ε versus Ln z is illustrated in Figure 5.

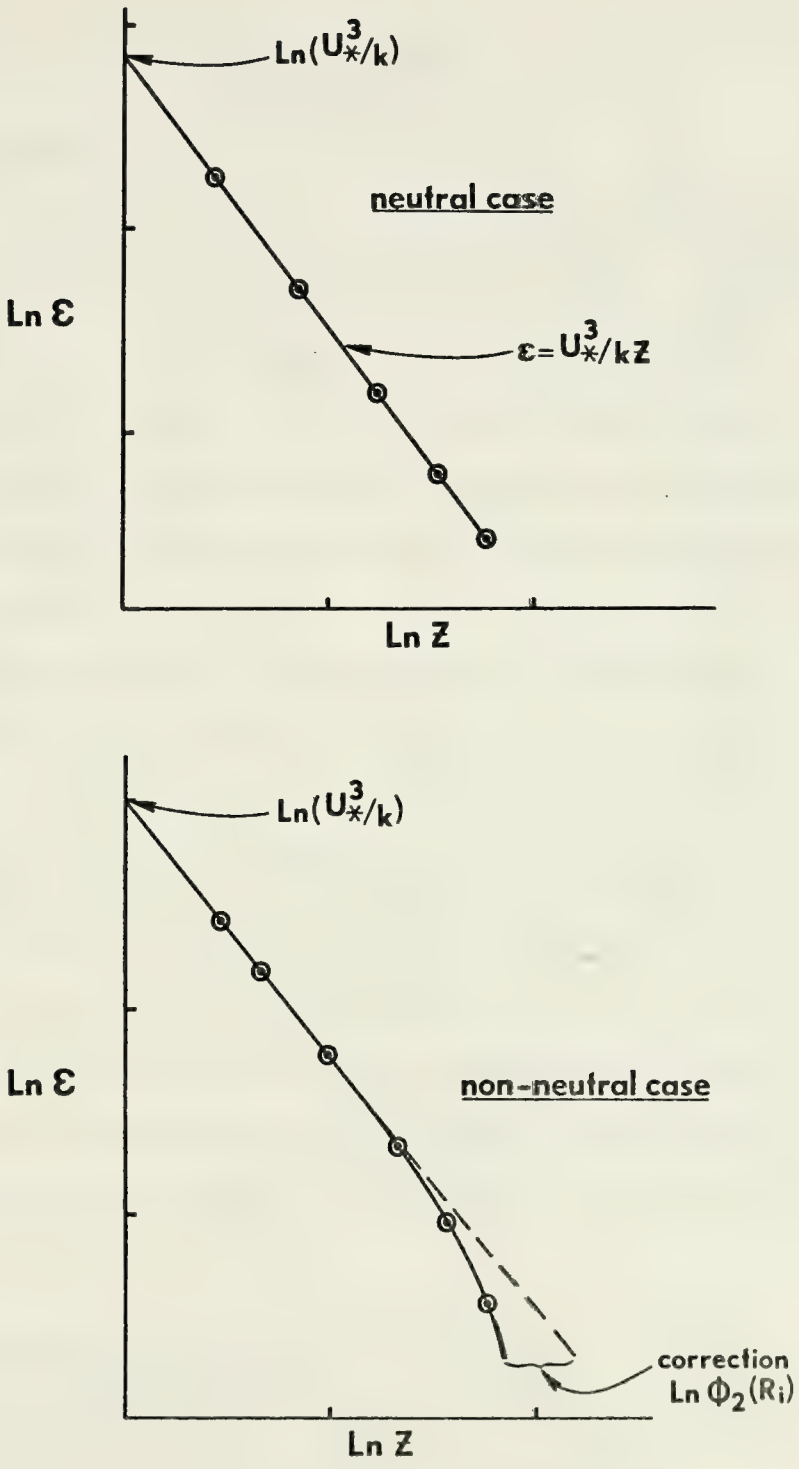


Figure 5. An Illustration of a Possible Effect of Stability on the Variation of ε with Height.

III. OBSERVATIONS

A. THE EXPERIMENT

The data considered in this study were obtained from measurements made aboard the R/V ACANIA, which is operated by the Department of Oceanography of the United States Naval Postgraduate School. As previously stated, San Nicolas Island was the experimental site and the majority of data were collected while the ship was at anchorage near the northwest tip of the island. Additional data were collected while the ship was enroute between Monterey and San Nicolas Island and also while the ship was transiting to the west side of the island. Since the data collected from anchorage comprise the largest percentage of successful runs and represents all stability conditions, data runs selected for analysis in this study are primarily anchorage data. Table II is a listing of the various data runs examined. Figure 6 shows the ship's track in the vicinity of San Nicolas Island and Figure 7 shows the route to and from the island.

B. DESCRIPTION OF EQUIPMENT AND MEASUREMENTS

Figure 8 shows the sensor placement at various levels along with the variables measured at each level.

1. Velocity Measurements

Velocity fluctuation measurements were made at three levels on the forward mast and one level on a single bow

TABLE II

Data Periods Considered in This Study

Date	Time	Digital Channel	Parameter
20 Sept. 73	1103-1138	1	u_1' [1]
		2	u_2'
		3	u_3'
		4	u_4'
20 Sept. 73	2008-2018	1	u_1'
		2	u_3'
		3	u_4'
		4	T_4'
		5	T_B'
		6	upper level lateral acceleration
		7	upper level vertical acceleration
		8	upper level vertical acceleration (integrated)
20 Sept. 73	2023-2053	1	T_4'
		2	u_3'
		3	u_4'
		4	u_1'

[1] The subscript refers to the level at which the measurement was made. Level 1 is the uppermost level.

TABLE II (continued)

Date	Time	Digital Channel	Parameter
20 Sept. 73	2323-2341	1	u_1'
		2	u_2'
		3	u_3'
		4	upper level fore-aft acceleration
		5	upper level lateral acceleration
		6	T_4'
		7	upper level vertical acceleration (integrated)
		8	upper level vertical acceleration
21 Sept. 73	0637-0652	1	upper level fore-aft acceleration
		2	u_3'
		3	u_1'
		4	T_4'
		5	T_B'
		6	upper level vertical acceleration
		7	upper level lateral acceleration
		8	upper level lateral acceleration (integrated)

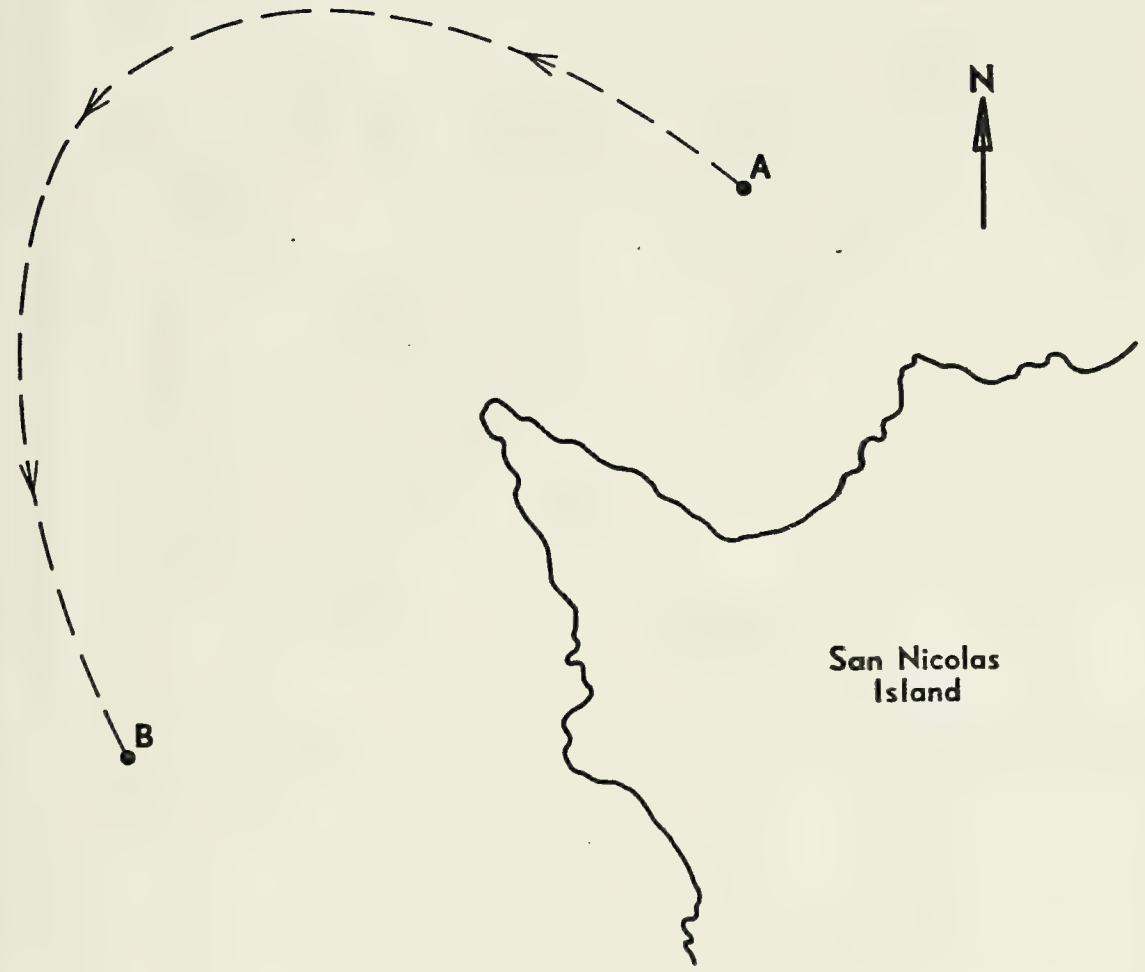


Figure 6. ACANIA's Track in SNI Area.

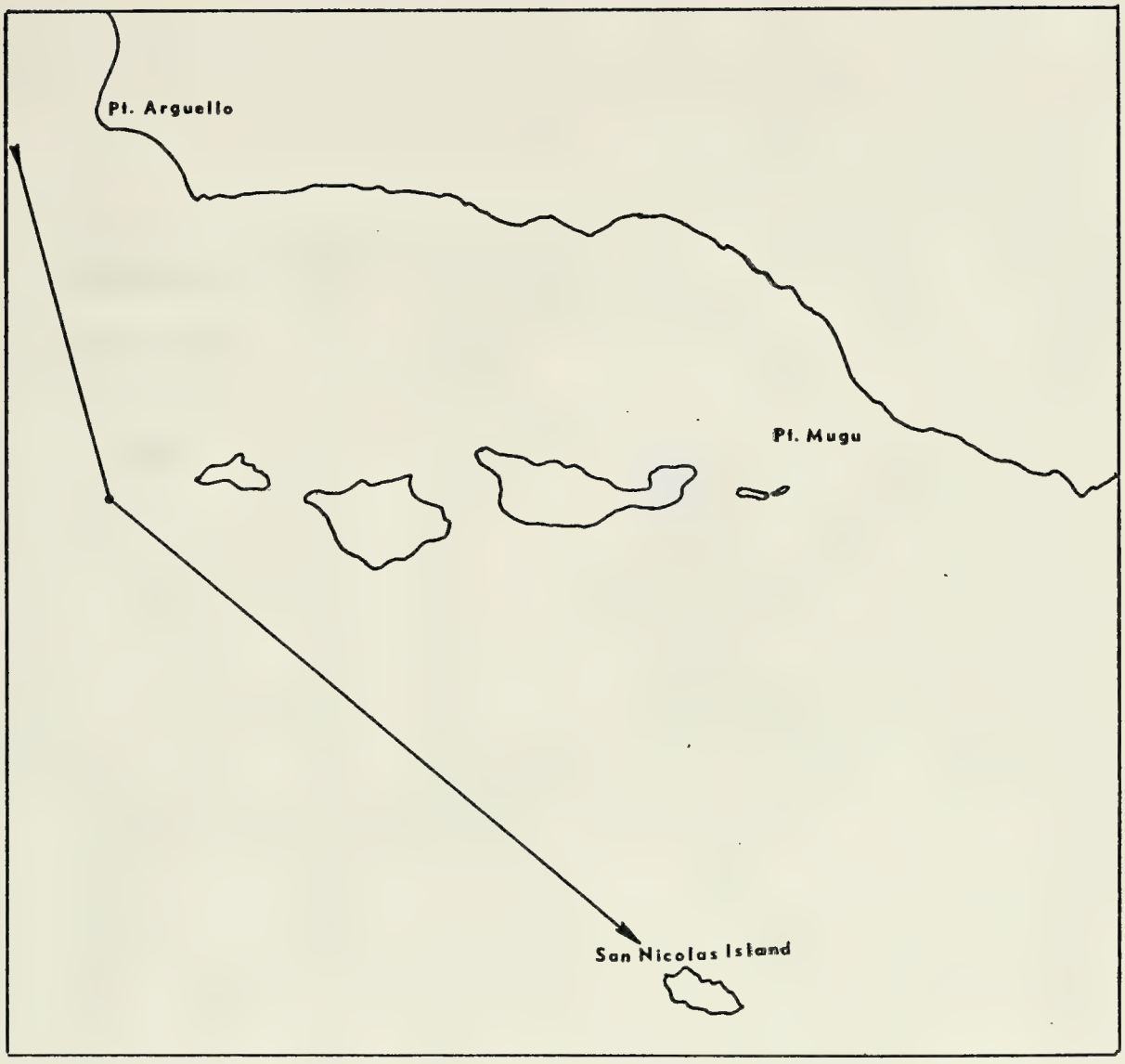


Figure 7. The San Nicolas Island Region.

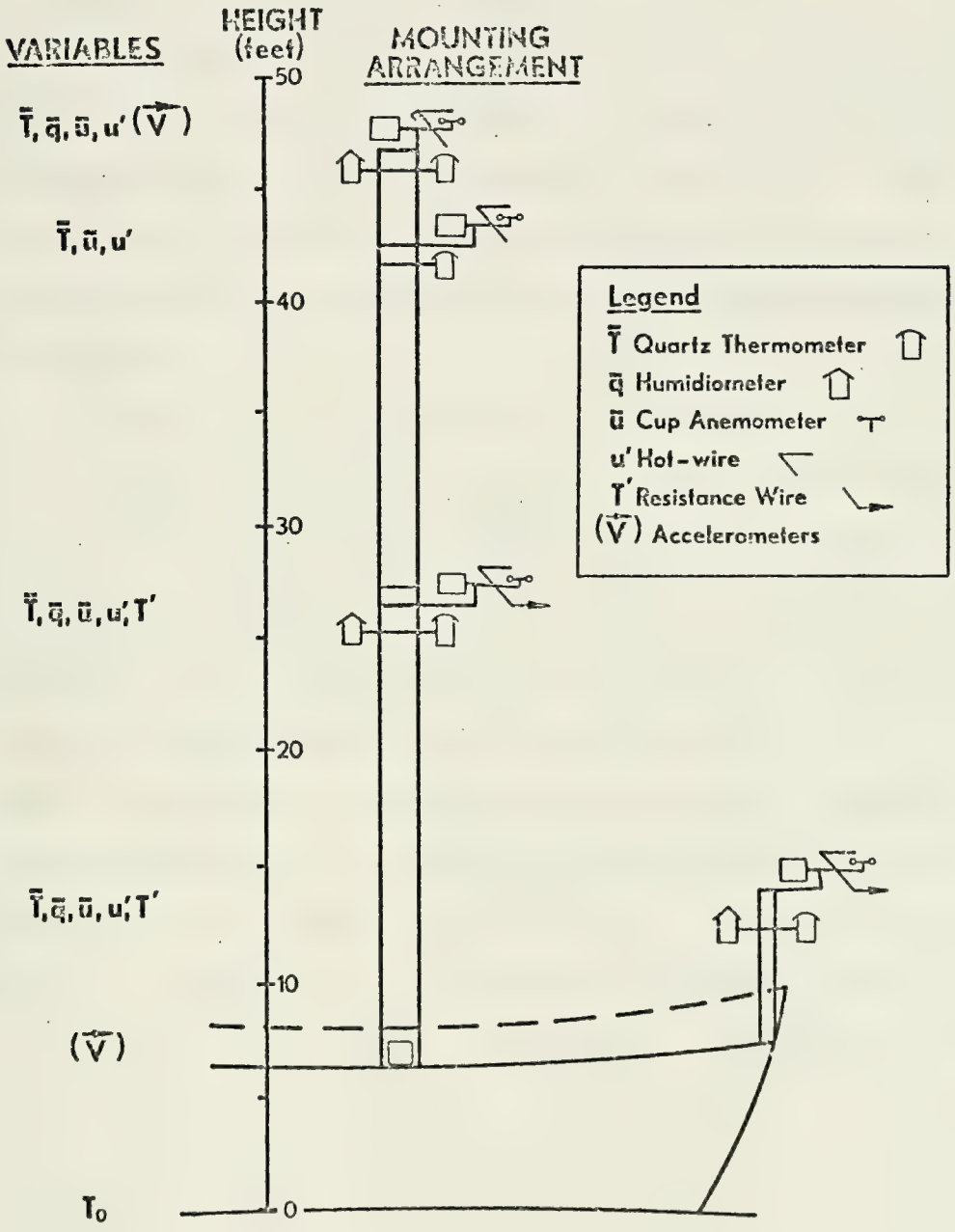


Figure 8. Mounting Arrangements

mast as shown in Figure 8. Thermo-Systems (TSI) Model 1210 probes with sliding support shields were selected for these measurements. The sensor consisted of a platinum coated tungsten wire 0.00015 inches in diameter and 0.060 inches long, small enough to resolve the viscous dissipation scale without needing to apply wire length corrections. The wire was fitted with plated ends for isolating the sensing area and thereby minimizing flow disturbance.

Electronics associated with each probe were a TSI Model 1054B Linearized Anemometer, a TSI Model 1056 Variable Decade Module and a Model 1057 Signal Conditioner. Schematics of the anemometer circuits appear in Appendix A. The anemometer had a linear frequency response from DC to 10 KHz and the variable decade module operated with a 0-60 ohm range. The signal conditioner had a linear frequency response from DC to 400 KHz and permitted voltage suppression in one volt steps from 0-29 volts. The voltage output from the conditioner was recorded on magnetic tape.

Sensor placement required 200 foot cables instead of the usual 15 foot cables. This resulted in a decrease in system frequency response but the decrease had little effect in the frequency band of interest. Ten probes were available for the experiment and they were placed into four groups. Each group of probes was calibrated with separate cables and electronics which permitted a complete system calibration for each of the four sensing levels.

The calibration was completed with a manometer and a TSI Model 1125 Calibrator shown in Figures 9 and 10. Empirical relations used in interpreting the hot wire signals are presented in Appendix B along with the computer code used to evaluate these measurements and resultant calibration curves for each probe.

The performance of the hot-wire system was excellent throughout the experiment. Only one probe failure was experienced despite continued probe exposure during the data gathering period.

2. Temperature Measurements

Temperature fluctuation measurements were made at two levels on the forward mast of R/V ACANIA as shown in Figure 8. Electronics used were TSI Model 1044 Temperature Modules. The unit power supply consisted of six volt batteries. It can be utilized to make both temperature and ΔT measurements. The temperature module is designed for measurements of temperature variations down to 0.001°C at frequencies up to 1 KHz. The schematics for the Model 1044 Temperature Module are shown in Appendix C.

Probe failure occurred at the beginning of the first data run and to permit temperature measurements to continue the probe unit was fitted with a 60 ohm platinum wire sensor.

3. Parallel Measurements

Mean measurements of the wind speed, temperature and relative humidity have been described by Cavanaugh

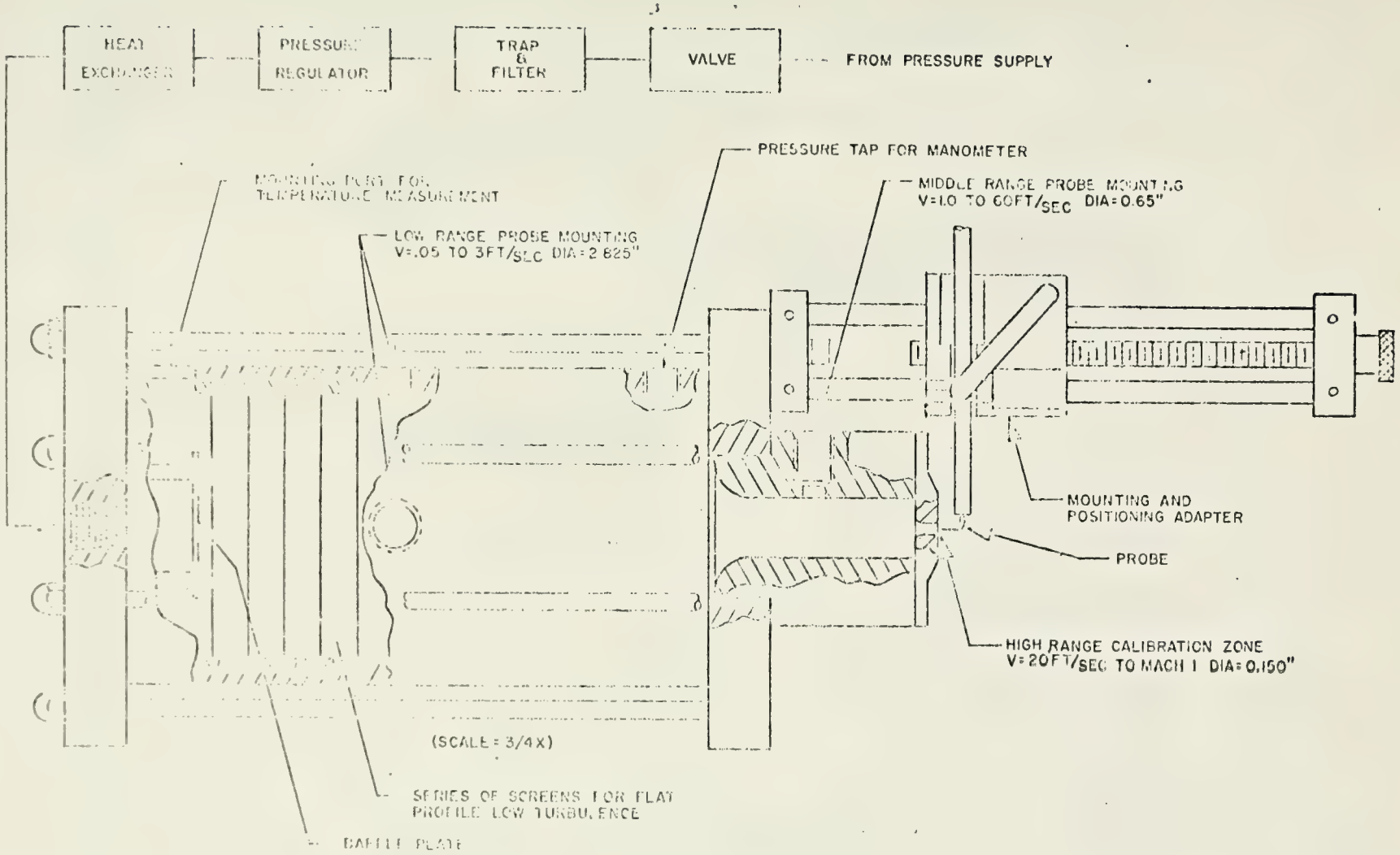


Figure 9. Probe Calibrator

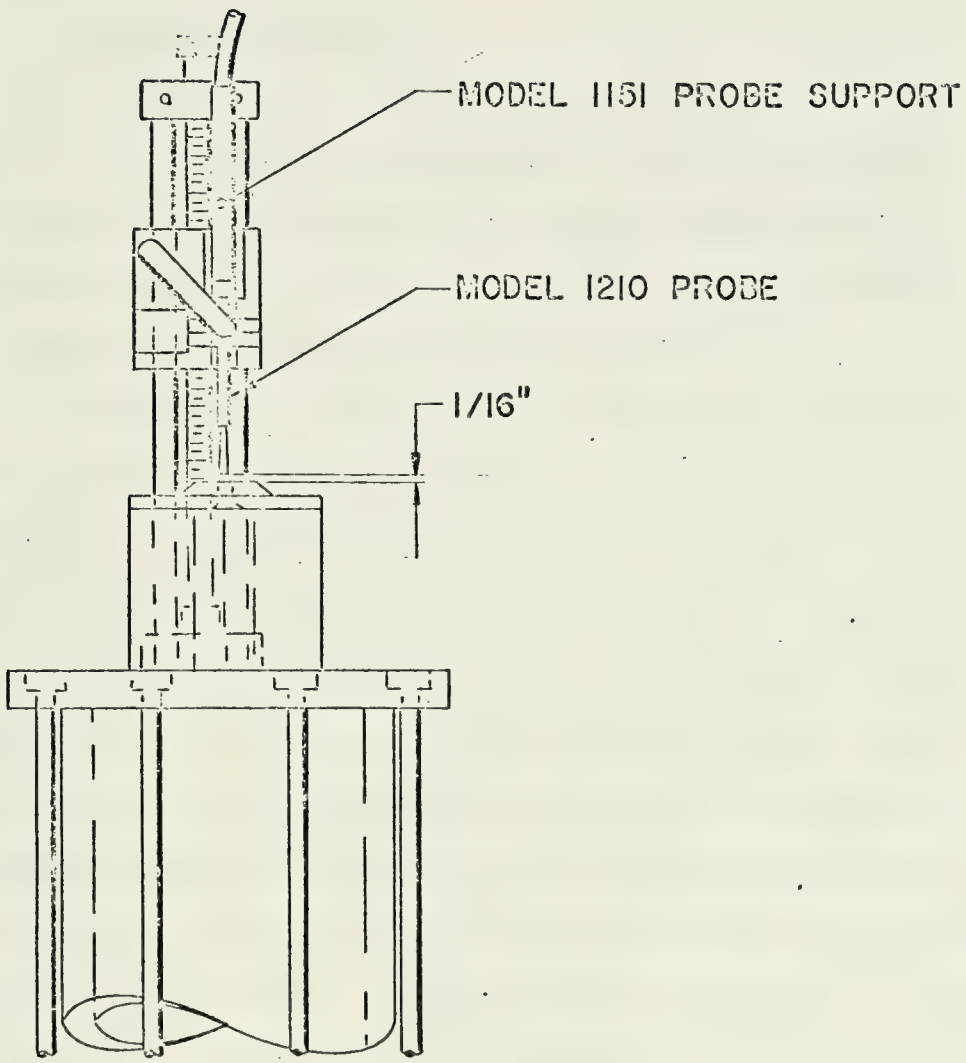


Figure 10. Vertical Probe Mounting with TSI Calibrator.

(1974). Measurements of ship's motion have been described by Welsh (1974).

C. SIGNAL PROCESSING AND RECORDING

1. Analog Recording

All data were recorded simultaneously in analog form with a 14 channel Sangamo Model 3562 FM Recorder. All recordings were made at a recording speed of 7 1/2 inches per second. At this recording speed the recorder had a frequency range from DC to 25 KHz.

A schematic diagram of the complete recording system is shown in Appendix D. The amplifier and suppressor combination in series with the sensor electronics and recorder channels were necessary to improve the signal to noise ratio of the inputs. The hot-wire signals were high pass filtered at 2 Hz during the majority of the runs. Two data runs were made without the filter to permit low frequency correlation between the velocity signal and ship's motion. The results of this correlation are discussed by Welsh (1974). The temperature signals were low pass filtered at 500 Hz. In addition to the signal recordings, a voice track was utilized to record observations pertinent to the data runs. Constant monitoring of amplified and preamplified signals was performed with an oscilloscope to evaluate the signals and to insure that the signal would not exceed amplifier or recorder input limits.

2. Real Time Analysis

Real time analysis was accomplished using a Spectral Dynamics Corporation (SD) Model SD301C Real Time Analyzer. This unit was used in conjunction with a Model SD309 Ensemble Averager, a Model 13116-2A X-Y Display Oscilloscope and an X-Y plotter to provide an instantaneous evaluation of the hot wire and temperature signals. The equipment allowed positive determination that measurements were sufficient to define the inertial subrange. A system operation diagram is provided in Appendix E along with several of the X-Y plots obtained from the real time analysis.

IV. DATA REDUCTION AND ANALYSIS

A. PRELIMINARY ANALYSIS

The analog tapes were played on a strip chart recorder to permit initial evaluations of the data. From this, data periods were chosen for subsequent reduction and analyses. This preliminary analysis disclosed a recording problem that had previously gone unnoticed. A periodic tape transport vibration had occurred due to the 7 1/2 ips gear drive and this obliterated the recorded signal. Fortunately, there were sufficient time intervals between vibrations to permit 20 minute data records to be obtained. It was from these data sections that the periods listed in Table II were obtained.

The difficulties encountered in making the temperature fluctuation measurements, as described in Section III, were evident in the strip chart recordings. The temperature data either failed to show sufficient signal strength or displayed a DC drift which rendered them impossible to digitize. An example of the two cases is shown in Figure 11.

The paucity of temperature data led to a focusing of attention on the velocity fluctuation measurements. The criteria for selection of subsequent data periods for inclusion in the reduction and analysis phase consisted of: (1) signal strength (2) averaging time (3) DC drift rate

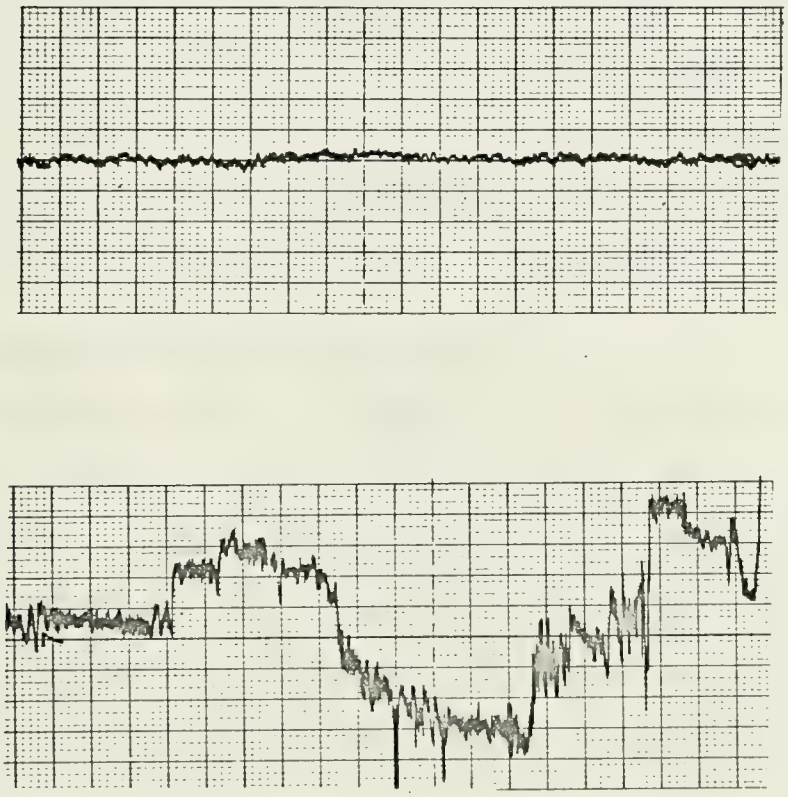


Figure 11. Inadequate Temperature Signals Showing (A) Insufficient Signal Strength and (B) DC Drift.

and (4) availability of mean profiles. Sufficient signal levels were required to minimize amplification during the analog-to-digital conversion process. Twenty minute data runs proved sufficient to permit ample averaging time for Fast Fourier Transform (FFT) calculations. DC drift was kept at a minimum to permit ease in digitization and to allow greater confidence in the data samples. Finally, data periods were selected to correspond to times when mean wind information was available. A typical signal meeting the above mentioned criteria is shown in Figure 12.

B. ANALOG-TO-DIGITAL CONVERSION

Analog-to-digital conversion was performed on a hybrid computer system located on the fifth floor of Spanagel Hall at NPS. The hybrid system consists of an analog computer, COMCOR Ci 5000, interfaced electrically with a digital computer, XDS 9300. A detailed discussion of the operation of this computer facility was given by McKendrick (1972) which should be referred to for additional information. A block diagram, provided in Figure 13, illustrates the analog-to-digital conversion sequence followed in this study.

C. SEVEN-TRACK TO NINE-TRACK CONVERSION

The analog-to-digital conversion process generated seven-track octal base data samples written on digital tape. The computer used to analyze the digital data was an IBM

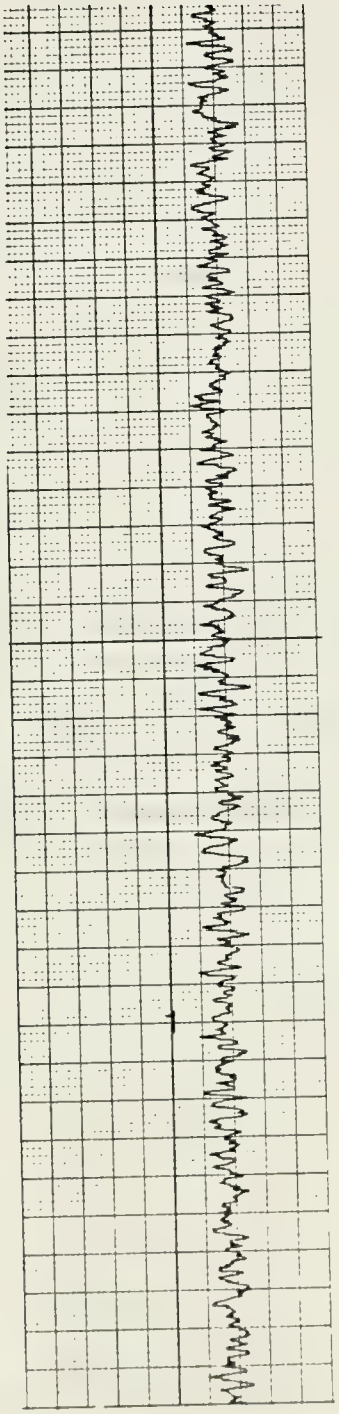


Figure 12. Typical Velocity Signal.

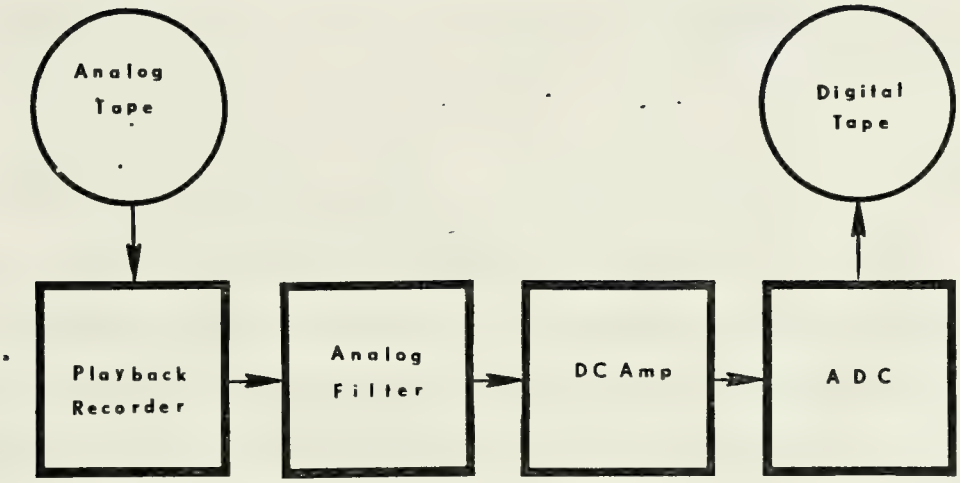


Figure 13. A-D Conversion Procedures.

360/67 computer. This computer utilizes nine-track hexidecimal based digital samples so a conversion between the seven-track and nine-track systems was necessary. A discussion of the procedures necessary for making the proper conversion to the nine-track hexidecimal based system are described in Naval Postgraduate School Computer Center Technical Note #0211-08. The two primary programs involved in this conversion are the TAPEOUT and CONVERT programs. These programs along with a description of digital tape operations are discussed in Appendix F.

D. DIGITAL ANALYSES PROGRAMS

Fast Fourier Transform (FTOR) and spectral analysis (SCOR) programs were available in the IBM 360/67 subroutine library. The following description of the FFT program package was taken from McKendrick. The programs were written by J. F. Garett and J. R. Wilson while students at the Institute of Oceanography at the University of British Columbia. The "OCEAN" subroutines of the UBCFTOR program instructs the IBM 360 to read the input tape, one block at a time, compute the FFT of the data block and then store the resulting Fourier coefficients on the output tape. The computer printout for the FTOR program is a listing of each digital channel and the Fourier coefficients produced. An example of this output is shown in Figure 14.

With these coefficients, the UBCSCOR program is used to compute the spectrum for a given channel, or the cross

SUMMARY COEFFICIENTS FOR 2413, 1TH BLOCK OF 256 SAMPLES
IN THIS BLOCK PARITY ERRORS ON TAPE = 0,ALL ONES NOT FOUND IN CHANNEL 1 0 TIMES

K	CHANNEL	NAME	UNITS	CAL.FACTOR
1	1	T' LEVEL 4	DEG/SEC	1.00E 00
2	2	U' LEVEL 3	M/SEC**2	1.00E 00
3	3	U' LEVEL 4	M/SEC**2	1.00E 00
4	4	U' LEVEL 1	M/SEC**2	1.00E 00

LAST HARM	CHANNEL 1 REAL	CHANNEL 1 IMAG	CHANNEL 2 REAL	CHANNEL 2 IMAG	CHANNEL 3 REAL	CHANNEL 3 IMAG	CHANNEL 4 REAL	CHANNEL 4 IMAG
0	-1.56E 05	0.0	1.40E 06	0.0	-1.25E 05	0.0	-5.25E 05	0.0
4	-5.54E 03	-1.31E 04	-2.44E 05	3.88E 05	-7.07E 04	-2.16E 05	-1.92E 05	3.26E 05
8	-4.47E 03	-3.63E 02	-1.59E 05	-2.56E 05	-6.11E 04	-5.23E 04	-6.18E 04	2.27E 05
12	-9.31E 02	4.83E 03	2.53E 05	-5.08E 04	-6.62E 04	-9.24E 04	-1.90E 04	5.51E 04
16	-6.35E 03	1.06E 04	7.30E 04	-5.00E 04	1.24E 05	-9.20E 04	-1.15E 04	5.84E 04
20	4.22E 03	-7.57E 03	-9.32E 03	-1.52E 04	4.32E 04	-6.24E 04	-1.58E 04	9.11E 04
24	1.79E 03	5.52E 02	2.39E 03	-2.00E 04	4.31E 04	3.45E 04	1.03E 04	7.76E 04
28	1.62E 01	-4.72E 02	3.14E 04	-9.99E 03	1.36E 04	5.61E 03	-8.86E 03	7.23E 03
32	-1.72E 03	-4.93E 02	1.10E 04	-6.41E 04	1.39E 04	-1.31E 04	1.06E 04	5.89E 04
36	2.56E 03	-3.58E 03	-8.52E 03	7.55E 04	-3.51E 04	2.04E 04	1.85E 04	1.41E 04
40	3.07E 03	-2.26E 03	2.81E 04	-8.77E 03	-7.81E 03	-3.52E 04	-3.13E 04	1.87E 04
44	-1.13E 02	-4.09E 00	6.37E 03	2.94E 04	4.14E 04	-3.41E 04	1.23E 04	3.46E 03
48	-2.18E 03	-3.49E 03	-2.08E 03	-1.12E 03	-1.18E 04	2.47E 03	-1.34E 04	1.52E 04
52	2.76E 03	-3.72E 03	3.00E 04	2.07E 04	1.83E 03	-3.21E 04	-6.92E 03	1.54E 04
56	6.08E 01	-2.01E 03	2.29E 04	1.25E 04	3.41E 04	-2.18E 04	-2.14E 04	-2.79E 02
60	2.67E 02	-6.52E 03	-8.08E 03	4.34E 04	2.92E 02	-3.26E 04	-2.45E 04	1.80E 04
64	9.88E 02	8.05E 03	2.45E 04	-1.41E 04	3.10E 03	2.47E 03	-9.02E 03	2.11E 04
68	1.49E 03	-2.59E 02	-1.69E 02	-2.21E 04	4.23E 04	-1.85E 04	6.84E 03	2.25E 04
72	4.66E 02	-1.22E 02	-1.48E 04	5.91E 02	-1.00E 04	-1.04E 04	1.35E 03	1.35E 04
76	4.41E 02	2.49E 02	1.34E 04	1.58E 03	-3.05E 03	1.19E 04	-2.05E 04	4.39E 03
80	-1.62E 02	1.82E 03	-4.53E 03	-7.76E 02	2.98E 04	-2.37E 04	5.07E 03	3.22E 03
84	8.91E 02	-9.66E 02	-7.82E 02	-1.70E 04	-1.38E 04	-2.30E 04	-1.13E 04	-5.94E 03
88	2.57E 03	1.52E 03	-5.29E 03	6.08E 03	1.42E 04	-3.25E 03	-4.61E 03	8.08E 03
92	-2.94E 03	-8.27E 02	-2.15E 04	-2.96E 04	1.73E 04	-4.81E 03	-1.85E 03	-7.31E 03
96	1.39E 03	-2.32E 03	3.23E 04	2.51E 04	2.32E 03	-2.96E 03	-2.49E 04	2.30E 03
100	-1.73E 03	-1.30E 02	-8.52E 03	3.14E 03	-5.40E 03	-1.52E 04	-1.46E 04	2.52E 03
104	1.81E 03	1.66E 03	-9.77E 03	-1.15E 03	2.33E 04	-1.87E 04	-1.59E 04	7.63E 03
108	-1.31E 03	2.20E 02	-5.00E 03	4.68E 03	2.23E 04	5.88E 03	-1.37E 04	1.36E 04
112	2.84E 03	-1.86E 03	1.10E 04	1.21E 03	1.02E 04	4.38E 03	-3.32E 03	1.25E 03
116	2.44E 03	1.31E 03	-5.53E 04	1.33E 03	-1.83E 04	-1.10E 04	-6.95E 03	1.19E 03
120	-1.17E 03	5.24E 02	-2.71E 04	-6.69E 03	3.68E 04	-8.05E 03	-1.81E 04	1.22E 04
124	1.88E 03	-2.50E 03	2.09E 04	1.20E 04	3.30E 04	7.29E 03	3.71E 02	1.14E 04
128	6.21E 02	-3.05E 02	-2.59E 04	-1.25E 04	7.53E 02	-8.00E 03	5.61E 03	-5.03E 02

COEFFICIENTS FOR BLOCK 1 WRITTEN IN FILE 1 ON OUTPUT TAPE

Figure 14. FTOR Output.

spectrum between a pair of channels, depending on what is selected by the user. The output of the SCOR program consists of a tabular computer printout, as shown in Figure 15, and a graphical plot of the spectrum versus frequency as shown in Figure 16. Appendix G of this thesis contains the preface comments of the FTOR and SCOR programs along with additional information for more efficient utilization of the spectral analysis package. Several difficulties were encountered during utilization of the analyses programs and consideration of these difficulties is the primary reason for inclusion of Appendix G.

SPECTRUM STATISTICS FOR 2413 CHANNEL 4 U' LEVEL 1
STATISTICS ARE BASED ON 8 BLOCKS OF 256 SAMPLES EACH
THE SAMPLING FREQUENCY WAS 500.0000SAMP/SEC , MAKING THE BLOCK LENGTH 0.51200 SECONDS
TREND IS THE AVERAGE OF (VALUE(A)-VALUE(B))/(BLOCK NO.(A)-BLOCK NO.(B))
A CALIBRATION FACTOR OF 1.000E 00 HAS BEEN APPLIED TO THE INPUT DATA

	FREQUENCY HERTZ	BANDWIDTH	SPECTRUM (M/SEC**2)**2/HERTZ	STD.DEV.	TREND	FREQ*SPECTRUM (M/SEC**2)**2	LAST HARMONIC
1	1.69E 00	1.95E 00	1.91E 11	2.61E 11	1.512E 10	3.223E 11	1
2	3.78E 00	1.95E 00	3.93E 10	2.93E 10	7.395E 08	1.486E 11	2
3	5.78E 00	1.95E 00	5.61E 10	4.30E 10	-2.517E 09	3.239E 11	3
4	7.75E 00	1.95E 00	3.37E 10	3.88E 10	-1.730E 09	2.609E 11	4
5	1.06E 01	3.91E 00	1.48E 10	1.03E 10	3.723E 03	1.565E 11	6
6	1.45E 01	3.91E 00	9.11E 09	3.43E 09	-5.368E 08	1.323E 11	8
7	1.93E 01	5.86E 00	4.44E 09	4.10E 09	6.856E 08	8.569E 10	11
8	2.61E 01	7.81E 00	2.08E 09	1.64E 09	1.757E 08	5.420E 10	15
9	3.48E 01	9.77E 00	1.92E 09	8.45E 08	-1.396E 08	6.689E 10	20
10	4.64E 01	1.37E 01	1.07E 09	3.82E 08	6.472E 07	4.956E 10	27
11	6.19E 01	1.76E 01	8.82E 08	5.06E 08	1.306E 08	5.456E 10	36
12	8.22E 01	2.34E 01	3.92E 08	1.80E 08	1.032E 07	3.219E 10	48
13	1.09E 02	3.13E 01	2.55E 08	1.25E 08	1.618E 07	2.782E 10	64
14	1.46E 02	4.30E 01	1.86E 08	8.01E 07	2.143E 07	2.721E 10	86
15	1.95E 02	5.66E 01	1.13E 08	4.80E 07	4.424E 06	2.210E 10	115
16	2.38E 02	2.54E 01	7.88E 07	2.93E 07	2.016E 06	1.875E 10	128

INTEGRAL (SUM) UNDER SPECTRUM = 8.42E 11 M/SEC**2**2
ZEROTH HARMONIC (DC) HAD
AVERAGE = -8.86E 05 M/SEC**2
VARIANCE = 4.29E 11 M/SEC**2**2
TREND = -6.49E 04 M/SEC**2

Figure 15. SCOR Spectral Statistics.

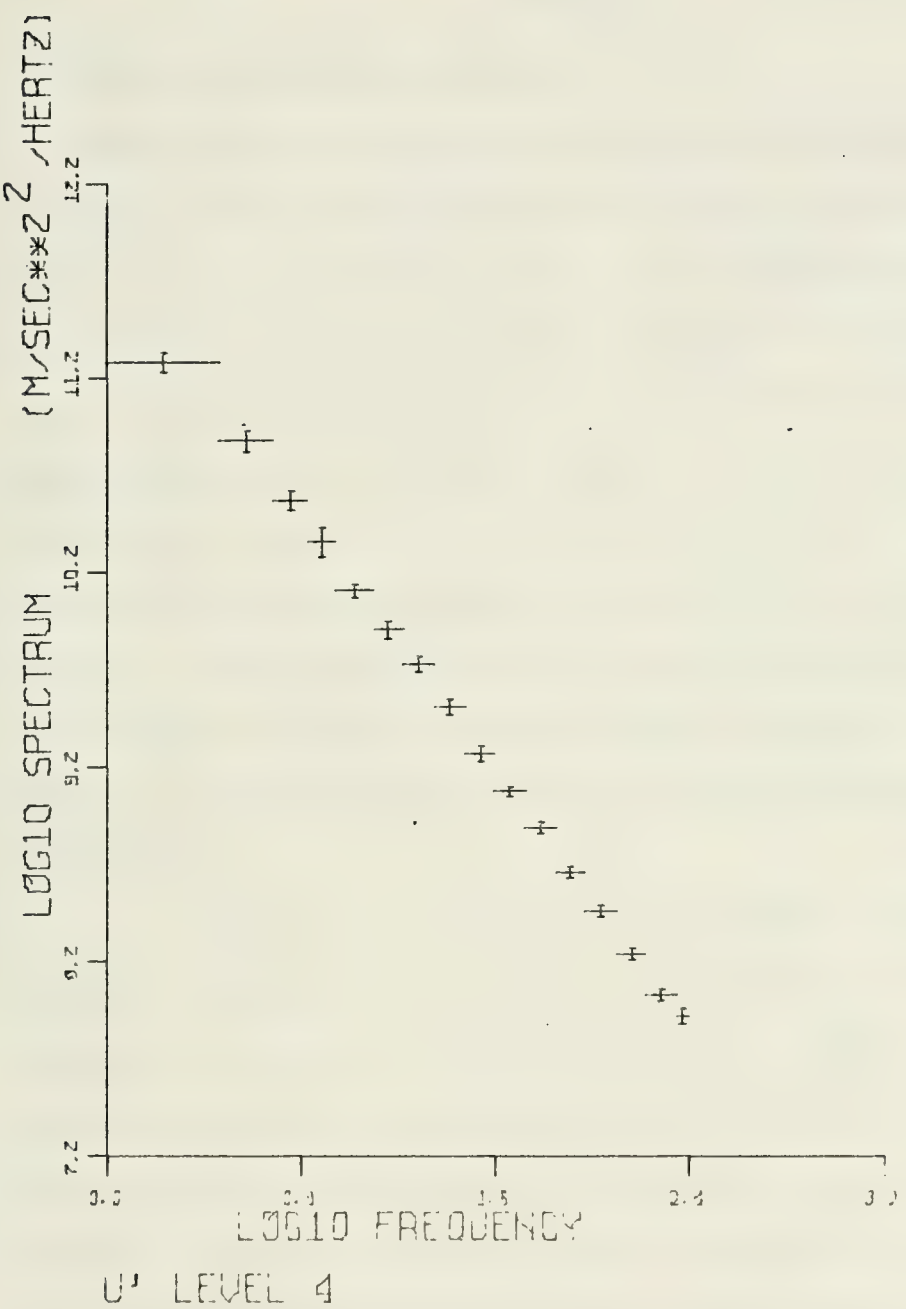


Figure 16. SCOR Spectral Plot.

V. RESULTS

A. ONE POINT SPECTRAL METHOD

The procedure first selected for estimating ε , and hence u_*, was to use single point values from the spectra, similar to that in Figure 16. A -5/3 slope was approximated for the spectrum and the frequency and spectral density, for a spectral value coincident with the line, were taken from computer output similar to that illustrated in Figure 15. Equation 10 was then used to obtain ε from values of frequency, spectral density, wind speed and probe height. The computed value of ε was then used in Equation 7 to obtain a value for the friction velocity (u_*). The computer program used for these calculations appears in Appendix H.

U_* values were obtained by this method for all data periods and tabulated results for one minute and 10 minute averages are listed in Tables III-VII. This method appeared successful for spectra such as those shown in Figure 16, which had a definite -5/3 slope for a majority of points. However, the single point spectral method is quite subjective when used with spectra such as the one shown in Figure 17. It is easily seen that selections of unrepresentative spectral estimates could result in values of ε which would differ significantly. Because of the subjective manner in which -5/3 slope lines could be drawn and

TABLE III

Momentum Flux Calculations for 1103-1138 20 Sept 1973 using the One Point Spectral Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	1.078	8.727
	10	1.319	9.129
13.20	1	1.010	8.532
	10	1.389	9.109
8.39	1	2.973	9.871
	10	2.075	8.865
4.52	1	2.418	7.602
	10	2.636	7.812

TABLE IV

Momentum Flux Calculations for 2008-2018 20 Sept 1973 using the One Point Spectral Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	9.742	17.674
	10	8.937	17.272
8.39	1	16.211	18.291
	10	11.679	15.769
4.52	1	20.806	15.643
	10	16.128	14.287

TABLE V

Momentum Flux Calculations for 2023-2053 20 Sept 1973 using the One Point Spectral Method

Height (m)	Time Average (min)	ε (cm^2 sec^{-3})	u_* (cm sec^{-1})
14.41	1	9.304	17.505
	10	9.556	17.662
8.39	1	14.042	16.768
	10	14.519	16.956
4.52	1	21.934	15.829
	10	22.634	15.996

TABLE VI

Momentum Flux Calculations for 2323-2341 20 Sept 1973 using the One Point Spectral Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	4.069	14.925
	10	3.543	12.688
13.20	1	3.316	12.973
	10	2.576	11.082
8.39	1	7.965	13.859
	10	6.265	12.813

TABLE VII

Momentum Flux Calculations for 0637-0652 21 Sept 1973 using the One Point Spectral Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	1.923	10.146
	10	1.114	8.625
8.39	1	7.830	13.991
	10	5.660	12.386

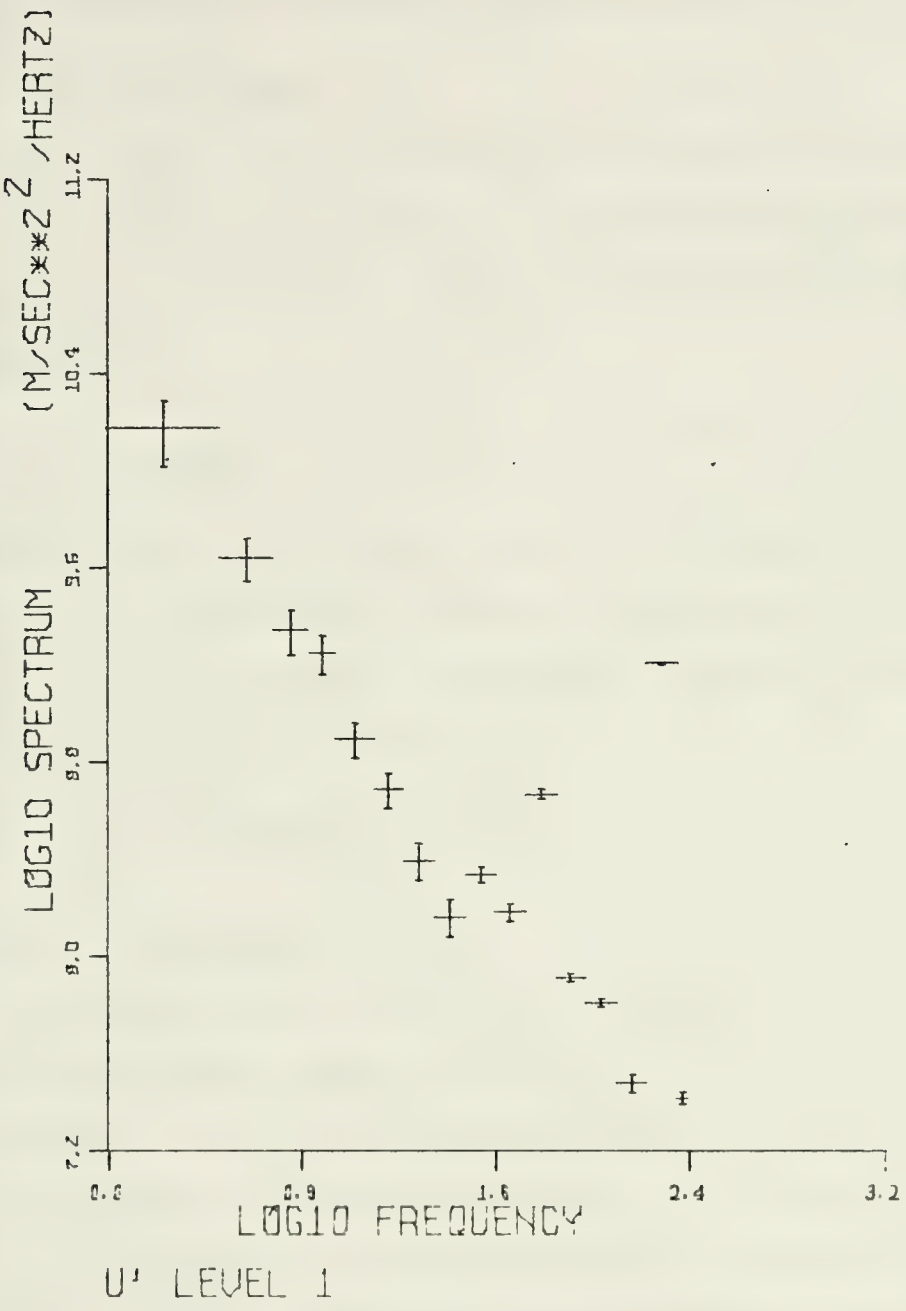


Figure 17. Velocity Spectrum Showing Deviation from -5/3 Slope.

a coincident spectral value selected, there was some doubt expressed in results from other than ideal spectra.

B. INTERCEPT METHOD

To avoid the subjectiveness of estimates of ε based on single spectral estimates, a second method was utilized. This method is based on Equation 10 rewritten in the following form

$$\text{Ln } k\phi(k) = -2/3 \text{ Ln } k + \text{Ln } \alpha\varepsilon^{2/3} \qquad (14)$$

For this expression a plot of Ln $k\phi(k)$ versus Ln k would result in a curve with a slope of one and an intercept value equal to Ln $\alpha\varepsilon^{2/3}$. From this intercept, the value of ε can be obtained from

$$\left[\frac{\text{Exp } b}{\alpha}\right]^{3/2} = \varepsilon$$

where b = intercept value.

The advantage in using the intercept method versus the single point spectral method is that the intercept is determined from an average of the points along a line defined by the -2/3 slope. Figure 18 is an example of most curves obtained from the application of Equation 14 to spectral results. Difficulty in approximating the slope was encountered in a few cases such as that illustrated in Figure 19 but in most instances the forcing of a +1 slope permitted easier detection of spectral harmonics

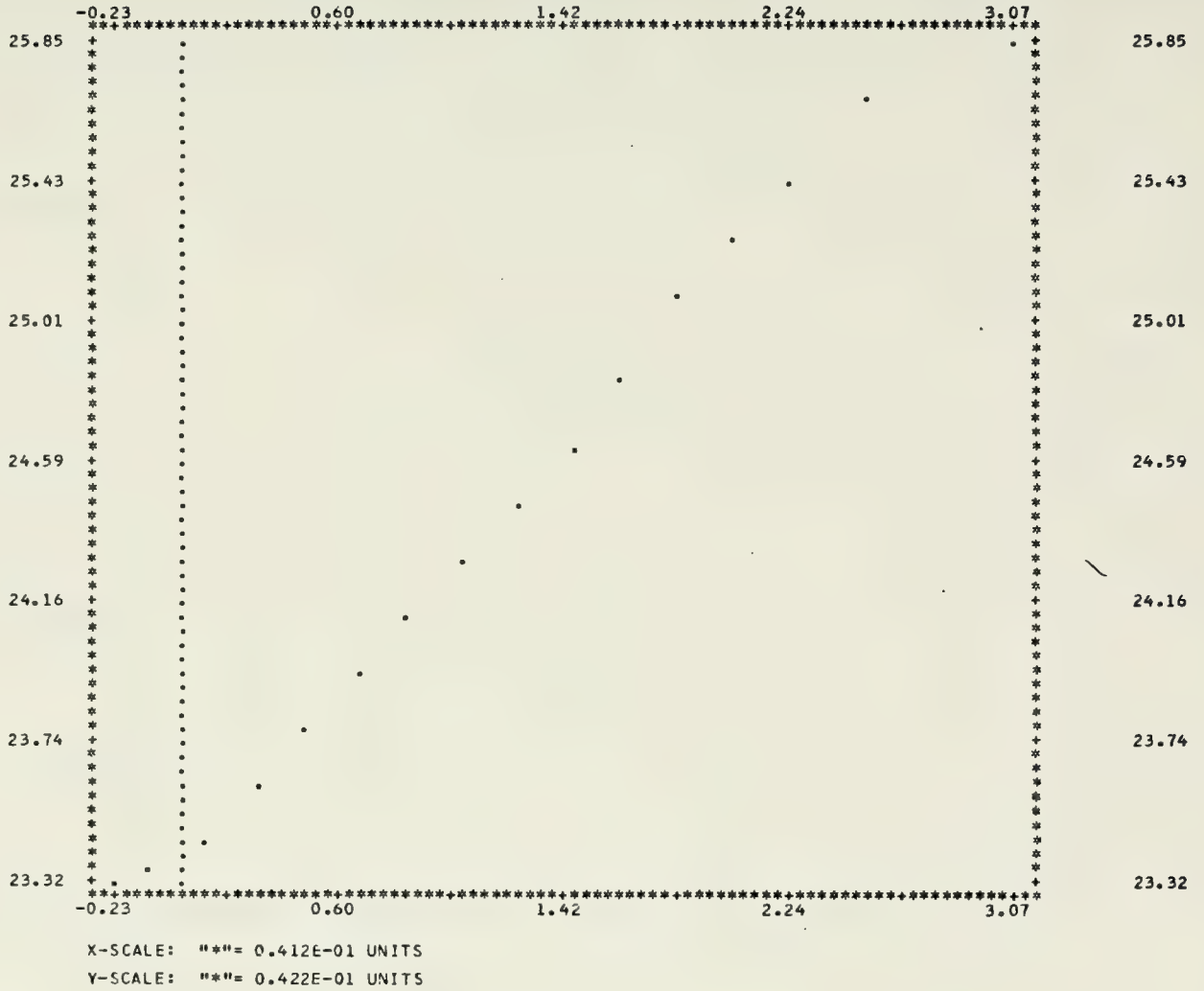


Figure 18. Ten Minute Intercept Plot for 1103-1138 20 Sept 73.

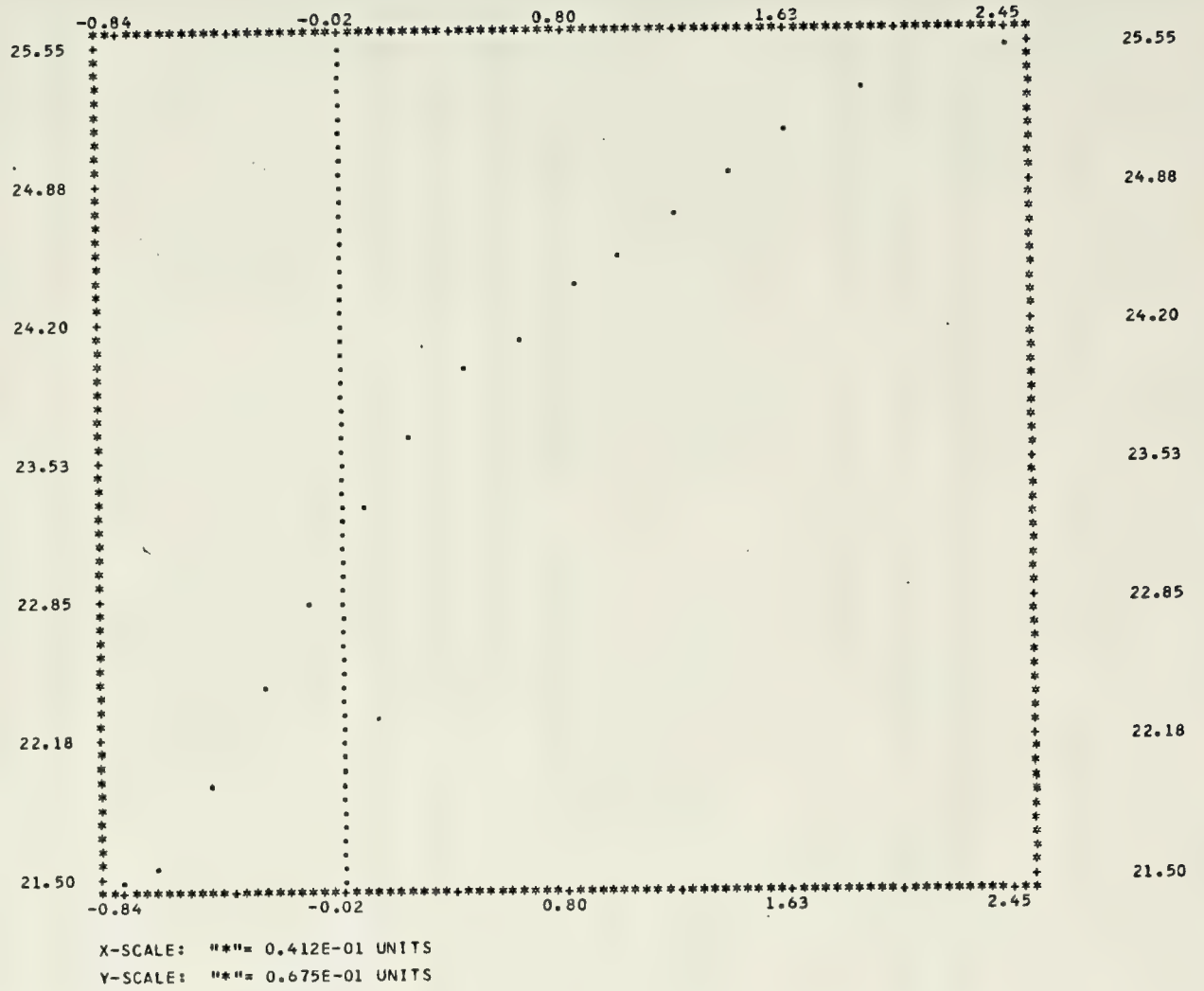


Figure 19. Three Minute Intercept Plot for 2023-2053 20 Sept 73.

which did not fit the -5/3 criteria. Table XI does not indicate a one minute spectral average since the curves for that time average were similar to Figure 20. It is clear that fitting a +1 slope to this scattering of points would be difficult.

The intercept method was used to calculate ε and u_* for all five data periods. The results of these calculations are listed in Tables VIII-XII.

C. COMPARISON OF METHODS

A comparison of Tables III-VII and Tables VIII-XII indicates that somewhat higher u_* values were obtained with the intercept method. The apparent validity of the higher values will be examined later.

Considering the intercept method, a majority of cases yielded larger u_* values for longer time averages. The importance of resultant higher u_* values will be apparent when comparisons are made between shipboard results and results from other studies. The subjective nature of selecting spectral estimates in the one point spectral method is manifested by larger deviations in u_* values associated with periods when spectra were not "near-perfect."

The one point spectral method was compared with the intercept method because of interests in designing procedures for quick estimates of u_* during measurements. If valid values of ε could be obtained from single spectral

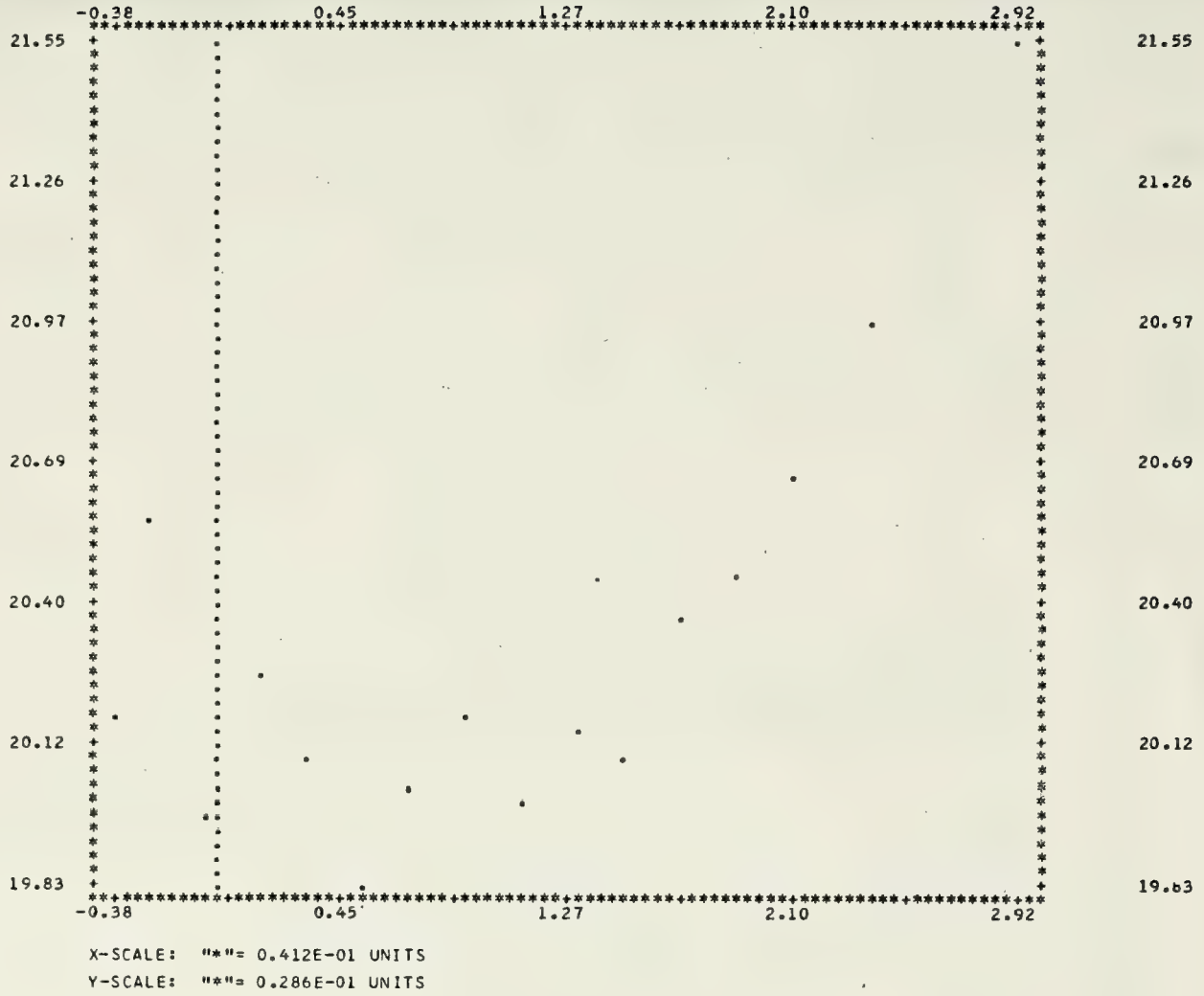


Figure 20. One Minute Intercept Plot for 2323-2341 20 Sept 73.

TABLE VIII

Momentum Flux Calculations for 1103-1138 20 Sept 1973 using the Zero Intercept Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	1.329	9.151
	4	1.378	9.330
	10	1.235	9.012
	20	1.372	9.248
13.20	1	1.445	9.139
	4	1.379	8.998
	20	1.503	9.260
8.39	1	2.635	9.600
	4	2.337	9.224
	20	2.622	9.584
4.52	1	3.086	8.233
	4	3.148	8.288
	20	3.689	8.738

TABLE IX

Momentum Flux Calculations for 2008-2018 20 Sept 1973 using the Zero Intercept Method

Height (m)	Time Average (min)	ε (cm^2 sec^{-3})	u_* (cm sec^{-1})
14.41	1	10.288	18.012
	3	8.285	17.135
	10	10.935	18.474
8.39	1	13.226	16.437
	3	11.828	15.988
	10	13.678	16.622
4.52	1	17.765	14.731
	3	14.677	13.846
	10	18.127	14.855

TABLE X

Momentum Flux Calculations for 2023-2053 20 Sept 1973 using the Zero Intercept Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	1	12.071	19.093
	3	11.825	18.985
	20	11.540	18.809
8.39	1	16.723	17.774
	3	16.496	17.694
	20	16.243	17.603
4.52	1	25.023	16.541
	3	24.492	16.432
	20	24.149	16.346

TABLE XI

Momentum Flux Calculations for 2323-2341 20 Sept 1973 using the Zero Intercept Method

Height (m)	Time Average (min)	ε ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	3	12.925	19.533
	10	13.564	19.849
13.20	3	13.471	19.235
	10	14.009	19.488
8.39	3	14.418	16.917
	10	15.025	17.151

TABLE XII

Momentum Flux Calculations for 0637-0652 21 Sept 1973 using the Zero Intercept Method

Height (m)	Time Average (min)	ϵ (cm^2 sec^{-3})	u_* (cm sec^{-1})
14.41	1	1.209	8.868
	4	1.955	10.407
	10	1.570	9.675
8.39	1	5.316	12.131
	4	8.451	14.158
	10	7.643	13.691

estimates then the structure function measured may be valid. The latter has been shown to be a poor approach on the basis of these results.

D. EVALUATION OF THE VARIATION OF U_* WITH HEIGHT

A long accepted concept in turbulence theory has been the existence of a constant-stress layer. This concept is often used to evaluate the representativeness of accumulated data (e.g., Stegen, et al) and will be applied to test the validity of assumptions and expressions used in the present study.

Table I was compiled by Stegen, et al for conditions when the measured mean wind speed was 5.12 m sec^{-1}. This mean speed corresponds to the wind conditions for the values tabulated in Tables VII and XII. A comparison of results in Table I and Tables VII and XII reveals lower values of u_* in the present study. As previously mentioned, the constant, (α), in Equation 10 is empirically derived and several values have been suggested in the literature. A value of $\alpha = 0.60$ was used in compiling the results in Table I while a value of 0.48, suggested by Pond, et al (1966), was used in the present study.

U_* results listed in Table VIII support a constant-flux assumption as well as the validity of Equation 7 for u_* calculations, for neutral or near neutral conditions. The anomalously low value of u_* at 4.52 meters could be the result of acceleration due to the ship's bow. It is

seen that as the spectral averaging time increases the value of the flux increases. This would be consistent with an interpretation that increased averaging time would reduce the observed acceleration effects.

Tables IX-XI correspond to periods of stable stratifications while Table XII reflects a period of unstable stratification. It is seen from Equation 12 that neglecting diabatic effects would introduce a bias into the data. A stability correction could be applied to adjust the flux values for the more general case of stratified flow.

E. THE VARIATION OF ε WITH HEIGHT

Figures 21-25 show the plots of Ln ε versus Ln z for the periods listed in Tables VIII-XII. On the basis of Equation 8, a plot of Ln ε vs Ln z should yield a -1 slope for neutral conditions. Results from Stegen, et al, Figure 3, were in agreement with this prediction.

In Figures 22 and 23 the slopes are less than -1 while in Figure 24 the slope is greater than -1. An initial concern when these results became known was whether possible attenuation of the sensors at lower levels was a factor. Such a concern is logical since the sensors near the surface would be likely to lose sensitivity more rapidly as a result of increased salt loading at lower levels.

The data period which occurred last is the one which shows the greatest slope which indicates that sensor deterioration at lower levels was not responsible for the

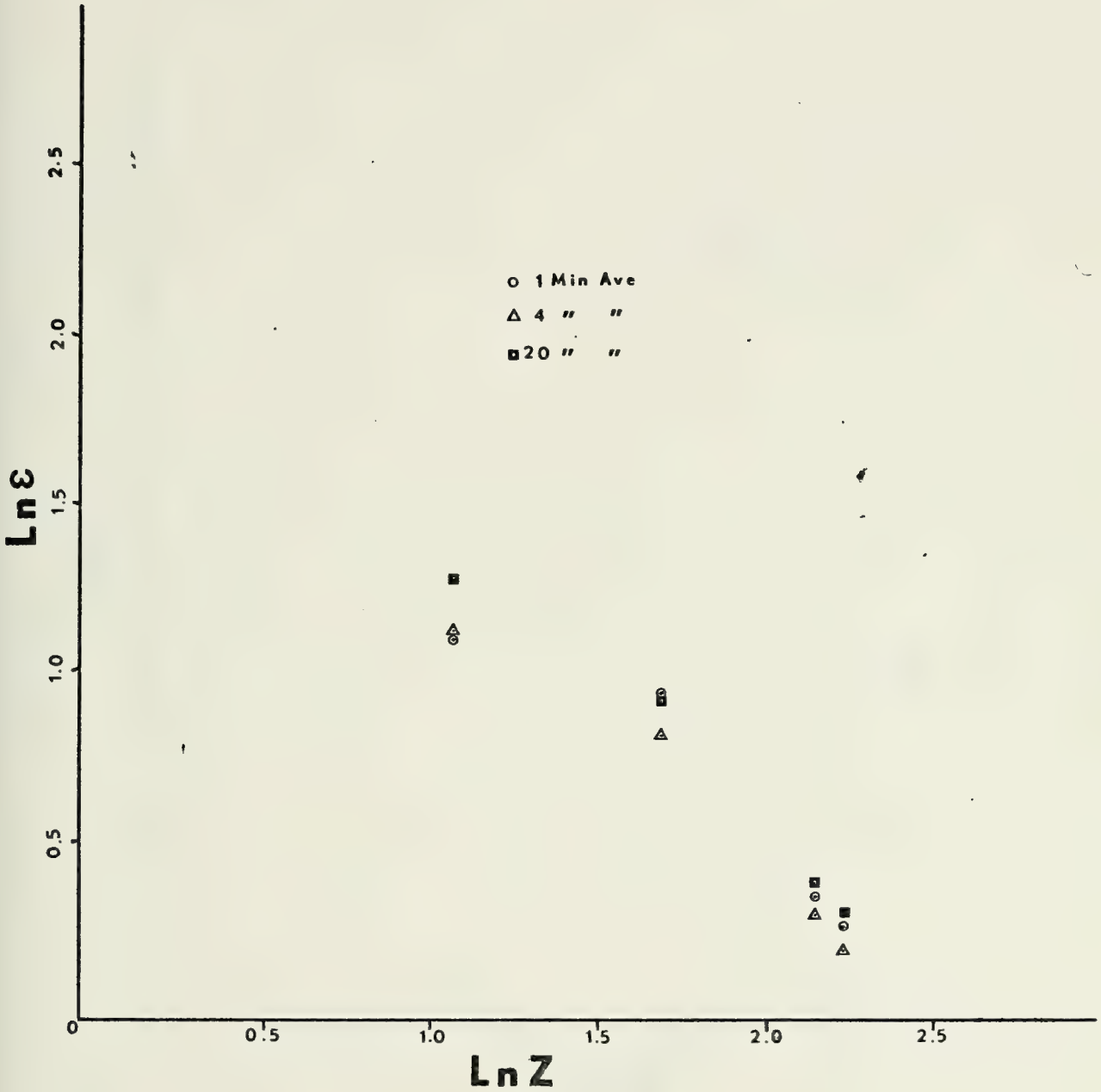


Figure 21. Measured Values of ε vs Height for 1103-1138 20 Sept 73. For Scaling Purposes a Factor of 5.0 was Subtracted from the x-Values.

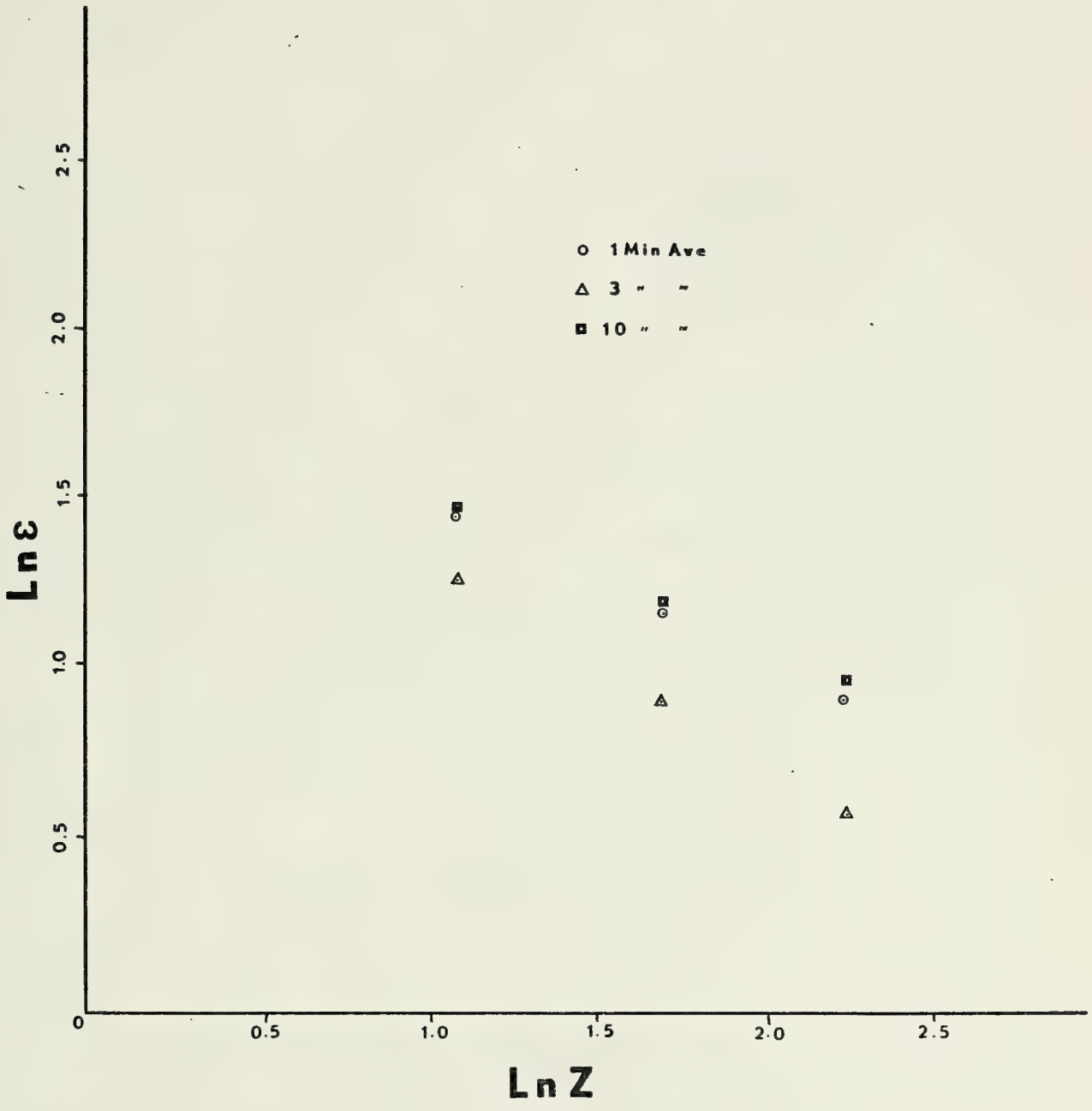


Figure 22. Measured Values of ε vs Height for 2008-2018 20 Sept 73. For Scaling Purposes a Factor of 5.0 and 1.4 were Subtracted from the X and Y Values, Respectively.

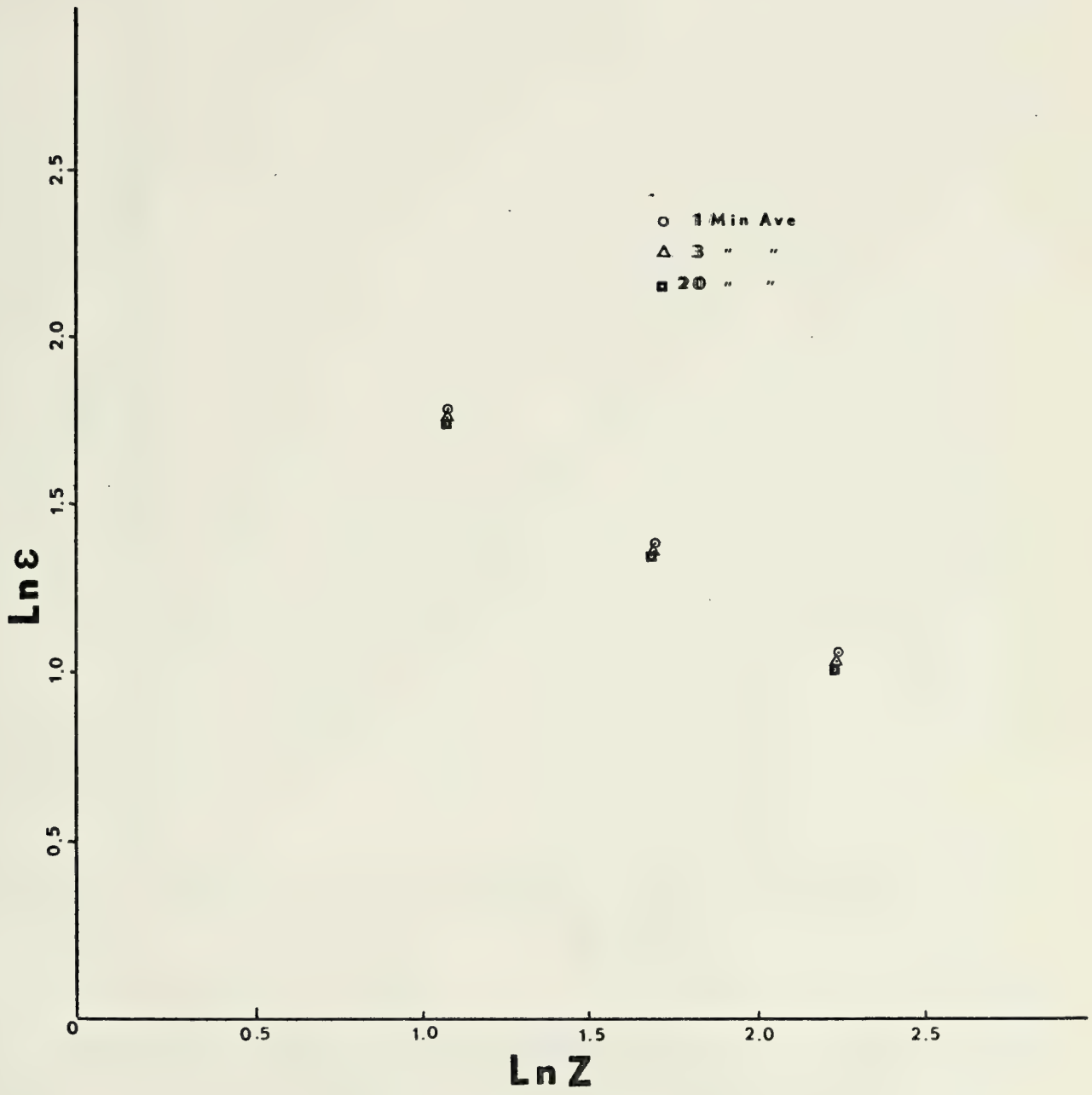


Figure 23. Measured Values of ε vs Height for 2023-2053 20 Sept 73. For Scaling Purposes a Factor of 5.0 and 2.0 were Subtracted from the X and Y Values, Respectively.

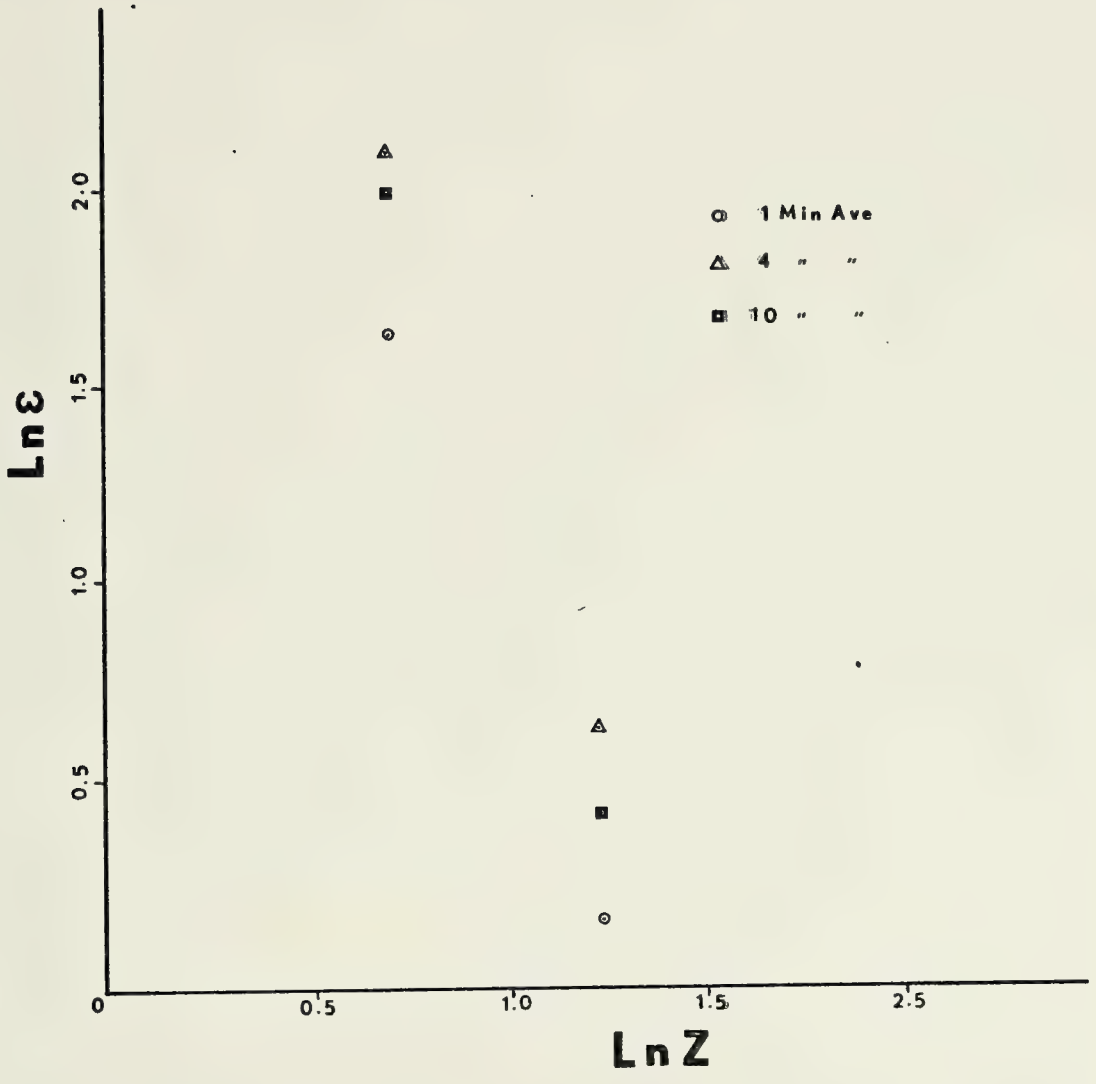


Figure 24. Measured Values of ε vs Height for 0637-0652 21 Sept 73. For Scaling Purposes a Factor of 6.0 was Subtracted from the X Values.

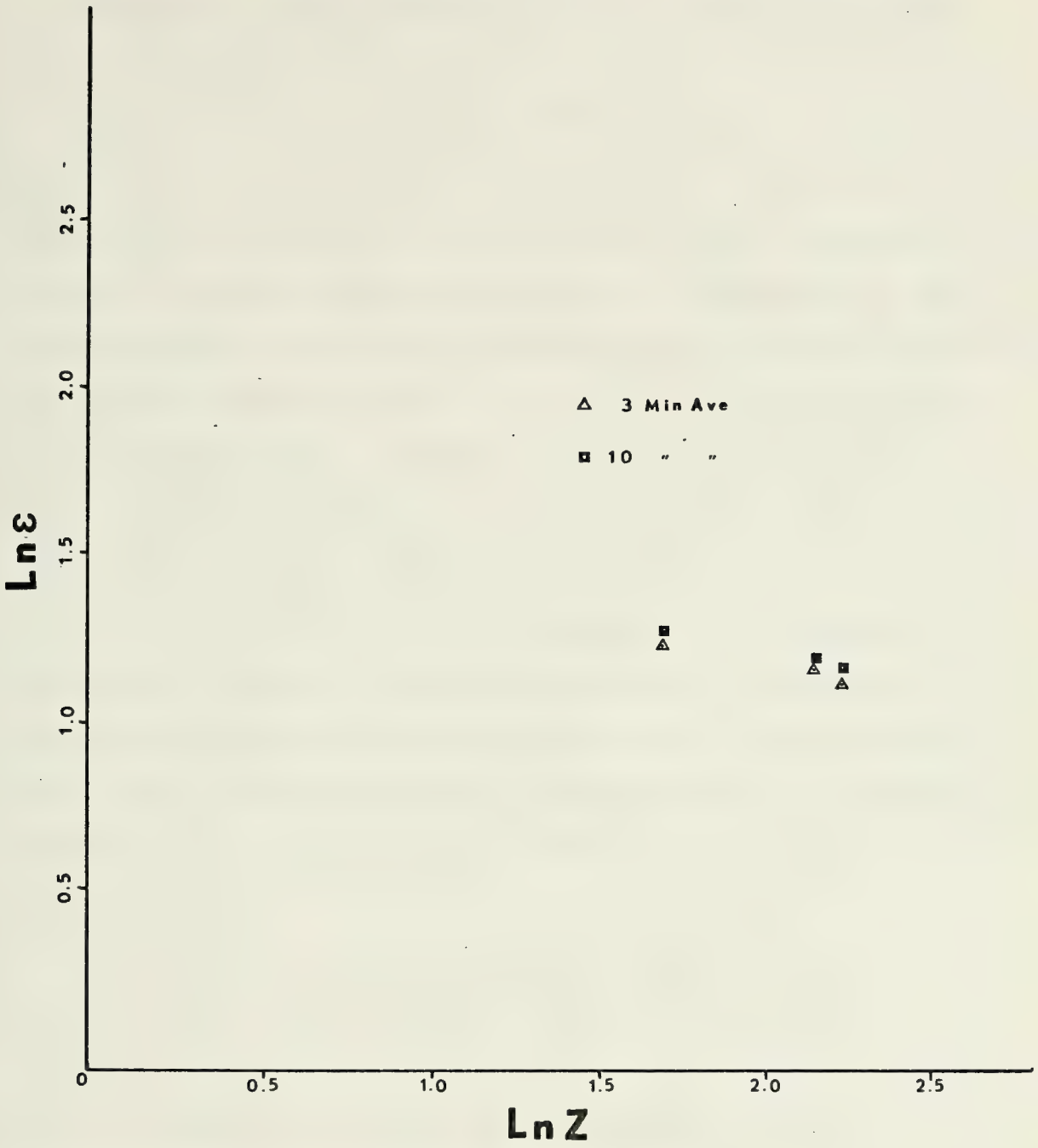


Figure 25. Measured Values of ε vs Height for 2323-2341 20 Sept 73. For Scaling Purposes a Factor of 5.0 and 1.4 were Subtracted from the X and Y Values, Respectively.

variation in slopes. Further support of this conclusion is provided by using Equation 11 as an independent method of determining the dissipation.

For the 2023-2053 20 Sept 73 data period, the spectra at all levels were similar to that shown in Figure 26, where scale separation between the pure inertial transfer and the viscous dissipation regions was discernable. The upper limits of the inertial subrange were determined from the spectra and Equation 11 was used to obtain an estimate of the dissipation. In Table XIII the values obtained by this method are compared to those obtained from spectral estimates. The inner scale computation is independent of sensor calibration since it is determined by frequency distributions and not on the spectral value. The apparent agreement between the two estimates is an in situ calibration which indicates the loss of sensitivity by individual sensors was not the cause for the deviation from the predicted slope.

The deviation from the predicted slope was also examined for possible influence of non-neutral stratifications or wind-wave coupling. Deacon (1951), from examinations of numerous vertical wind profiles, proposed the following expression for the wind shear

$$\frac{\partial \bar{u}}{\partial z} = \frac{u_*}{kz_o} \left(\frac{z}{z_o}\right)^{-\beta} \qquad (15)$$

where β is a function of stability.

Figure 26. Twenty Minute Velocity Spectrum for 2023-2053 20 Sept 73.

TABLE XIII

A Comparison of Dissipation Obtained by Spectra (ε) and Dissipation Obtained from the Inner Scale (ε_o)

Height (m)	ε ($cm^2\ sec^{-3}$)	ε_o ($cm^2\ sec^{-3}$)	u_* ($cm\ sec^{-1}$)
14.41	9.556	9.516	17.662
8.39	14.519	14.304	16.956
4.52	22.634	22.492	15.996

The variation of β as a function or Ri, proposed by Deacon, is shown in Figure 27. In Deacon's results, the variation of β may be described in terms of hydrostatic stability. For neutral conditions, $\beta = 1$ so Equation 15 then reduces to Equation 6 and the -1 slope on the Ln ε versus Ln z plot is predicted.

For unstable conditions β is greater than 1 and for stable conditions β is less than 1. Deacon's results predict that the expected slope of a Ln ε versus Ln z plot would deviate from the neutral case with slopes less than -1 for periods of stable stratifications and with slopes greater than -1 for unstable conditions. Examinations of Figures 22-24 indicate why such considerations are important in interpreting the shipboard results. Figures 22-23 correspond to periods of stable stratifications with the 2023-2053 20 September data period being the most stable. In both figures, slopes less than -1 occur, with the more stable of the two periods showing the greatest deviation from the -1 slope. The results are, therefore, consistent with arguments proposed by Deacon. Figure 24 corresponds to an unstable period and shows a slope greater than -1 as predicted by Equation 15.

The results were further examined with respect to predictions from the Monin-Obuhkov similarity theory. The theory states that in the boundary layer there exists a characteristic length determined by the stability and turbulence which can be used as a scaling parameter. For

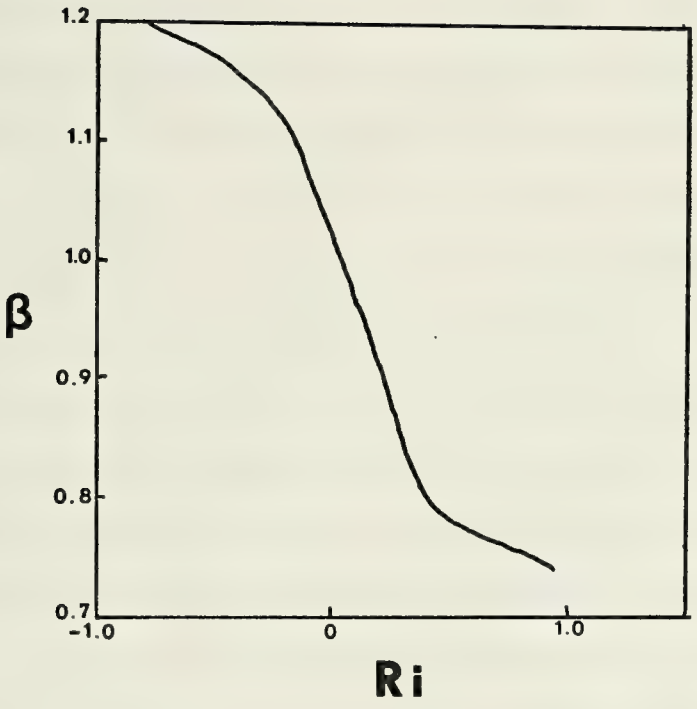


Figure 27. Variation of β with Ri (after Haltiner and Martin).

neutral conditions the appropriate characteristic length is the height above the marine boundary.

Equations 12 and 13 show the effect of non-neutral considerations in developing an expression describing the vertical variation of ε. Equation 12 indicates a relationship between the scaling parameters Ri and L. Such a relationship was described by Busch (1973) in a review of information available in the literature. As presented by Busch, the function $\phi_1(\frac{z}{L}) - \frac{z}{L}$ in Equation 12 has the form $(\phi_m - \frac{z}{L})$ where several flux-profile relationships have been suggested for ϕ_m. Table XIV includes the formulations which Busch used to describe ϕ_m along with constants estimated by Paulson (1970). Relationships between the Monin-Obuhkov length and the Richardson number were first used to obtain stability length (L) corrections for the shipboard results, since Richardson numbers were available from profile measurements described by Cavanaugh (1974). Values of L were then used to define $(\phi_m - \frac{z}{L})$ from relationships in Table XIV.

Figures 28 and 29 show the effects of stability corrections for the periods with stable stratifications listed in Tables IX and X, respectively. Comparisons of the corrected and uncorrected results indicate that adjustments were toward the predicted -1 slope. The fact that the stability correction produces a -1 slope supports the basic premise of the Monin-Obuhkov theory and the validity of the relationships in Table XIV.

TABLE XIV

Flux-Profile Relationships Describing the Stability Function, ϕ_m.

ϕ_m	Stability Condition
$1+7\frac{z}{L}$	$\frac{z}{L} \geq 0$
$(1-16\frac{z}{L})^{-1/4}$	$\frac{z}{L} \leq 0$
$(1-12Ri)^{-1/4}$	$Ri < -0.1$
$(1- 3Ri)^{-1}$	$-0.1 \leq Ri \leq 0.036$
$0.88(1-6Ri)^{-1}$	$0.036 \leq Ri \leq 0.1$

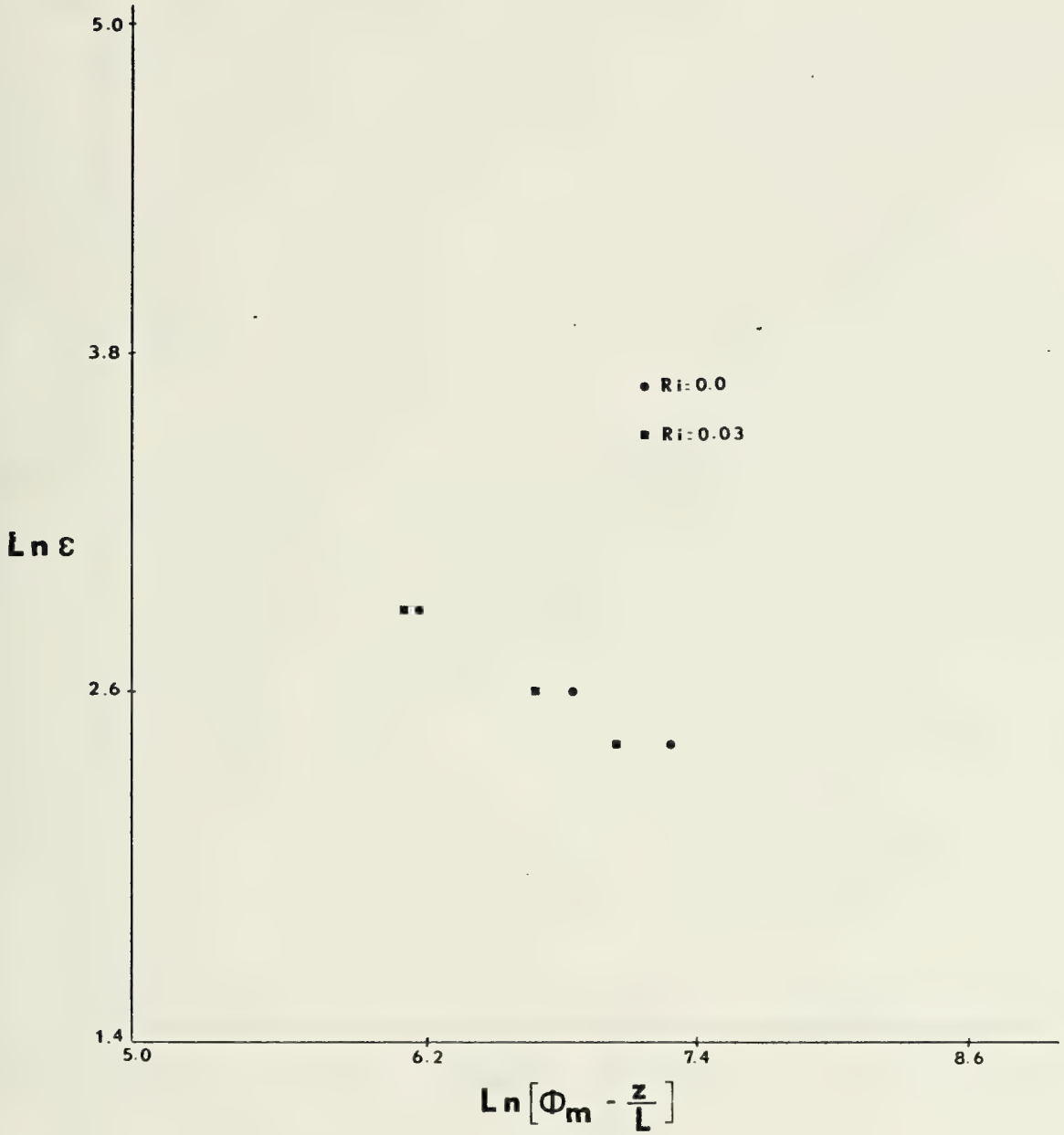


Figure 28. Effect of Stability Correction for 2008-2018 20 Sept 73.

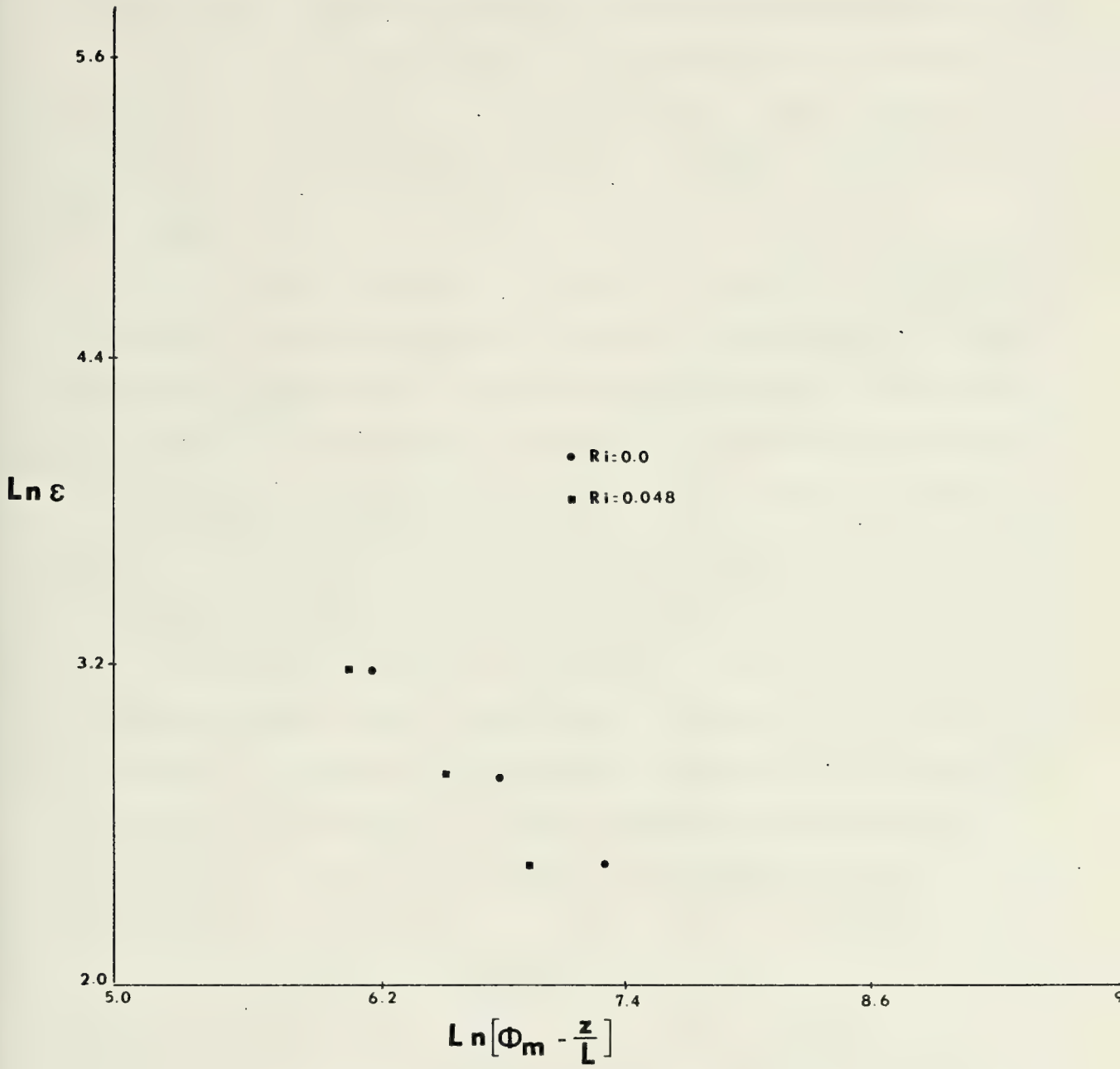


Figure 29. Effect of Stability Correction for 2023-2053 20 Sept 73.

The Monin-Obuhkov theory and the flux-profile relationships were also examined for the period with unstable stratification. Figure 30 shows the results of this examination. For $-0.05 \leq Ri \leq -0.15$ there is a tendency for adjustment toward the predicted -1 slope. However, further decreases in the Richardson number caused an unexpected reversal of the adjustment.

It is seen from Figure 30 that a value of -1.0 for the Richardson number results in a vertical variation of ε which deviates significantly from the predicted slope. The reason for this deviation can be explained by examining the function, $\phi_m(\frac{z}{L} - \frac{z}{L})$. Figure 31, from Garratt (1972), shows a plot of this function using the expressions in Table XIV. To provide the correction necessary to obtain a -1 slope, $(\phi_m - \frac{z}{L})$ must decrease for decreasing values of $\frac{z}{L}$. It is apparent from Figure 31 that this criterion is not met. On the basis of these results there is some evidence that the expression $\phi_m(1-16\frac{z}{L})^{-1/4}$ cannot provide the adjustment necessary to correct the plot for conditions of large instability.

The fact that the stability corrections did not completely restore the -1 slope, even in the stable case, leads to examinations of the possible effects of wind-wave coupling. Davidson and Frank (1971) observed wave-related velocity fluctuations and wave-related momentum transfer in spectral results obtained over natural waves. Davidson

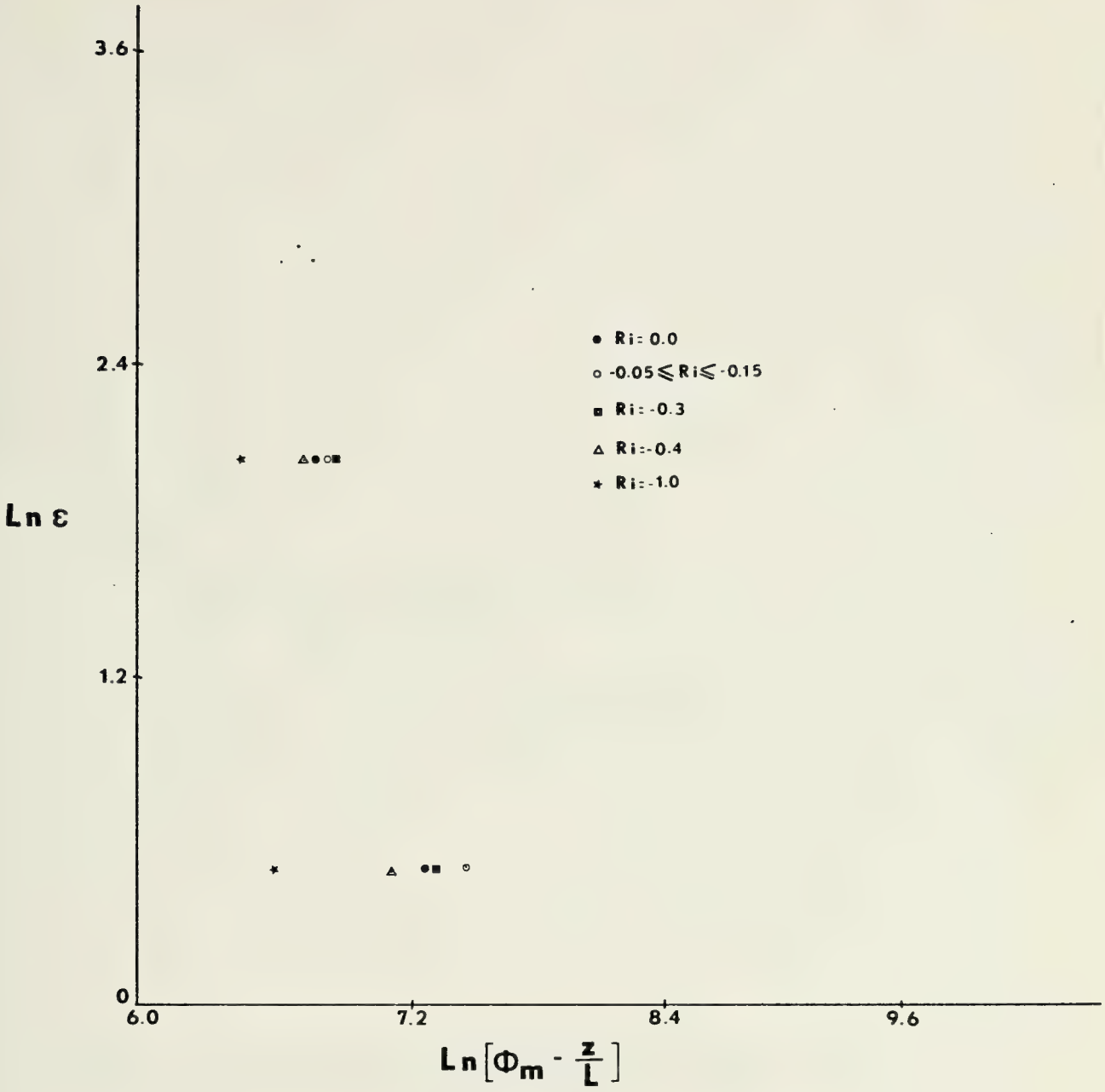


Figure 30. Effect of Stability Correction for 0637-0652 21 Sept 73.

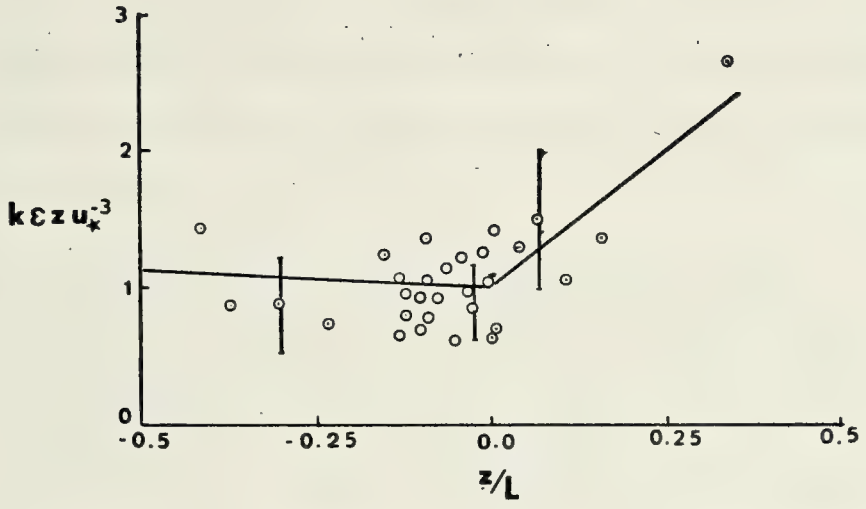


Figure 31. Non-dimensional Dissipation Rate as a Function of z/L (after Garratt).

(1974) described the influence of wind-wave coupling as having the same effect as would be due to the influence of stable stratification. The wave-related effect described by Davidson was a reduction in momentum transfer from that associated with neutral conditions. The results of the present study are consistent with Davidson's findings in that there is a decreased momentum transfer, u_*, as the surface is approached. If this were due to the influence of wind-wave coupling, it would yield the observed deviation from the neutral slope, shown in Figures 22 and 23.

F. VARIATION OF TEMPERATURE FLUCTUATIONS

Figure 32 represents the only temperature spectrum obtained from the five data periods which displayed the predicted -5/3 slope. Figure 33 is an example of the temperature spectra obtained from the majority of data runs. The paucity of temperature data precluded serious evaluations of the temperature fluctuation expressions.

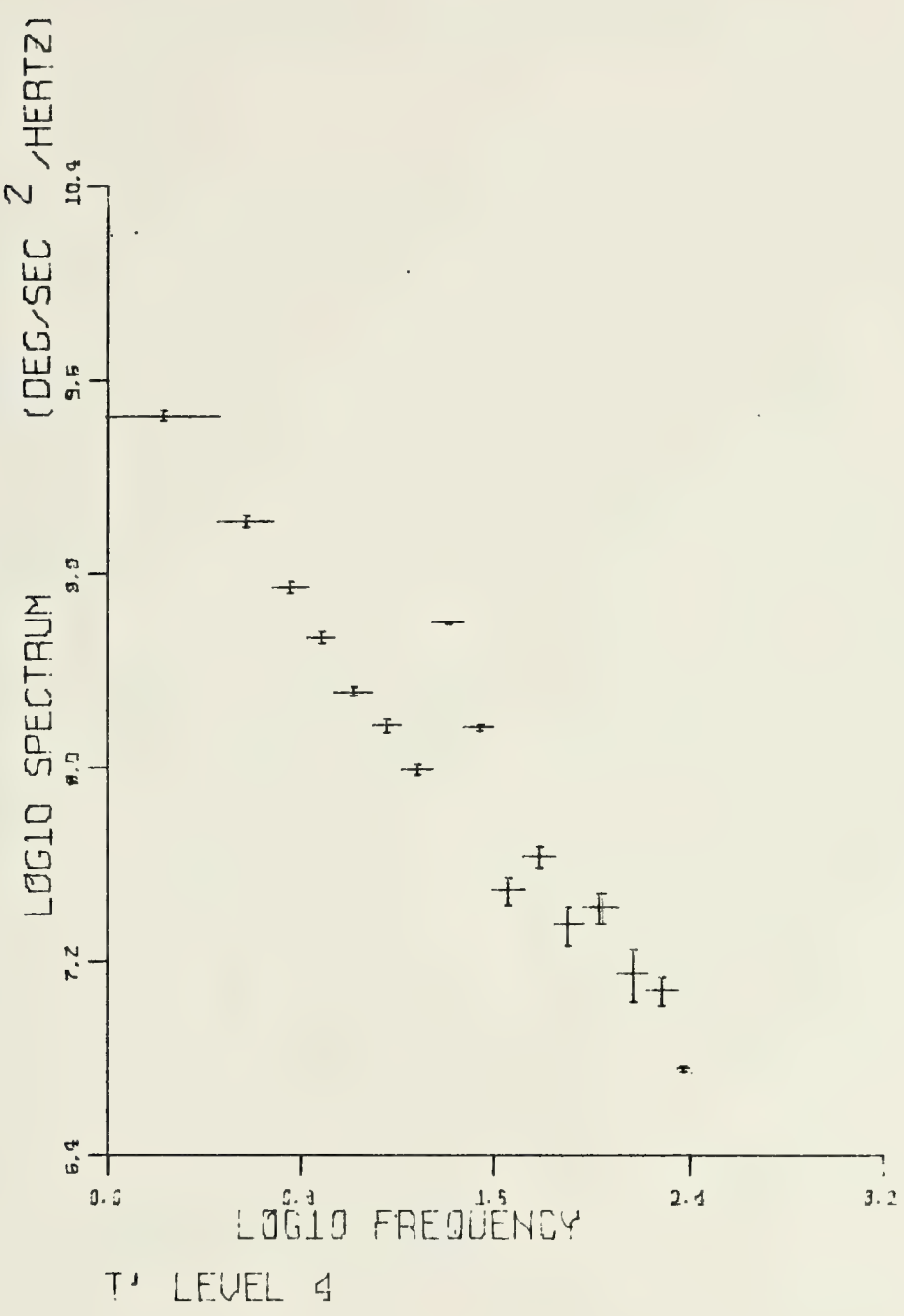


Figure 32. Ten Minute Temperature Spectrum for 2323-2341 20 Sept 73.

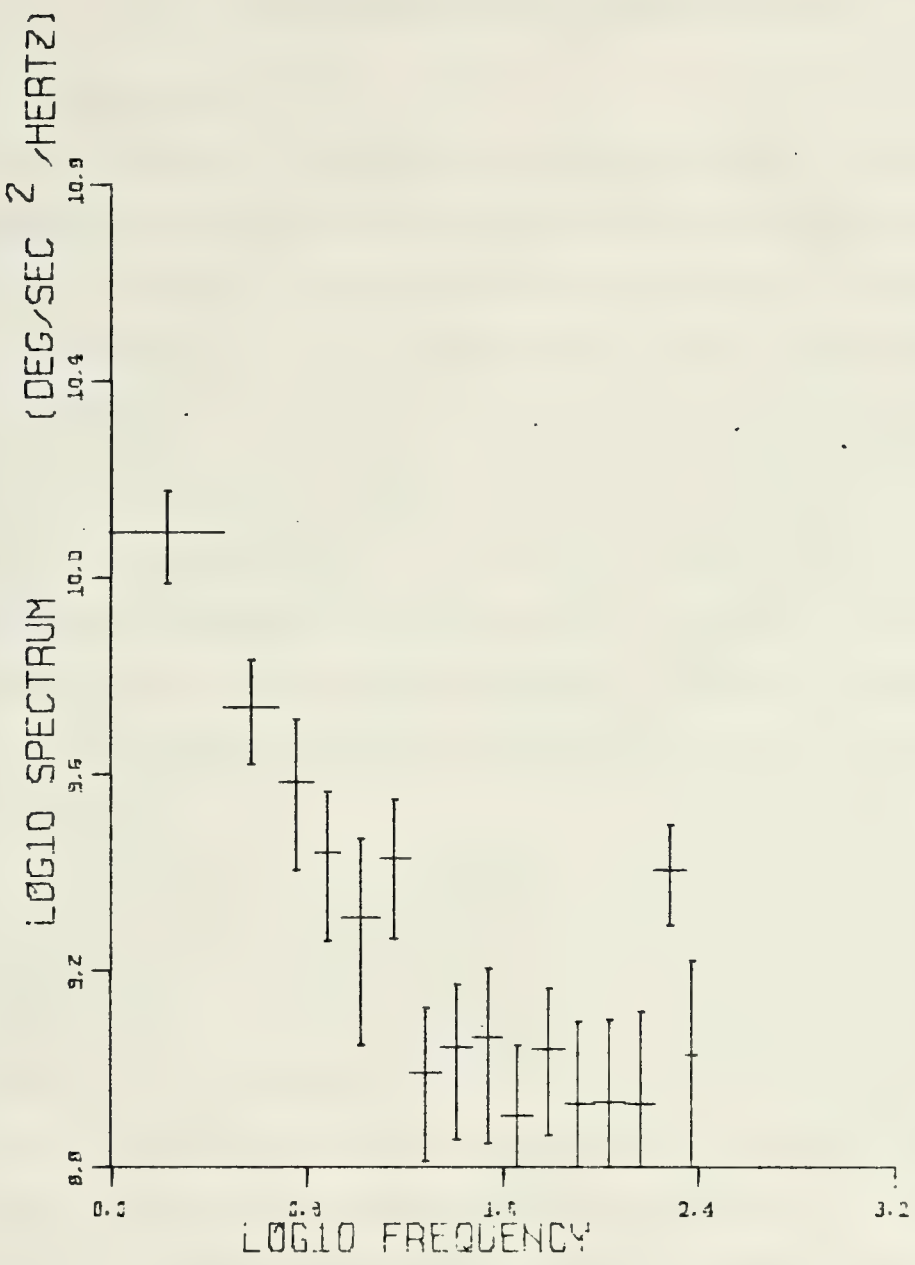


Figure 33. Ten Minute Temperature Spectrum for 2008-2018 20 Sept 73.

VI. CONCLUSIONS AND RECOMMENDATIONS

A. CONCLUSIONS

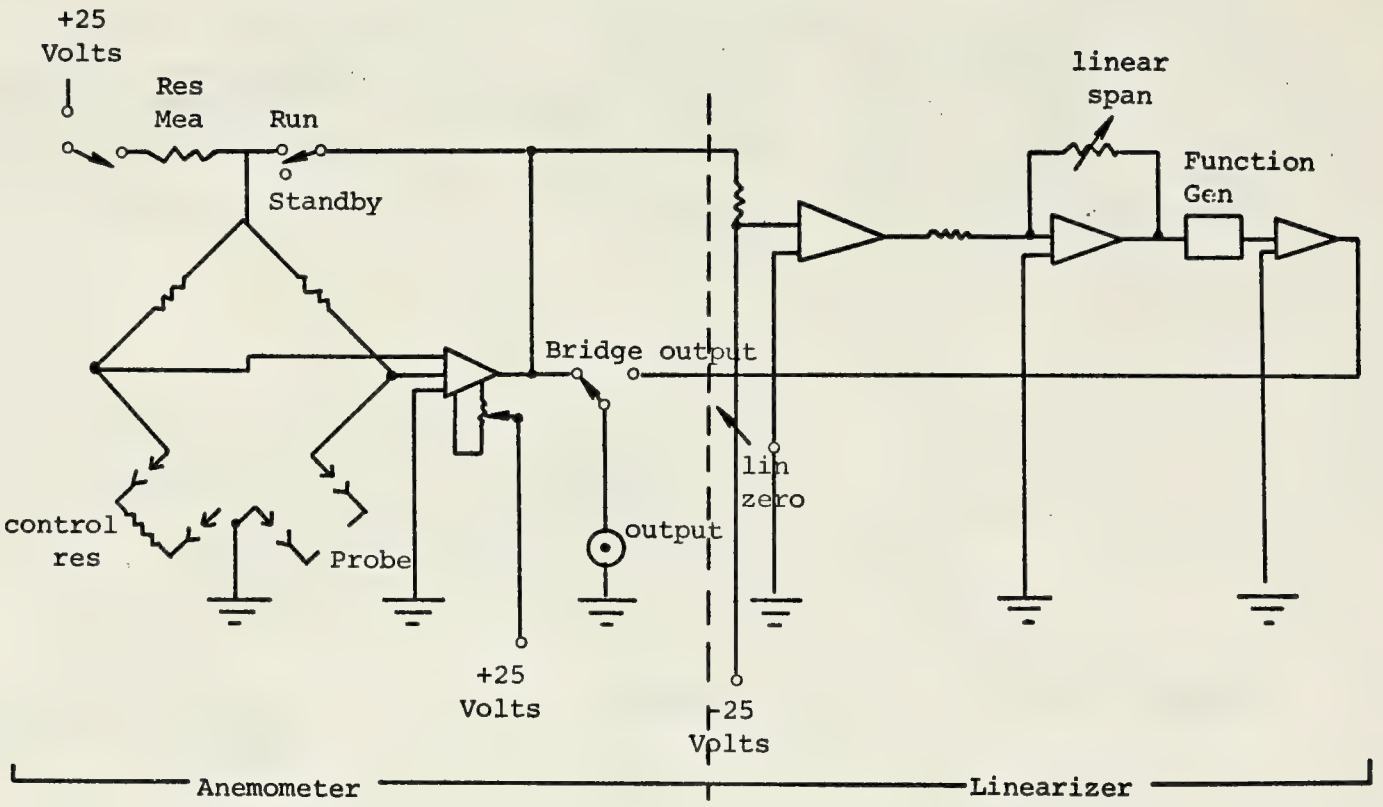
The results obtained from the one point spectral method are generally lower than those obtained by the intercept method. However, the simplicity of the one point spectral method would permit a more rapid determination of the dissipation and if a general estimate were all that was desired, this method would be acceptable. The results of the intercept method show excellent agreement among levels and with results from other studies. The longer time averages (~20 min.) appear to be necessary to avoid acceleration effects at the lower level.

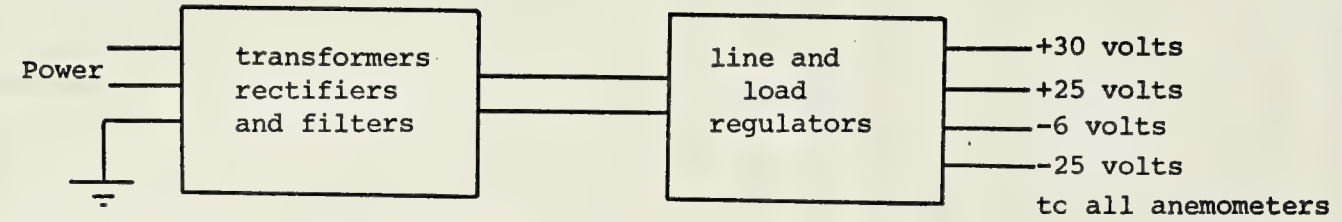
The close agreement between dissipation values derived from the spectral estimates and the inner scale calculations confirm the spectral estimates and also the choice of the constant, $\alpha = 0.48$. Results on the variation of ε with height also verified the formulations used in calculating the dissipation and flux. In addition, the sensitivity of the results to the varying conditions of hydrostatic stability and, perhaps, wind-wave coupling support the predictions proposed by Deacon and Davidson.

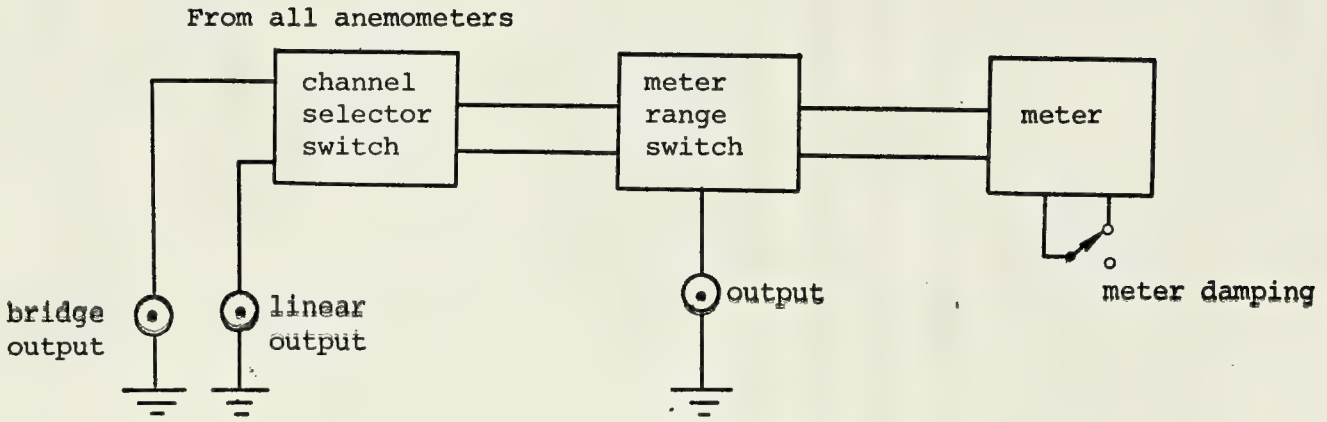
B. RECOMMENDATIONS FOR FUTURE EXPERIMENTS

It is strongly recommended that a real time spectrum analyzer be used in future observational experiments. In addition to the capability for instantaneous evaluation of spectral characteristics, the resulting spectral plots could be used for general estimates of the dissipation. If observational experiments are to be made on a more frequent basis, there is insufficient time to properly evaluate the data before the next experiment. The use of real time analysis techniques would preclude the need for digitization and tape manipulations and save valuable and costly computer time.

APPENDIX A


+25
Volts
Res
Mea
Run
Standby
linear
span
Function
Gen
Bridge output
lin
zero
control
res
Probe
output
+25
Volts
25
Volts
Anemometer
Linearizer


Power
transformers
rectifiers
and filters
line and
load
regulators
+30 volts
+25 volts
-6 volts
-25 volts
tc all anemometers


From all anemometers
channel
selector
switch
meter
range
switch
meter
bridge
output
linear
output
output
meter damping

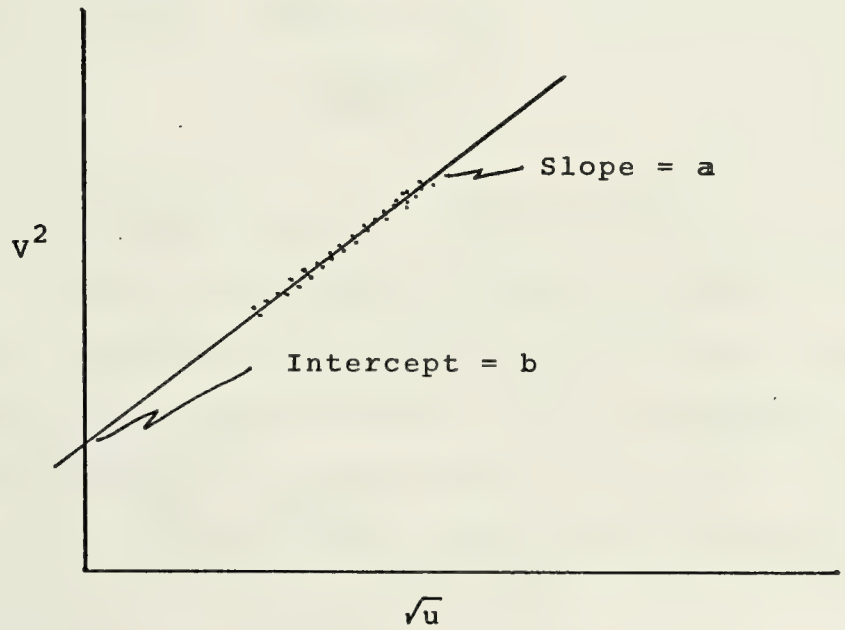
APPENDIX B

A. CALIBRATION AND SCALING PROCEDURES

1. Velocity Calibration

Calibration of the velocity sensors was accomplished using a manometer and a TSI Model 1125 Calibrator. The calibration procedure was to record voltage output versus manometer height over a certain range of velocities. The computer program included in this Appendix was utilized to generate the calibration curve for further use in establishing the calibration factor. This procedure was followed for each of the velocity systems and resulted in the calibration curves included in this Appendix.

The calibration curve obtained from this program resulted in a plot of V^2 versus $\sqrt{u}$ where V is voltage and u is wind speed.



This curve describes a line

$$V^2 = a(u)^{1/2} + b \qquad (1)$$

For use in data analysis it was necessary to obtain a scale such that

$$C \times e' = u'$$

where C = calibration factor; e' = voltage fluctuation and u' = velocity fluctuation. Differentiation of Equation (1) yields

$$2V\,dv = 1/2\ au^{-1/2}\,du$$

or

$$\left[\frac{2x2\ V\ u^{1/2}}{a}\right] dv = du$$

or

$$\left[\frac{4Vu^{1/2}}{a}\right] e' = u'$$

The calibration factor is then

$$C = \left[\frac{4Vu^{1/2}}{a}\right]$$

where "C" scales between volts and cm/sec.

The procedures for actual calculation of this factor consisted of (1) obtaining the slope of the calibration curve (2) selecting a "u" valve equal to that observed during the measurement period and (3) entering the curve with this "u" value to obtain the corresponding voltage.

2. Scaling Procedures for Estimation of Epsilon

In terms of the output of the spectral analyses programs the units associated with $f\phi(f)$ or $k\phi(k)$ were $(\text{volts})^2$. An examination of Equation (1), Section II, shows that the units should be cm^2/sec^2. Recalling that the calibration factor previously discussed scales between volts and cm/sec, it is necessary to multiply the ε value by

$$\left[\frac{(\text{cm}^2/\text{sec}^2)}{(\text{volts})^2}\right]^{3/2} = \left[\frac{\text{cm/sec}}{\text{volts}}\right]^3 = (C)^3$$

to obtain the value of ε in cm^2/sec^2.

To obtain the correct value of ε it is also necessary to consider the gains used during the record and analog-to-digital conversion phases. In addition a scale factor is needed that scales between the analog voltage and the digital output. A 10 db gain was used when the raw signals were recorded and an additional 50 db gain was employed during the A-D process. The scaling between the voltage input and the corresponding digital output is obtained by considering that the maximum voltage input to the COMCOR Ci 5000 is 100 volts and this corresponds to a digital maximum of 2^{23} on the XDX 9300.

The total gain and scaling for the observational data then becomes

$$V(\text{volts}) \times G1 \times G2 \times SC\left(\frac{\text{digital}}{\text{volts}}\right) = \begin{matrix}\text{Value obtained} \\ \text{from IBM 360}\end{matrix}$$

where V = signal from velocity unit

G1 = amplification prior to record (10 db)

G2 = amplification during A-D conversion (50 db)

SC = analog-to-digital scaling factor ($2^{23}/100$)

To obtain the value which corresponds to that which can be used with the calibration factor previously obtained

$$V = (\text{IBM 360 value} \times 1/SC \times 1/G1 \times 1/G2)$$

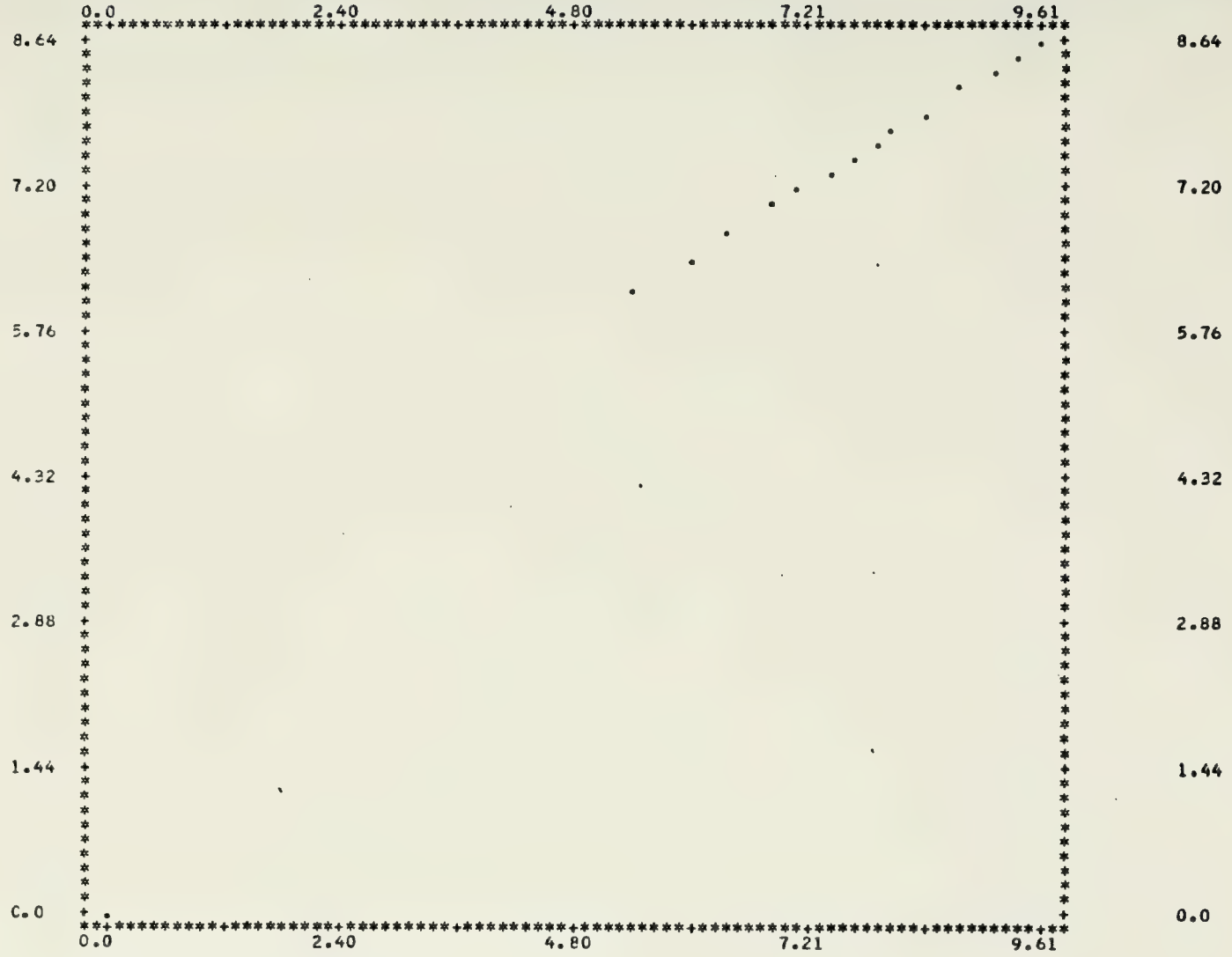
The final scaling then becomes

$$\left[[\text{Scale} \times \text{Gain1} \times \text{Gain2}] \times C\right]^3$$

or in this instance

$$\left[[100/2^{23} \times 0.1 \times 0.02] \times C\right]^3$$

```
C*************************************************************
C*************************************************************
C*************************************************************
C***                                                        **
C***                                                        **
C***   THIS PROGRAM IS DESIGNED TO COMPUTE A CALIBRATION    **
C***   CONSTANT FOR USE IN THE SPECTRAL ANALYSES PACKAGE.   **
C***   THE INPUT PARAMETERS CONSIST OF THE MANOMETER HEIGHT**
C***   AND THE CORRESPONDING VOLTAGE.  THE PROGRAM WILL     **
C***   CALCULATE AND PRODUCE A PRINTER PLOT OF VOLTAGE      **
C***   VERSUS VELOCITY.  A BEST FIT CURVE CAN THEN BE       **
C***   DRAWN THROUGH THE DATA POINTS TO OBTAIN THE          **
C***   CALIBRATION FACTOR.                                  **
C***                                                        **
C***                                                        **
C***       STATEMENT OF VARIABLES                           **
C***                                                        **
C***                                                        **
C***   H.........MANOMETER HEIGHT IN INCHES                 **
C***                                                        **
C***   V.........VOLTAGE                                    **
C***                                                        **
C***   VSQRD.....VOLTAGE SQUARED(ORDINATE OF GRAPH)         **
C***                                                        **
C***   U.........VELOCITY IN FEET PER SECOND                **
C***                                                        **
C***   X.........SQUARE ROOT OF H                           **
C***                                                        **
C***   USQRT.....SQUARE ROOT OF U(ABCISSA OF GRAPG)         **
C***                                                        **
C***                                                        **
C***                                                        **
C*************************************************************
C*************************************************************
C*************************************************************
      REAL*8 TITLE(10)
      DIMENSION VSQRD(15),USQRT(15),U(15)
      READ (5,20) TITLE
   20 FORMAT (10A8)
      WRITE (6,30)
   30 FORMAT ('1',T9,'H',T18,'V',T28,'VSQRD',T39,'U',T47,'US
     1QRT')
      N=15
      DO 60 I=1,N
      READ (5,40) H,V
   40 FORMAT (2F10.3)
      X=SQRT(H)
      VSQRD(I)=V**2
      U(I)=65.3*X
      USQRT(I)=SQRT(U(I))
      WRITE (6,50) H,V,VSQRD(I),U(I),USQRT(I)
   50 FORMAT ('0',5F10.3)
   60 CONTINUE
      WRITE (6,70)
   70 FORMAT ('1')
      CALL PLOTP (USQRT,VSQRD,N,0)
      WRITE (6,80) TITLE
   80 FORMAT ('0',10A8)
      STOP
      END
```



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Y-SCALE: "*"= 0.144E 00 UNITS

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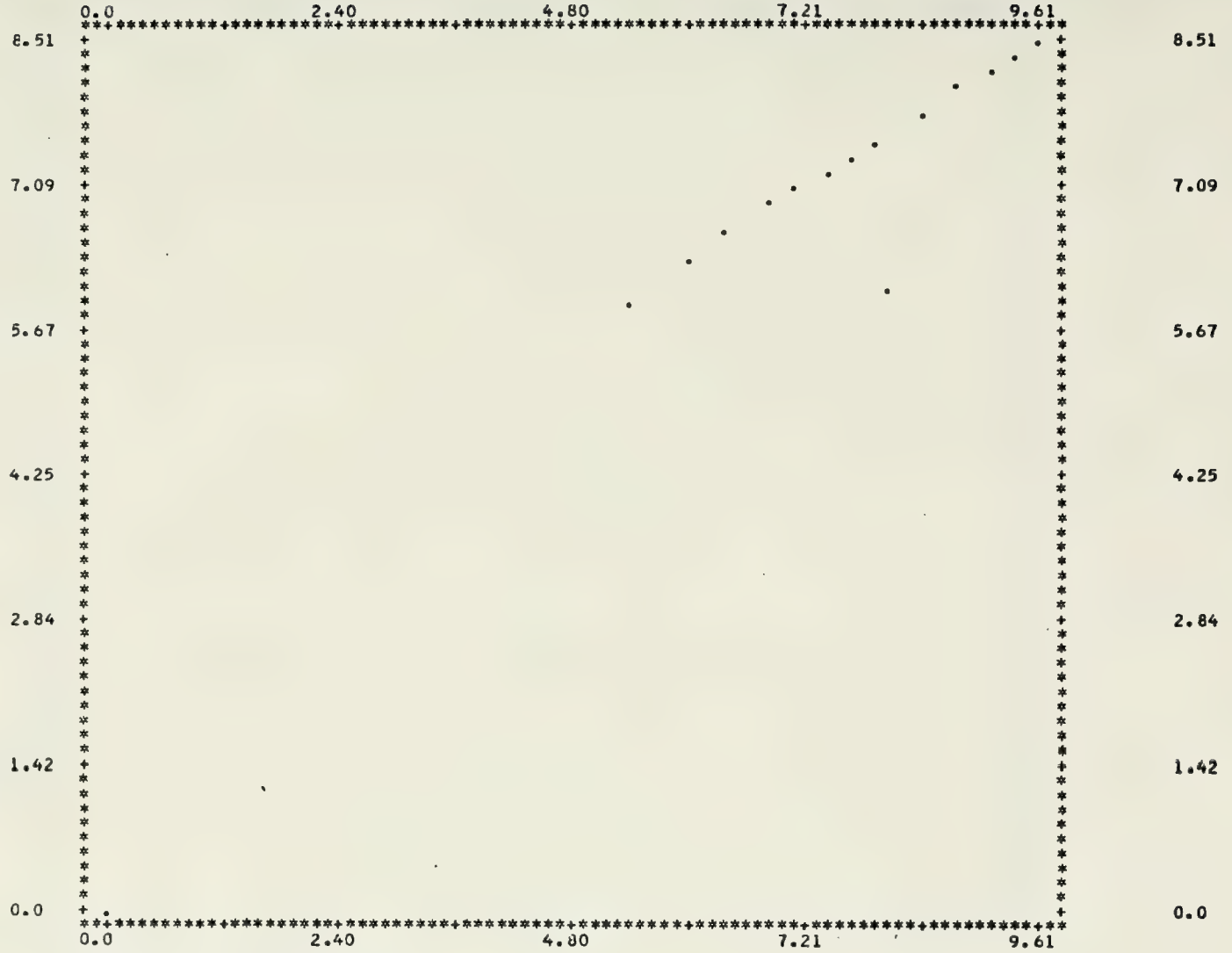

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Y-SCALE: "*"= 0.142E 00 UNITS

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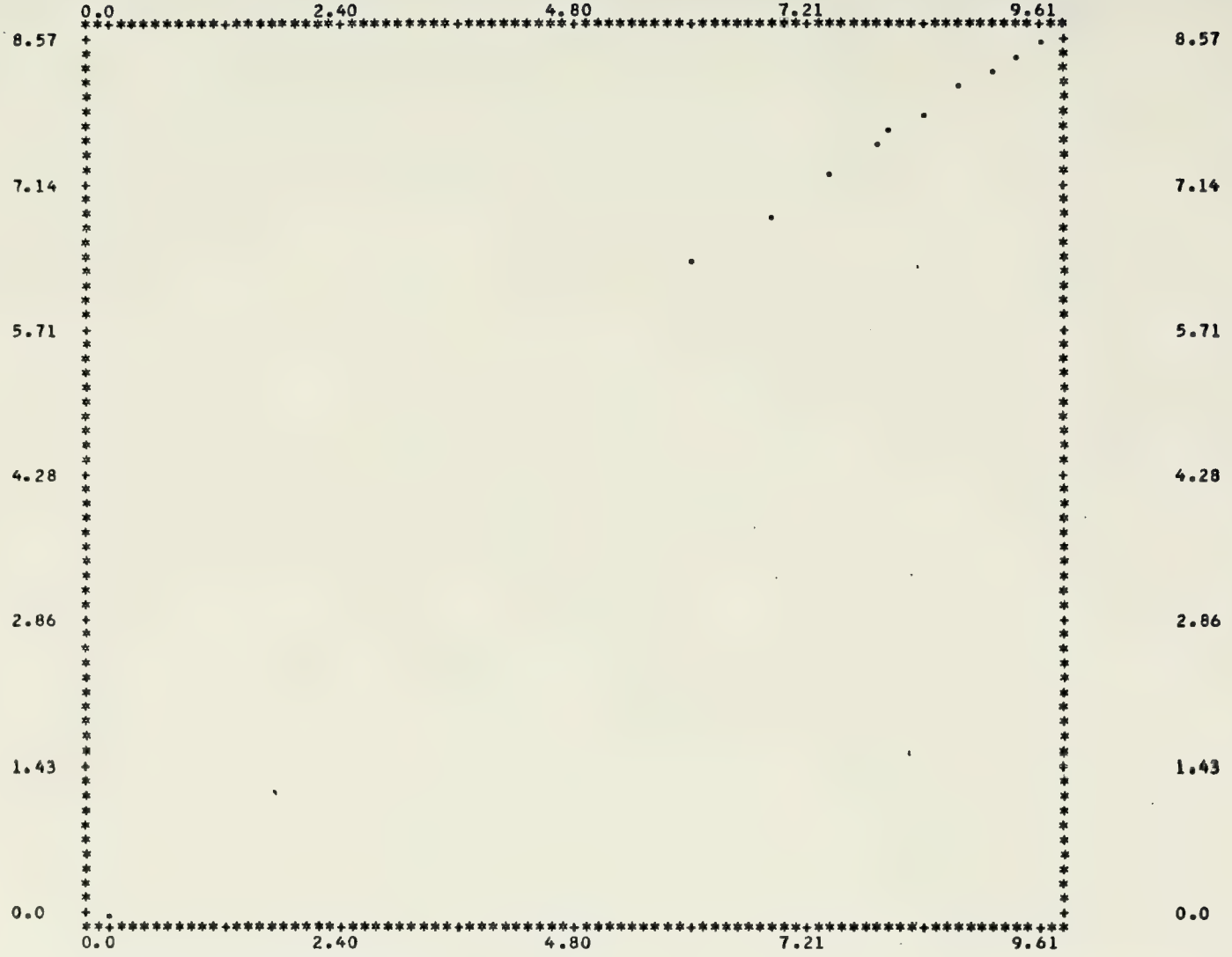

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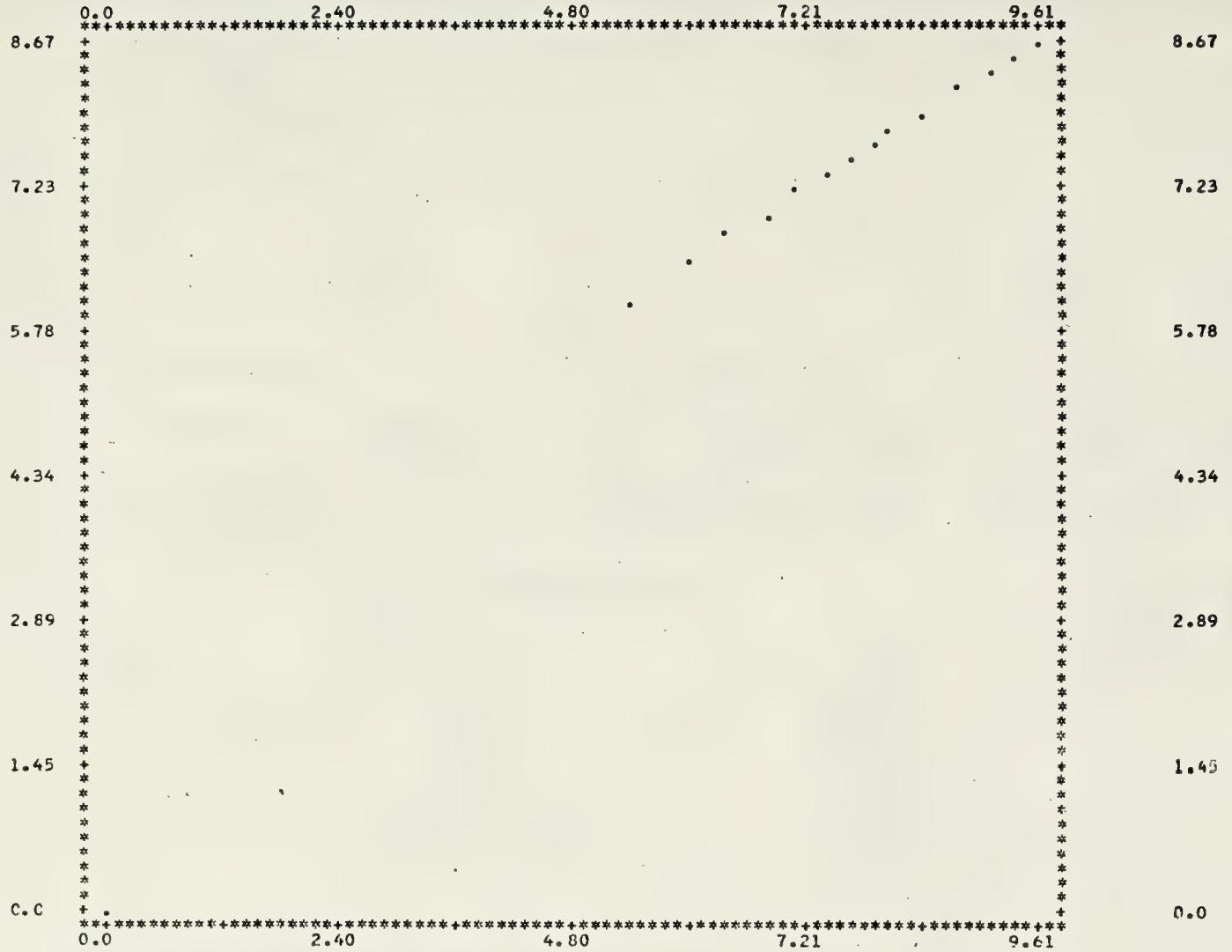
Y-SCALE: "*"= 0.143E 00 UNITS

HOT WIRE PROBE NUMBER 28



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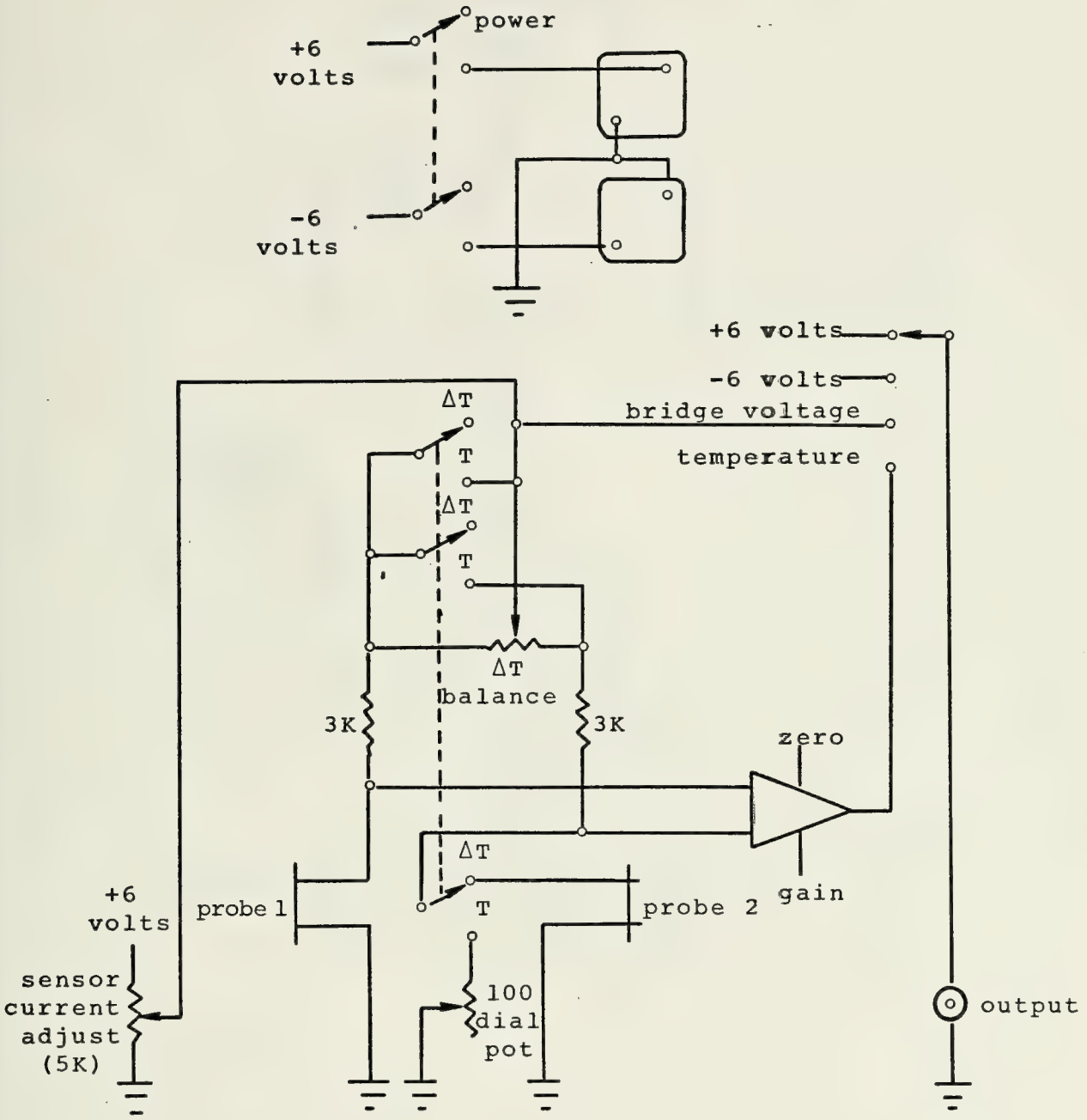
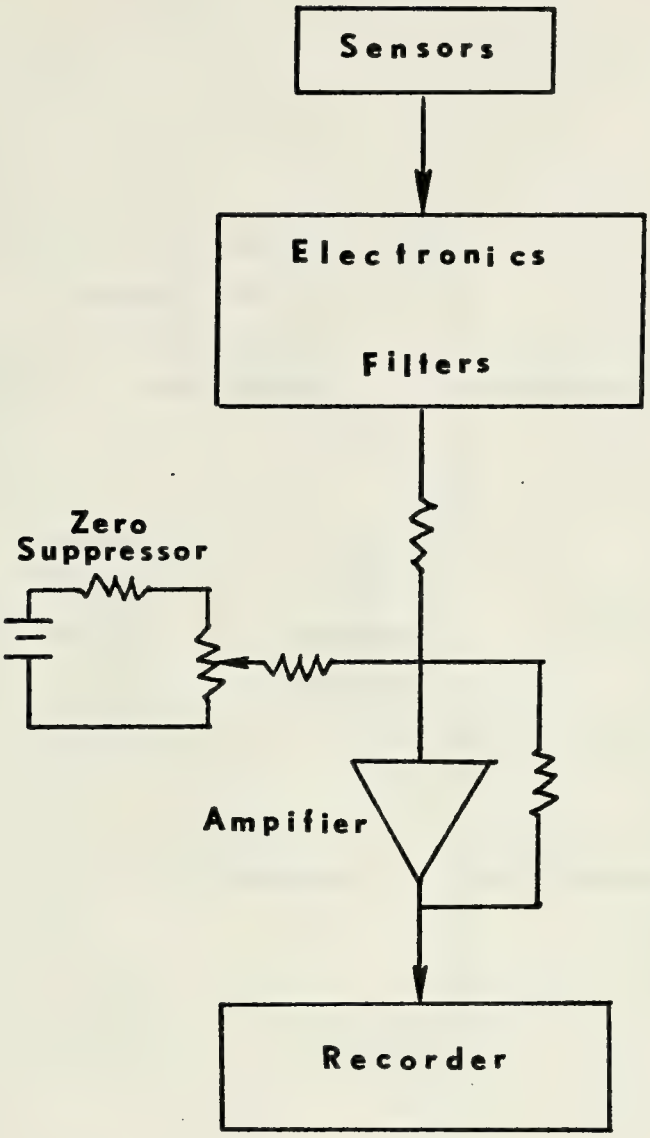
Y-SCALE: "*"= 0.145E 00 UNITS

HOT WIRE PROBE NUMBER 4A

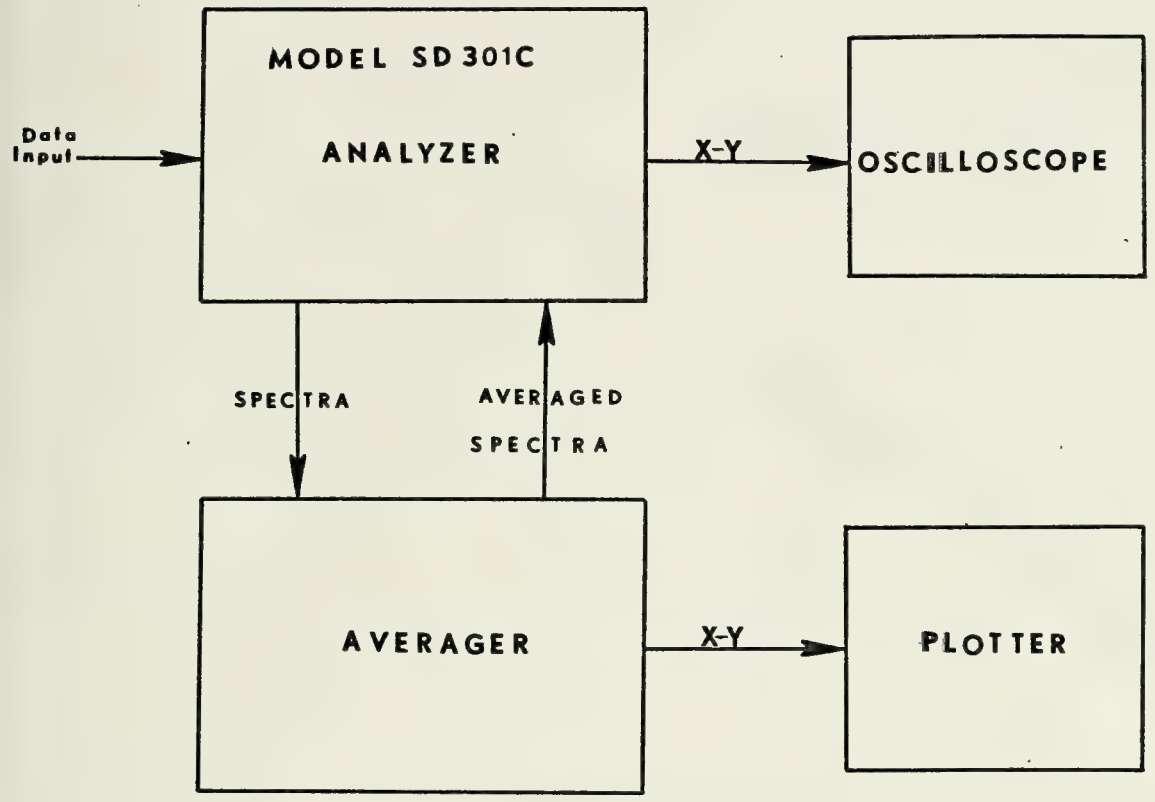
APPENDIX C


power
+6 volts
-6 volts
+6 volts
-6 volts
bridge voltage
temperature
ΔT
T
ΔT
T
ΔT balance
3K
3K
zero
gain
ΔT
T
probe 1
probe 2
+6 volts
sensor current adjust (5K)
100 dial pot
output

APPENDIX D


Sensors
Electronics
Filters
Zero
Suppressor
Ampifier
Recorder

APPENDIX E


MODEL SD 301C
ANALYZER
Data Input
X-Y
OSCILLOSCOPE
SPECTRA
AVERAGED SPECTRA
AVERAGER
X-Y
PLOTTER

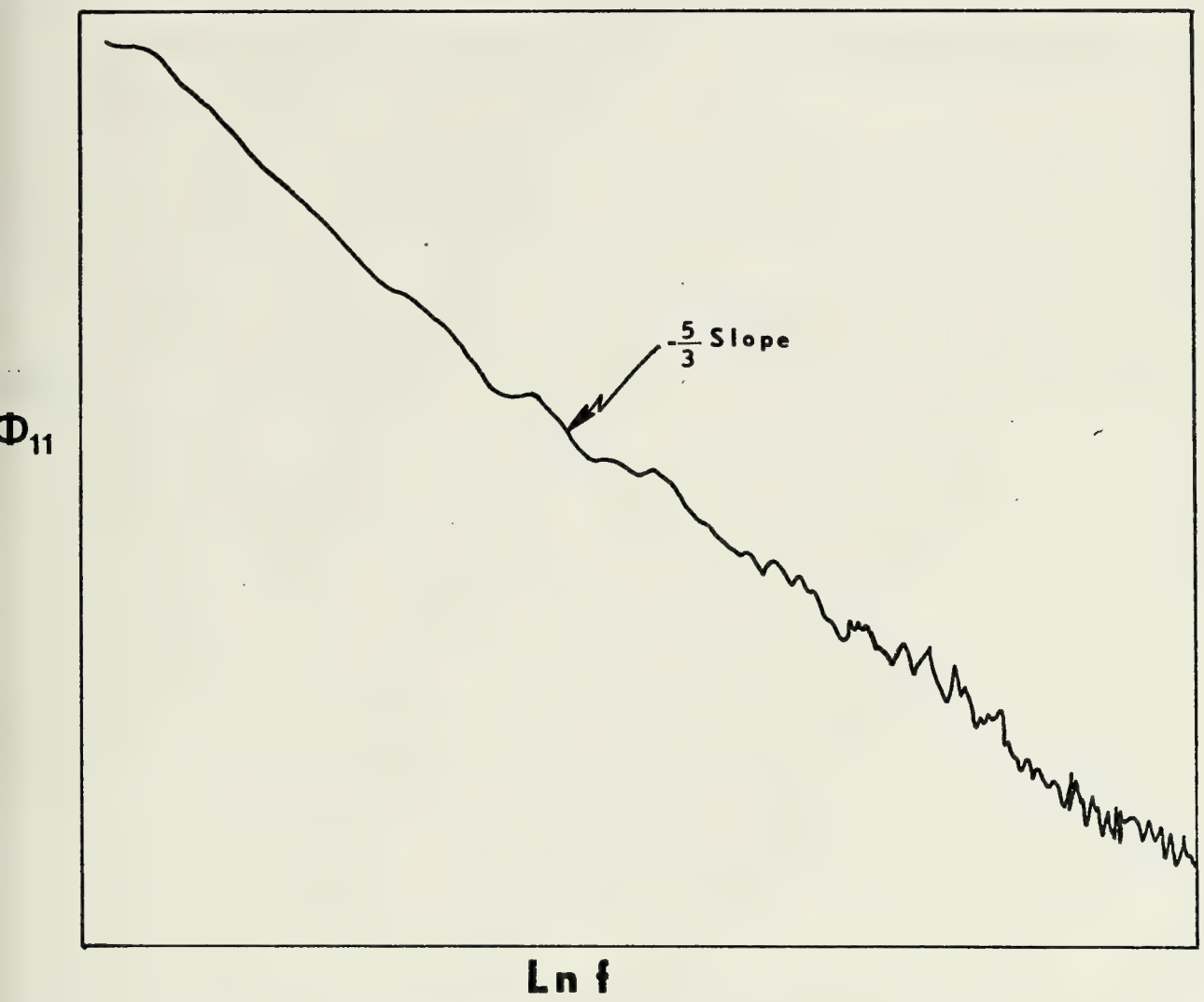


Figure E1. Real Time Spectral Analysis of Velocity Signal for 2008-2018 20 Sept 73.

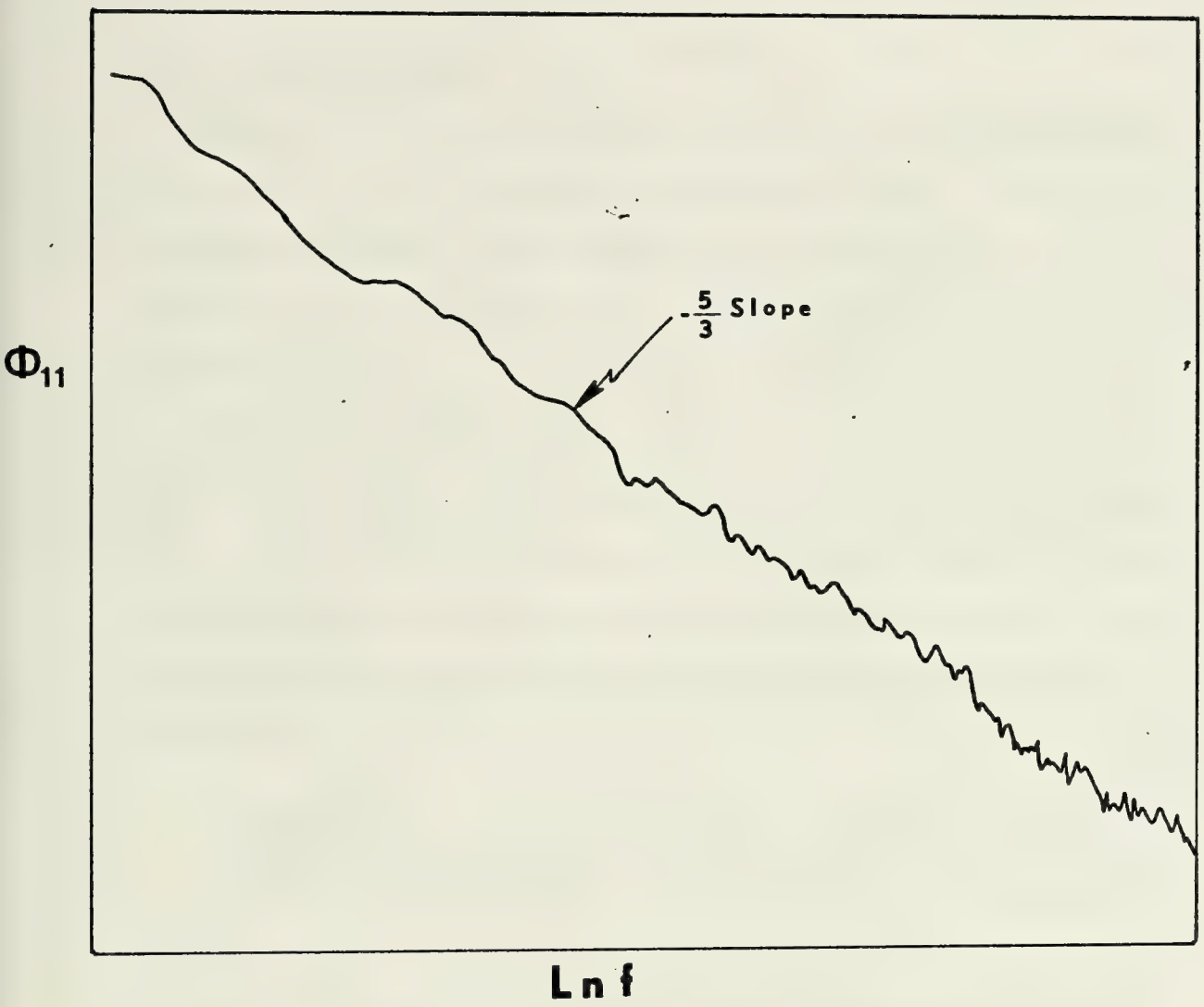


Figure E2. Real Time Spectral Analysis of Velocity Signal for 2023-2057 20 Sept 73.

APPENDIX F

A. TAPEOUT PROGRAM

TAPEOUT is a general purpose program used to determine the label and file contents of magnetic tapes. The program can take an otherwise unreadable tape and provide the user with sufficient information to permit access to the tape. TAPEOUT will print a file number, density, parity, length in bytes of the record and a dump of the record. In this study the two key outputs were the record length and record dump. These outputs permitted the user to obtain the block-size and ascertain the location of erroneous records. The following is an example of the TAPEOUT deck set-up used in this study.

```
//JOHNSTON JOB (2413,0392,XM24), 'JOHNSTON SMC 2561'
//EXEC TAPEOUT, PARM='2.0,,2'
//TAPEIN DD UNIT=2400-1,LABEL=(,BLP), VOL=SER=KARLYN
/*
```

TAPEOUT is part of the IBM 360/67 subroutine library and a discussion of the parameters (PARM=) is available in the computer center consultant's office and also in Computer Center Technical Note No. 0211-08.

B. CONVERT PROGRAM

The seven-track octal tape is converted into nine-track hexidecimal data samples using the CONVERT program. The block characteristics of the data samples are still

maintained on the nine-track tape but two additional parameters are affixed to each block. These two parameters, NCHAN and KMAX, are affixed to the beginning of each block. NCHAN is the number of channels of analog data digitized on the seven-track tape. KMAX is a numerical value set equal to the maximum number of samples per block. The insertion of these numerical parameters at the beginning of each block and the change in the block format by the FORM subroutine will put the seven-track tape in the proper format for use in the UBCFTOR program. The CONVERT program used in this study along with sample JCL cards is given below.

```
//JOHNSTON JOB (2413,0392,XM24),'JOHNSTON SMC 2561'
//CONVERT EXEC FORTCLG,REGION.GO=100K
//FORT.SYSIN DD
      DIMENSION IDAT(1024), DAT(1024)
      FACTOR = 1.
      REWIND 2
      REWIND 4
      NCHAN = 8
      NRECL = 1024
      J = 0
   10 READ (2,20,END=60,ERR=40) IDAT
   20 FORMAT (20(50A4),24A4)
      J=J+1
      CALL FORM(IDAT,NRECL)
      DO 30 I=1,NRECL
      WRITE (4) NRECL,NCHAN,DAT
      GO TO 10
   40 WRITE (6,50) J
   50 FORMAT ('0',5X,'READ ERROR,RECORD NO.=',I4)
      GO TO 10
   60 WRITE (6,70) J
   70 FORMAT ('0',5X,'END OF TAPE,RECORD NO.=',I4)
      END FILE 4
      RETURN
      END

/*
```

```
//GO.FT02F001 DD UNIT=2400-1, VOL=SER=KARLYN,LABEL=(,NL),
//    DISP=OLD,DCB=(DEN=2,RECFM=VS,BLKSIZE=8192)
//GO.FT04F001 DD UNIT=2400, VOL=SER=NPS170, DSNAME=DEREK,
      LABEL=(1,SL),DISP=(NEW,KEEP),DCB=(DEN=2,RECFM=VS,
//    BLKSIZE=8200)
```

It is noted that the user inputs to the program consist of the dimension of the arrays IDAT and DAT and the value of NRECL. IDAT and DAT should be dimensioned at least NSAMP x NCHAN thus signifying the need for recording the digitizing parameters. The argument NRECL must be assigned a value equal to NSAMP x NCHAN. The value of the scaling factor has been set equal to one in this study since it was found to be easier to perform all calibrations and scalings in one step following the use of the spectral analysis programs. Computer Center Technical Note No. 0211-08 provides additional information concerning the CONVERT program.

C. DIGITAL TAPE OPERATIONS

Unlike the Hybrid computer system, where all tape manipulations were performed by the user with technical assistance from the computer facility staff, the IBM 360 computer system manipulations were performed by the staff members. In order to have the tapes handled as desired, explicit instructions had to be given. These instructions were given in two ways. The first instruction consisted of a Job Request Form addressed to the computer center staff identifying the tapes to be utilized and whether they were to be read off of (RINGOUT) or written on (RINGIN). The second

instructional procedure was conducted using job control language (JCL) addressed to the computer and read as part of the submitted program.

1. Job Control Language

Job control language cards provide information to the computer about tape identification, tape disposition, tape data files, tape mount numbers and data format. The cards are appended to the program and read through the "hot card reader" as part of the program, whereas the Job Request Form is submitted "over the counter" to the computer center personnel. An example of a JCL card for tape processing would be:

```
//GO.FT08F001 DD UNIT=2400-1,VOL=SER=KARLYN,LABEL=(1,SL),
//    DSNAME=DEREK,DISP=(NEW,KEEP), DCB=(DEN=2,RECFM=VS,
//    BLKSIZE=8192)
```

While the majority of the JCL card remains unchanged, there are portions which are subject to change from tape to tape. These portions are discussed below.

FT08 - This group indicates the tape mount on which the tape is to be placed. The two digit number (08 in this case) must match the number provided in the program's "READ" or "WRITE" statement.

F001 - This group indicates the sequential number of passes through the tape which has occurred up to this point. In this case it is the first pass.

UNIT=2400-1 - This group specifies the tape as a seven-track tape. The nine-track designation is 2400.

VOL=SER=KARLYN - This group identifies the tape to be processed. In this case the name "KARLYN" signifies the tape is an "external" tape with the name "KARLYN" physically appearing on the tape. An "internal" tape would have a serial number such as NPS211. These tapes are kept on file in the computer center and cannot be physically removed from the facility.

LABEL=(1,SL) - This group identifies the tape file to be processed and specifies that the tape has a standard label. "External" tapes may be processed as no label tapes (NL) but "internal" tapes will be given a standard label before the user gains access to them. This is accomplished by the computer center staff processing a "canned" program which places a standard label on the serialized tape.

DSNAME=DEREK - This group specifies the data set name (DSNAME) applicable to the specified LABEL group. The data set name may be a unique name limited to six alphanumeric characters. Once a file has been given a data set name access to the data file can only be obtained if this same DSNAME is used. This process can be circumvented by the use of by-pass label processing (BLP) but does provide protection against accidental erasures.

DISP=(NEW,KEEP) - This group specifies the tape disposition once it has been processed.

DCB=(DEN=2,RECFM=VS,BLKSIZE=8192) - This group is referred to as the data control block. The density (DEN=2),

tape record format (RECFM=VS) and block size (BLKSIZE= 8192) are stipulated using this group. The density specifies the number of bytes per inch, in this case the number 2 denotes 556 bytes per inch. This corresponds to a manual setting of the DENSITY dial on the face of the seven-track tape unit. RECFM=VS specifies that the record format is variable spaced, the result of recording and digitizing on the seven track unit. The block size specifies the number of bytes per block of data. If 2048 words per block were used, four bytes per word would result in 8192 bytes per block.

APPENDIX G

A. GENERAL

All the UBC time series analysis programs (FTOR, SCOR, FC PLOT) were originally listed on faculty tape NPS216, file 1-3 respectively. The programs have since been placed on computer center disk, MARY, and are stored in machine language which disallows a listing of the program for user study. However, source decks for UBCFTOR and UBCSCOR have been retained by Dr. Kenneth Davidson of the Meteorology Department and by Dr. Noel Boston of the Oceanography Department. These source decks can be used to obtain a listing of the programs for individual study. The most recent computer center documentation on the use of the time series analysis package is given in the following memorandum written by Miss Sharon Raney of the computer center staff. This memorandum provides the information and JCL necessary for utilization of the disk-stored analysis programs.

B. FTOR

The preamble to the FTOR program is given following this discussion. It provides the user with the information needed to prepare the input data cards necessary for program execution. One of the most misleading parameters called for in the input values is the variable NBLOCK.

This value is provided by the user on the second data card with the value supposedly entered in columns 4-5. In actuality the value is read as a five digit integer thereby making the maximum value of NBLOCK 99999 vice 99 as implied by the program preface.

An important consideration involves the value of the variable MPRINT. This variable controls the computer printout of the FTOR program. If the user desires to suppress the printout the insertion of a specific value can save considerable paper and cut computer time significantly. In the unsuppressed mode, the output will follow the format shown in Figure 13, Section IV. The suppressed output will consist of one line outputs for each data block which will inform the user that "coefficients for block __ have been written on the file __ of the output tape." By using the suppressed output, computer turn-around time was significantly reduced.

C. SCOR

The preamble to the SCOR program also provides the user with the information necessary to compile the data input cards. The SCOR program requires the input of several variables whose values are determined during the A-D conversion process. One of the values on the first data card is the number of data blocks on which the spectral analysis will be performed. This value is set by the user and cannot exceed the number of data blocks processed by the FTOR

program. As was the case in the FTOR program the maximum number of blocks which can be handled is 99999 and not 99 as the preface would lead the user to believe.

As was discussed earlier in this thesis the output of the SCOR program consists of a computer printout and a graphic plot. The graphic plot consists of an output in which spectral density is plotted against frequency for all channels being processed. Since the original formulation of the SCOR program, the computer facility at the Naval Postgraduate School has installed a new plotting routine called NEWPLOT. This routine limits the user to 30 inches of plotting paper. The author found it necessary to submit a job request asking that plotting routine CALPLOT be used to prevent early termination of spectral plots consisting of four or more channels. The computer center staff has been alerted to this problem and any future user should consult with a staff member before using the SCOR program.

8 June 1973

MEMORANDUM

From: Sharon D. Raney
To: Users of UBC Time Series Analysis Package

Subj: New Operating Instructions for UBC Time Series Analysis Package

1. The new FTOR deck setup is given in Figure 1.

   The dimension size of array DATA must correspond to the block size of the data on the input tape. This tape is generally the data as converted from the seven track XDS generated tape to the nine track IBM/360 tape.

   Formerly, this array was dimensioned in subroutine OCEAN2 and had to be changed whenever the sample size changed. This meant the entire source deck for FTOR had to be used for each run.

   FTOR is now compiled in FORTRAN IV (H) which generates a more efficient code and consequently speeds up execution time.

2. When the same dimension size is to be used repeatedly, Figure 2 shows how to obtain an object deck and how to execute FTOR with the object deck.

3. Figure 3 shows the deck setup for SCOR.

4. Notice the change in the format of the Job Control Language (JCL) to define the tape files. These changes enable more efficient processing by the operator. Note the use of the IN parameter in the LABEL parameter. This must be specified when the file is to be read only. OUT is used when the file is to be written only. All data sets are PASSed not KEEP. The UNIT-AFF is used on subsequent files of a tape as is the VOL=REF.

5. Any questions concerning these new operating instructions should be directed to Sharon Raney at X2631 or Ingersoll Hall Room 107.

```
//FTOR EXEC FORTHCLG,REGION.FORT=150K,REGION.GO=175K
//FORT.SYSIN DD *
      DIMENSION DATA(3072)
      CALL FTOR(DATA)
      RETURN
      END
//LINK.SYSLIB  DD
//             DD
//             DD  DSNAME=F1178.TSLIB,UNIT=2314,VOL=SER=MARY,DISP=SHR
//GO.FT08F001 DD UNIT=2400,VOL=SER=NPS290,DISP=(OLD,PASS),
//    DSN=DEREK,DCB=(DEN=2,RECFM=VS,BLKSIZE=6152),LABEL=(1,SL,,IN)
//GO.FT08F002 DD UNIT=AFF=FT08F001,VOL=REF=*.GO.FT08F001,DSN=DEREK,
// DISP=(OLD,PASS),LABEL=(2,SL,,IN),DCB=(DEN=2,RECFM=VS,BLKSIZE=6152)
//GO.FT08F003 DD UNIT=AFF=FT08F001,VOL=REF=*.GO.FT08F001,DSN=DEREK,
// DISP=(OLD,PASS),LABEL=(3,SL,,IN),DCB=(DEN=2,RECFM=VS,BLKSIZE=6152)
//GO.FT03F001 DD UNIT=2400,VOL=SER=NPS133,DISP=(NEW,PASS),
//    DSN=COEFQ1,DCB=(DEN=2,RECFM=VS,BLKSIZE=12300),LABEL=(1,SL,,OUT)
//GO.FT03F002 DD UNIT=AFF=FT03F001,VOL=REF=*.GO.FT03F001,DSN=COEFQ1,
// DISP=(NEW,PASS),LABEL=(2,SL,,OUT),DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//GO.FT03F003 DD UNIT=AFF=FT03F001,VOL=REF=*.GO.FT03F001,DSN=COEFQ1,
// DISP=(NEW,PASS),LABEL=(3,SL,,OUT),DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//GO.SYSIN  DD  *

          FTOR DATA CARDS GO HERE
```

Figure G1.

```
//FTOR  EXEC  FORTHCD,REGION.FORT=150K
//FORT.SYSIN  DD  *
      DIMENSION DATA(3072)
      CALL FTOR(DATA)
      RETURN
      END

//FTOR  EXEC  LGO,REGION.GO=175K
//LINK.SYSLIB  DD
//            DD
//            DD  DSNAME=F1178.TSLIB,UNIT=2314,VOL=SER=MARY,DISP=SHR
//LINK.SYSIN  DD  *

            OBJECT DECK PUNCHED IN ABOVE JOB GOES HERE - MAKE SURE
            THERE ARE NO BLANK CARDS ON FRONT OR BACK OF THIS DECK

//GO.FT08F001 DD UNIT=2400,VOL=SER=NPS290,DISP=(OLD,PASS),
//    DSN=DEREK,DCB=(DEN=2,RECFM=VS,BLKSIZE=6152),LABEL=(1,SL,,IN)
//GO.FT08F002 DD UNIT=AFF=FT08F001,VOL=REF=*.GO.FT08F001,DSN=DEREK,
// DISP=(OLD,PASS),LABEL=(2,SL,,IN),DCB=(DEN=2,RECFM=VS,BLKSIZE=6152)
//GO.FT08F003 DD UNIT=AFF=FT08F001,VOL=REF=*.GO.FT08F001,DSN=DEREK,
// DISP=(OLD,PASS),LABEL=(3,SL,,IN),DCB=(DEN=2,RECFM=VS,BLKSIZE=6152)
//GO.FT03F001 DD UNIT=2400,VOL=SER=NPS133,DISP=(NEW,PASS),
//    DSN=COEFQ1,DCB=(DEN=2,RECFM=VS,BLKSIZE=12300),LABEL=(1,SL,,OUT)
//GO.FT03F002 DD UNIT=AFF=FT03F001,VOL=REF=*.GO.FT03F001,DSN=COEFQ1,
```

Figure G2.

```
// DISP=(NEW,PASS),LABEL=(2,SL,,OUT),DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//GO.FTC3F003 DD UNIT=AFF=FT03F001,VOL=REF=*.GO.FT03F001,DSN=COEFQ1,
// DISP=(NEW,PASS),LABEL=(3,SL,,OUT),DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//GO.SYSIN  DD  *

          FTOR DATA CARDS GO HERE
```

```
//  EXEC  PGM=UBCSCOR,REGION=150K
//STEPLIB  DD  UNIT=2314,VOL=SER=MARY,DSNAME=F1178.TSLIB,DISP=SHR
//FT06F001 DD SYSOUT=A
//SYSPLOT DD SYSOUT=B
//SYSPLOTS DD UNIT=SYSDA,SPACE=(TRK,(2,6))
//FT03F001 DD UNIT=2400,VOL=SER=NPS133,DISP=(OLD,PASS),
//    LABEL=(1,SL,,IN),DSN=COEFQ1,DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//FT03F002  DD  UNIT=AFF=FT03F001,VOL=REF=*.FT03F001,DISP=(OLD,PASS),
//    LABEL=(2,SL,,IN),DSN=COEFQ1,DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//FT03F003  DD  UNIT=AFF=FT03F001,VOL=REF=*.FT03F001,DISP=(OLD,PASS),
//    LABEL=(3,SL,,IN),DSN=COEFQ1,DCB=(DEN=2,RECFM=VS,BLKSIZE=12300)
//FT05F001 DD *

          SCOR DATA CARDS GO HERE
```

Figure G3.

```
C FOURIER TRANSFORM OF TIME SERIES DATA SUPPLIED THROUGH
C 'OCEAN' SUBROUTINES USING P-K FORT FAST FOURIER TRANSFORM
C SUBROUTINE (SHARE SDA3465) IN THE IBM SYSTEM 360 MODEL 67.
C
C LAST REVISION JANUARY 24,1969                JOHN GARRETT
C
C   NBLOCK BLOCKS OF 2**NPOW SAMPLES EACH ARE READ FOR KCHAN OF THE
C NCHAN CHANNELS AVAILABLE TO THE 'OCEAN' SUBROUTINES.  THE CONTENTS OF
C ANY CHANNEL MAY BE REPLACED BY A LINEAR COMBINATION OF ITSELF WITH ANY
C OTHER CHANNEL.
C
C  FOR EACH BLOCK 2**(NPOW-1) COMPLEX FOURIER COEFFICIENTS ARE
C COMPUTED FOR EACH OF THE KCHAN CHANNELS.  THESE ARE THEN WRITTEN ON THE
C OUTPUT (TAPE) 03 IN THE FORMAT DESCRIBED BELOW. IN ADDITION THE
C COEFFICIENTS MAY BE SUMMED IN GROUPS OF (2**(NPOW-1))/32 AND
C PRINTED OUT.
C
C  ADDITIONAL OPTIONS ARE DESCRIBED UNDER THE RELEVANT CONTROL
C PARAMETERS BELOW.
C
C      IT SHOULD BE NOTED THAT THE COEFFICIENTS PRODUCED ARE THOSE OF THE
C FOURIER SERIES
C      Y(J) = SUM OVER K = 0,N/2 OF REAL PARTS OF
C                  (C(K)*EXP((2*PI*I/N)*J*K))
C      WITH J = 0,N-1,Y(J)REAL,AND I = SQRT(-1)
C
C THE FOLLOWING SUBROUTINES ARE REQUIRED
C       OCEAN1,OCEAN2,OCEAN3,RWUNLD
C       SKPFL
C       CONVOL
C       USCRMB
C       P-K FORT
C
C THE FOLLOWING LOGICAL INPUT/OUTPUT DEVICES ARE USED IN THIS PROGRAM
C       2 = SCRATCH TAPE FOR TEMPORARY STORAGE OF COEFFICIENTS IF
C           LOFR=1 BELOW
C       3 = OUTPUT (TAPE) FOR COEFFICIENTS
C       5 = (CARD) INPUT FOR CONTROL PARAMETERS
C       6 = PRINTED OUTPUT
C       INUNIT = INPUT TAPE OF TIME SERIES DATA FOR 'OCEAN' SUBROUTINES
C
C INPUT INFORMATION REQUIRED
C    *****IMPORTANT NOTE. READ THE COMMENT CARDS IN THE OCEAN
C    SUB-ROUTINE.  SOME FACTORS WILL HAVE TO BE CHANGED TO FIT BLKSIZE.
C     FIRST DATA CARD IN COLUMN NUMBER
C     1-9    IDUSER = USER IDENTIFICATION NUMBER (9-DIGIT INTEGER)
C     14-15  NCHAN = NUMBER OF CHANNELS DIGITIZED ON OCEAN TAPE
C     25     NTYPE = (NOT RELEVENT. SET TO ZERO.)
```

```
C      34-35 INFILE = FILE NUMBER OF DATA ON OCEAN TAPE
C      44-45 INUNIT = NUMBER OF UNIT ON WHICH INPUT TAPE IS MOUNTED
C      55    NSEARH = (NOT RELEVENT. SET TO ZERO.)
C      61-70 SAMFRQ = SAMPLING FREQUENCY OF DIGITIZING  (SAMPLES/SECOND)
C                     (MUST  INCLUDE  A DECIMAL POINT )
C      SECOND DATA CARD
C      4-5   NBLOCK = NUMBER OF BLOCKS DESIRED
C      14-15 NPOW- MAXIMUM NUMBERS OF SAMPLES PER BLOCK WILL BE 2**NPOW,
C              MAX NPOW IS 13 (8192 SAMPLES/BLOCK) BUT NPOW WILL BE
C              REDUCED UNTIL (2**NPOW)*KCHAN WILL FIT IN MEMORY. FOR
C              KCHAN OF 10 THIS WILL GIVE NPOW = 10 (1024 SAMPLES/BLOCK).
C      24-25 MTAPE =+1 FOR OUTPUT TAPE TO BE WRITTEN
C                  =-1 FOR NO OUTPUT TAPE
C      34-35 NFILE - OUTPUT COEFFICIENTS WILL BE NFILE-TH FILE ON TAPE
C      43-45 MAXERR = (NOT RELEVENT. SET TO ZERO.)
C      54-55 MPRINT = -1 SUPPRESSES SUMMARY COEFFICIENTS PRINT OUT
C                   = 0 OR GREATER PERMITS PRINT OUT
C      THIRD DATA CARD
C      4-5   KCHAN = NUMBER OF CHANNELS TO BE TRANSFORMED (MAX 10)
C      15    LOFR = 2 IF COEFFICIENTS TO BE COMPUTED FROM DATA SMOOTHED
C                   AND SUBSAMPLED (DECIMATED) USING CONVOL SUBROUTINE.
C                   WEIGHTS USED IN SMOOTHING AND DECIMATING FACTOR ARE
C                   DETERMINED BY CHOICE OF CONVOL USED.
C           = 1 IF ALTERNATE BLOCKS TO BE MADE UP OF SAMPLES FROM DATA
C                   SMOOTHED AND DECIMATED USING CONVOL SUBROUTINE.
C                   COEFFICIENTS WILL APPEAR ON OUTPUT TAPE IN FILE
C                   IMMEDIATELY FOLLOWING THAT CONTAINING RESULTS FROM
C                   UNSMOOTHED DATA
C               = 0 IF DATA TO BE LEFT ALONE
C      25    IHANN = 1 IF FOURIER COEFFICIENTS TO BE HANNED AND
C                    NORMALIZED (*SQRT(8/3))
C                  = 0 IF NOT
C
C      NEXT KCHAN CARDS
C      1-5   NO. OF PRIMARY A TO D CHANNEL
C      6-10  NO. OF SECONDARY A TO D CHANNEL
C      11-20 CALIBRATION ASSOCIATED WITH THE PRIMARY A TO D CHANNEL
C      21-30 CALIBRATION ASSOCIATED WITH THE SECONDARY A TO D CHANNEL
C      31-66 ALPHAMERIC NAME OF RESULTING PRIMARY CHANNEL
C      71-78 8 CHARACTER NAME OF UNITS FOR RESULTING PRIMARY CHANNEL
C
C  THE DATA TRANSFORMED AS THE PRIMARY CHANNEL IS THEN
C
C      CALIBRATION1 X VALUE OF PRIMARY + CALIBRATION2 X VALUE OF
C      SECONDARY CHANNEL
C
C
C  A SECOND SET OF DATA CARDS WILL PRODUCE A SECOND ANALYSIS. A BLANK
```

```
C CARD TERMINATES THE RUN.
C
C FORMAT OF OUTPUT TAPE FOR EACH BLOCK TRANSFORMED IS AS FOLLOWS
C      FIRST LOGICAL RECORD IS AN ARRAY OF 256 WORDS CALLED
C     ARTAPE
C      ARTAPE(1)= IDUSER
C      ARTAPE(2)= BLOCK NUMBER
C      ARTAPE(3) = NUMBER OF SAMPLES /BLOCK
C      ARTAPE(4) = NTAP (SEE BELOW)
C      ARTAPE(5) = NUMBER 6F CHANNELS TRANSFORMED
C      ARTAPE(6) = SAMPLING FREQUENCY
C      ARTAPE(10) = IHANN
C      ARTAPE(10+K) = MCHAN(K)
C      ARTAPE(31+9(K-1)) = ACHNAM(K)     (9A4)
C      ARTAPE(121+2(K-1)) = AUNITS(1,K)   (2A4)
C      ARTAPE(140+K) = CAL(K)
C
C      NEXT NTAP LOGICAL RECORDS OF 256 WORDS EACH CALLED
C     TAPRAY AND CONSIST OF
C      1 WORD CONTAINING INTEGER HARMONIC NO (0 TO IBLOCK/2) FOLLOWED BY
C      2*KCHAN WORDS CONTAINING FOR EACH OF THE KCHAN CHANNELS THE
C        REAL PART OF THE FOURIER COEFF  AT THIS HARMONIC(FIRST WORD)
C        FOLLOWED BY THE IMAGINARY PART(SECOND WORD).
C      ONLY COMPLETE SEQUENCES OF 1+(2*KCHAN) WORDS ARE INCLUDED IN A
C      TAPRAY SO THAT THE LAST FEW WORDS MAY CONTAIN ZEROS
C
C AN END OF FILE IS WRITTEN ON THE OUTPUT TAPE AT THE END OF A SEQUENCE
C      OF BLOCKS
C
C   J.F. GARRETT                    INSTITUTE OF OCEANOGRAPHY
C   J.R. WILSON                     UNIVERSITY OF BRITISH COLUMBIA
C                                   VANCOUVER 8,CANADA
C
```

```
C                                                                       00010
C  SPECTRUM AND CROSS SPECTRUM STATISTICS FROM FOURIER                  00020
C  COEFFICIENT TAPE PRODUCED BY 'FTOR' PROGRAM ON IBM                   00030
C  SYSTEM 360 MODEL 67                                                  00040
C                                                                       00050
C  LAST REVISION JANUARY 27,1969          JOHN GARRETT                  00060
C                                                                       00070
C  THIS PROGRAM READS FOURIER COEFFICIENTS FROM TAPE PRODUCED BY FTOR    00080
C  PROGRAM, AND FROM THE APPROPRIATE SUMS OF THESE PRODUCES SPECTRA AND  00090
C  COSPECTRA. THE SUMS USED MAY BE FIXED WITH FREQUENCY OR MAY GO IN HALF00100
C  OCTAVES FROM A SPECIFIED LOW FREQUENCY. AN AVERAGE, STANDARD DEVIATION00110
C  AND LINEAR COEFFICIENT OF REGRESSION OVER THE IBMAX BLOCKS USED (SEE  00120
C  FTOR DESCRIPTION) ARE GIVEN FOR EACH VALUE OF SPECTRAL DENSITY.       00130
C  AT EACH FREQUENCY, THE COSPECTRUM BETWEEN (1) AND (2) IS GIVEN BY     00140
C        ( R(1)*R(2) + I(1)*I(2))/ 2.0                                  00150
C     A VARIETY OF PLOTTED OUTPUT IS AVAILABLE.  IN ALL A HORIZONTAL BAR 00160
C  INDICATES THE FREQUENCY INTERVAL INCLUDED IN THE ESTIMATE PLOTTED, AND00170
C  A VERTICAL BAR INDICATES THE EXPECTED STANDARD DEVIATION OF THE       00180
C     SERIES (N) AT THAT FREQUENCY                                      00190
C  AND THE QUADRATURE SPECTRUM BY                                       00200
C                                                                       00210
C        ( R(2)*I(1) - R(1)* I(2))/ 2.0                                 00220
C  WHERE ( R(N) + (I(N)*SQRT(-1)) ) IS THE COMPLEX FOURIER COEFFICIENT  00230
C  ESTIMATE (= STD.DEV. OF BLOCKS AVERAGED TO GIVE ESTIMATE/ SQRT(NUMBER00240
C     OF BLOCKS))                                                       00250
C                                                                       00260
C  THE FOLLOWING SUBROUTINES MUST BE SUPPLIED BY USER                   00270
C       PHASES                                                          00280
C       PLVAL,TIC,LABEL                                                 00290
C                                                                       00300
C  THE FOLLOWING LOGICAL INPUT/OUTPUT UNITS ARE USED BY THIS PROGRAM    00310
C       3= (TAPE) SUPPLYING COEFFICIENTS AND IDENTIFICATION AS          00320
C          PRODUCED BY FTOR                                             00330
C       5= (CARDS) CONTROL PARAMETERS                                   00340
C       6= PRINTED OUTPUT                                               00350
C                                                                       00360
C  THE FOLLOWING INPUT IS REQUIRED                                      00370
C                                                                       00380
C  A CARD IS REQUIRED TO IDENTIFY YOUR GRAPHICAL OUTPUT FOR THE COMPUTING00390
C  CENTRE STAFF. IT MUST BE PRESENT WHETHER PLOTS ARE PRODUCED OR NOT.   00400
C  THE FIRST 72 COLUMNS OF THIS CARD WILL BE REPRODUCED ON THE BEGINNING00410
C  OF YOUR PLOT. THIS CARD APPEARS ONLY ONCE IN THE JOB AND IS THE FIRST00420
C  DATA CARD. THE FOLLOWING SET OF CARDS IS PRESENT FOR EACH FILE OF    00430
C  FOURIER COEFFICIENTS TO BE PROCESSED.                                00440
C                                                                       00450
C   FIRST CARD,IN COLUMN                                                00460
C      1-9    IDUSER = USER IDENTIFICATION NUMBER FOR DATA DESIRED      00470
C      14-15 ICMAX = NUMBER OF CHANNELS TO BE USED (MAX 10)             00480
```

```
C     24-25 IBMAX = NUMBER OF DATA BLOCKS FOR STATISTICS                    00490
C     34-35 IBSTAR = STATISTICS START WITH BLOCK NO. IBSTAR                 00500
C     44-45 NFILE = DATA IS IN NFILE-TH FILE ON FOURIER COEFFICIENT TAPE    00510
C      54     IAXIS = 0 (BLANK) IF PLOT AXES TO BE SET BY PROGRAM          00520
C                  = 1 IF AXES TO BE SET BY USER                           00530
C      55     IPLOT = 0 IF NO PLOTTED OUTPUT DESIRED                       00540
C                 =1 IF SPECTRAL DENSITY TO BE PLOTTED AGAINST FREQUENCY   00550
C                 =2 IF LOG10 SPECTRAL DENSITY TO BE PLOTTED AGAINST FREQUENCY00560
C                 =3 IF LOG10 SPECTRAL DENSITY TO BE PLOTTED AGAINST LOG10 00570
C                   FREQUENCY                                              00580
C                 =4 IF       (FREQ*SPECTRAL DENSITY) TO BE PLOTTED        00590
C                   AGAINST LOG10 FREQUENCY                                00600
C                 =5 SAME AS IPLOT=1 EXCEPT COHERENCE AND PHASE PLOTTED    00610
C                   INSTEAD OF CO AND QUAD SPECTRA                         00620
C                 =6 SAME AS =2 EXCEPT COHERENCE AND PHASE PLOTTED INSTEAD 00630
C                   OF CO AND QUAD                                         00640
C                 =7 SAME AS 3 EXCEPT COHERENCE AND PHASE INSTEAD OF CC+QU 00650
C                 = 8 SAME AS 4 WITH COHERENCE AND PHASE INSTEAD OF CO + QU 00660
C      65     IPHASE = 0 FOR NO PHASE CORRECTIONS                          00670
C                   = 1 FOR PHASES TO BE CORRECTED.                        00680
C                                                                          00690
C  CARD INSERTED ONLY IF IAXIS = 1                                         00700
C    IN COLUMN                                                             00710
C    1-10   VALUE OF ORIGIN FOR SPECTRUM AND COSPECTRUM AXIS(F10.)         00720
C    11-20  UNITS PER INCH FOR SPECTRUM AND COSPECTRUM AXIS (F10.)         00730
C                 AXIS WILL BE 5.00 INCHES LONG                            00740
C    21-30  VALUE OF ORIGIN FOR QUADSPECTRUM AXIS  (F10.)                  00750
C    31-40  UNITS PER INCH FOR QUAD SPECTRUM AXIS (F10.) AXIS WILL BE      00760
C                 5.00 INCHES LONG.  (COHERENCE AND PHASE WILL BE          00770
C                 SCALED BY PROGRAM IF PLOTTED INSTEAD OF CO AND QUAD.)    00780
C    41-50 VALUES OF ORIGIN FOR FREQUENCY AXIS (F10. )                     00790
C    51-60  UNITS PER INCH FOR FREQUENCY AXIS (F10.)                       00800
C    61-70  LENGTH OF FREQUENCY AXIS IN INCHES (F10.)                      00810
C  N.B. WHEN LOG10 PLOTS HAVE BEEN REQUESTED NUMBERS ABOVE MUST ALL        00820
C    REFER TO LOG10,.E.G. UNITS PERINCH = 1.00 MEANS 1 DECADE PER INCH     00830
C                                                                          00840
C NEXT CARD,IN COLUMN                                                      00850
C      5      LINOCT = 0 FOR CONSTANT BANDWIDTH,GIVEN BY BANDW BELOW       00860
C                   = 1 FOR EXPONENTIAL BANDWIDTHS ( GIVES LOG10 FREQ.     00870
C                       SCALE IN ALL PLOTS  )                              00880
C      6-15   STRFRQ = APPROXIMATE CENTER FREQUENCY OF FIRST POINT OF      00890
C                     SPECTRUM, IN HERTZ. (MUST INCUDE A DECIMAL POINT)    00900
C                     FIRST BAND WILL INCLUDE ZEROTH HARMONIC IF STRFRQ     00910
C                     IS LESS THAN BANDW                                   00920
C      16-25 BANDW = APPROX. BANDWIDTH FOR FIXED BANDWIDTH SPECTRA,        00930
C                    IN HERTZ. (MUST INCLUDE A DECIMAL POINT)              00940
C      30      INDOW = 1 IF FOURIER COEFFCIENTS TO BE HANNED BEFORE        00950
C                    SPECTRA COMPUTED                                      00960
```

```
C                    = 0 IF NOT                                                 00970
C   SUBSEQUENT ICMAX CARDS                                                      00980
C      4-5    CHANNEL NUMBER OF A CHANNEL FOR WHICH SPECTRA ARE WANTED         00990
C             NUMBER IS USUALLY NUMBER OF A-D CHANNEL USED FOR CONVERSION      01000
C      14-15,19-20,24-25,29-30 TO 59-60 , CHANNEL NUMBERS OF UP TO ICMAX       01010
C             CHANNELS FOR WHICH CROSS SPECTRA WITH CHANNEL GIVEN IN           01020
C             COLS.4-5 ARE DESIRED. SPECTRUM IS HERE CONSIDERED AS CROSS       01030
C             SPECTRUM OF CHANNEL WITH ITSELF, I.E. THE NUMBER IN 4-5          01040
C             MUST REAPPEAR IF SPECTRUM IS TO BE OBTAINED. ALSO,CROSS          01050
C             SPECTRA ARE DONE ONLY IF EACH CHANNEL APPEARS IN THE LIST        01060
C             ON THE OTHER CHANNELS CARD. THUS TO GET SPECTRUM FOR             01070
C             CHANNEL 2 AND CROSS SPECTRUM BETWEEN 2 AND CHANNEL 8, THERE      01080
C             MUST BE A CARD WITH  2 IN COL.5 AND BOTH 2 AND 8 IN THE LIST     01090
C             AND ANOTHER CARD WITH 8 IN COL.5 AND 2 IN THE LIST.              01100
C                                                                              01110
C   PHASE CORRECTION DECK( INSERT ONLY IF IPHASE NOT ZERO )                    01120
C     PHASE COPRECTIONS APPLIED WILL BE OBTAINED BY LINEAR INTERPOLATION       01130
C      BETWEEN VALUES SUPPLIED AT FREQUENCIES LISTED BELOW                     01140
C   FIRST K CARDS( K LESS THAN 6 )                                             01150
C      1-10,11-20,....,71-80 , FREQUENCIES( F10.4 ) AT WHICH PHASE             01160
C        CORRECTIONS ARE TO BE SUPPLIED ( UP TO 48 OF THEM )                   01170
C          IF LESS THAN THE FULL 48 FREQUENCIES ARE SUPPLIED, THEN             01180
C             THE LAST FREQUENCY MUST BE LEFT BLANK.                           01190
C   SUBSEQUENT ICMAX SETS OF K CARDS EACH                                      01200
C      1-10,11-20,....,71-80 , PHASE CORRECTIONS( F10.4 ) TO BE APPLIED        01210
C        AT THE ABOVE FREQUENCIES. EACH SET CONTAINS THE CORRECTIONS           01220
C          FOR A GIVEN CHANNEL, AND THE SETS ARE IN THE SAME ORDER AS THE      01230
C          SPECTRUM CARDS. IF NO CORRECTIONS ARE TO BE APPLIED TO A            01240
C          CHANNEL, THE K CARDS FOR THAT CHANNEL SHOULD BE BLANK.              01250
C              CORRECTIONS MUST BE IN RADIANS. A POSITIVE CORRECTION WILL      01260
C          CAUSE THE CORRECTED PHASE TO LEAD THE UNCORRECTED ONE.              01270
C                                                                              01280
C   LAST CARD MUST BE BLANK UNLESS ANOTHER FILE IS TO BE PROCESSED, IN         01290
C   WHICH CASE A COMPLETE NEW SEQUENCE OF CARDS APPROPRIATE TO THE NEW         01300
C   FILE SHOULD FOLLOW.                                                        01310
C                                                                              01320
```

```
C*************************************************************************
C*************************************************************************
C*************************************************************************
C***                                                                   ***
C***                                                                   ***
C***                                                                   ***
C***   THIS PROGRAM WAS DESIGNED TO COMPUTE EPSILON AND USTAR VALUES   ***
C***   FROM INPUTS OF SPECTRAL DENSITY, FREQUENCY, WIND SPEED, PROBE   ***
C***   HEIGHT AND VELOCITY CALIBRATION DATA.  THE PROGRAM WILL ALSO    ***
C***   PROVIDE PRINTER AND CALCOMP PLOTS OF EPSILON VERSUS HEIGHT.     ***
C***                                                                   ***
C***                                                                   ***
C***                                                                   ***
C*************************************************************************
C*************************************************************************
C*************************************************************************
C
C
C
      REAL*8 LABEL/'        '/,TITLE(10),TITLED(12)
      DIMENSION X(3),Y(3)
C
CCCCC
CCCCCCC
CCCCCCC
CCCCC
      DATA ALPHA,VONKAR/2.0408,0.40/
      VCUBED = 0.148**3
      PI = 2.*3.14159
      DO 20 I=1,3
      X(I)=0.0
      Y(I)=0.0
   20 CONTINUE
C
CCC
C
      READ (5,30) TITLE
   30 FORMAT (10A8)
C
CCC
C
      READ (5,35) TITLED
   35 FORMAT (6A8)
C
C
```

```
C     VARIOUS STAGES OF THE EXPERIMENT.  A DESCRIPTION OF THE SETTINGS
CC    FOLLOWS:
CCC
CCC      GAIN 1 REPRESENTS THE SIGNAL AMPLIFICATION PRIOR TO RECORD
CCC
CCC      GAIN 2 REPRESENTS THE AMPLIFICATION DURING ANALOG TO DIGITAL CONVERSION
CCC
CCC      SCALE REPRESENTS THE SCALE FACTOR USED TO CONVERT FROM VOLTAGE OUTPUT
CCC      TO DIGITAL OUTPUT DURING THE SDS 9300 TO IBM 360 CONVERT
CCC      STAGE
C
      GAIN1=0.1
      GAIN2=0.02
      SCALE=100./(2**23)
      I=1
      WRITE (6,40)
   40 FORMAT ('1',T8,'PHI11',T24,'FREQ',T39,'UBAR',T57,'Z',T71,'WAVE NO'
     1,T88,'EPSILON',T104,'USTAR',T120,'EPSILON(S)')
      WRITE (6,50)
   50 FORMAT ('0',10X)
      WRITE (6,50)
C
CCC   READ THE DATA VALUES FOR THE ENERGY SPECTRUM, FREQUENCY, MEAN WIND SPEED,
CCC   PROBE HEIGHT, NUMBER OF PROBE LEVELS AND VELOCITY CALIBRATION FACTOR
C
   60 READ (5,70,END=90) PHI11,F,UBAR,Z,N,C,FSUBS
   70 FORMAT (E10.3,3F10.3,I1,F10.3,F10.3)
C
CCC   THE CALIBRATION FACTOR PROVIDES THE DIMENSIONAL SCALING
C
      CAL=(SCALE*GAIN1*GAIN2*C)**3
C
CCC   COMPUTE WAVE NUMBER, EPSILON, AND USTAR VALUES
C
      WAVENO = PI*F/UBAR
      PHI=F*PHI11
      EPSLO1=(ALPHA*PHI*WAVENO**0.666667)**1.5
      EPSLO2=EPSLO1*CAL
      USTAR=(EPSLO2*VONKAR*Z)**0.33333
      WSUBS = PI*FSUBS/UBAR
      EKSUBS = (WSUBS**4)*VCUBED
      WRITE (6,80) PHI11,F,UBAR,Z,WAVENO,EPSLO2,USTAR,EKSUBS
   80 FORMAT ('0',T5,E11.4,7(3X,F13.7))
      X(I)=ALOG10(Z)
      Y(I)=ALOG10(EPSLO2)
      I=I+1
      GO TO 60
   90 WRITE (6,100)
```

```
100 FORMAT ('1',T20,'GRID COORDINATES')
    WRITE (6,50)
    WRITE (6,110)
110 FORMAT ('0',T15,'X VALUES',T38,'Y VALUES')
    DO 130 I=1,N
    WRITE (6,120) X(I),Y(I)
120 FORMAT ('0',T10,F13.7,10X,F13.7)
130 CONTINUE
    WRITE (6,140)
140 FORMAT ('1',10X)
    CALL PLOTP (X,Y,3,0)
    WRITE (6,150) TITLE
150 FORMAT ('0',10A8)
    CALL DRAW (3,X,Y,0,1,LABEL,TITLED,0.5,0.5,0,0,0,0,9,9,0,LAST)
    STOP
    END
```

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11. Mr. Steve Rinard — 1
Department of Meteorology
Naval Postgraduate School
Monterey, California 93940

12. Mr. Robert Smith — 1
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Chairman, Department of Oceanography
Naval Postgraduate School
Monterey, California 93940

16. LT Michael P. Cavanaugh — 1
c/o Mr. James A. Cavanaugh
3607 Husted Drive
Chevy Chase, Maryland 20015

17. LT Patrick T. Welsh — 1
Student, Naval Destroyer School
Naval Station
Newport, Rhode Island 08240

18. R/V ACANIA — 1
Department of Oceanography
Naval Postgraduate School
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Marine Boundary Layer
Dissipation of Turbulent Kinetic Energy
Momentum Flux
Friction Velocity

20. ABSTRACT *(Continue on reverse side if necessary and identify by block number)*

Velocity and temperature fluctuation measurements were made over the open ocean from instruments mounted on the R/V ACANIA. These data were examined to determine the validity of present formulations and prediction techniques.

Values of momentum flux, u_*^2, were inferred from the rate of dissipation of turbulent kinetic energy, ε. Dissipation values were obtained from spectral estimates and inner scale estimates. Values of u_* were examined for representativeness on the basis of the constant-flux assumption and by comparisons

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with other studies. The vertical variation of the dissipation rate was examined for possible effects of stability and wind-wave coupling.

The momentum flux, computed from spectra, supported the constant-flux assumption for neutral conditions. For periods of instability, the stability corrections applied to the vertical variation of ε resulted in the proper adjustments toward the predicted slope. The reductions in momentum transfer during periods of stable stratifications were consistent with wind-wave coupling effects described by Davidson. The shape of a spectrum of temperature fluctuations was in agreement with predictions.